

Page 4	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2013	9709	11

<p>1 (i) $64 + 576x + 2160x^2$</p> <p>(ii) $576a(x^2) + 2160(x^2) = 0$ $a = -\frac{2160}{576}$ oe (eg $-\frac{15}{4}$) or -3.75</p>	<p>B1B1B1 [3]</p> <p>M1</p> <p>A1 [2]</p>	<p>Can score in (ii)</p>
<p>2 Attempt integration</p> <p>$f(x) = 2(x+6)^{\frac{1}{2}} - \frac{6}{x} (+c)$</p> <p>$2(3) - \frac{6}{3} + c = 1$</p> <p>$c = -3$</p>	<p>M1</p> <p>A1A1</p> <p>M1</p> <p>A1 [5]</p>	<p>Accept unsimplified terms</p> <p>Sub. $x = 3, y = 1$. c must be present</p>
<p>3 (i) DB = $6\mathbf{i} + 4\mathbf{j} - 3\mathbf{k}$ cao DE = $3\mathbf{i} + 2\mathbf{j} - 3\mathbf{k}$ cao</p> <p>(ii) DB.DE = $18 + 8 + 9 = 35$ $\mathbf{DB} = \sqrt{61}$ or $\mathbf{DE} = \sqrt{22}$ $35 = \sqrt{61} \times \sqrt{22} \times \cos \theta$ oe $\theta = 17.2^\circ$ (0.300 rad) cao</p>	<p>B1</p> <p>B1 [2]</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1 [4]</p>	<p>Use of $x_1x_2 + y_1y_2 + z_1z_2$</p> <p>Correct method for moduli</p> <p>All connected correctly</p> <p>Use of e.g. BD. DE can score M marks (leads to obtuse angle)</p>
<p>4 (i) $4(1 - \cos^2 x) + 8\cos x - 7 = 0$ $4c^2 - 8c + 3 = 0 \rightarrow (2\cos x - 1)(2\cos x - 3) = 0$ $x = 60^\circ$ or 300°</p> <p>(ii) $\frac{1}{2}\theta = 60^\circ$ (or 300°) $\theta = 120^\circ$ only</p>	<p>M1</p> <p>M1</p> <p>A1A1 [4]</p> <p>M1</p> <p>A1 [2]</p>	<p>Use $c^2 + s^2 = 1$</p> <p>Attempt to solve</p> <p>Allow 300° in addition</p>
<p>5 (i) $x = (\pm)\sqrt{y-1}$ $f^{-1} : x \mapsto \sqrt{x-1}$ for $x > 1$</p> <p>(ii) $ff(x) = (x^2 + 1)^2 + 1$ $x^2 + 1 = (\pm)13/4$ $x = 3/2$</p> <p>Alt. (ii) $f(x) = f^{-1}(185/16) = 13/4$ M1 $x = f^{-1}(13/4)$ M1 $x = 3/2$ A1</p>	<p>B1</p> <p>B1B1 [3]</p> <p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>OR $y^2 = x - 1$ (x/y interchange 1st)</p> <p>Or $x^4 + 2x^2 - (153/16) = 0$</p> <p>Or $x^2 = 9/4, (-17/4)$</p> <p>www. Condone $\pm 3/2$</p> <p>Alt. (ii) $f(3/2) = 13/4$ B1 $f(13/4) = 185/16$ B1 $x = 3/2$ B1 SC.B2 answer 1.5 with no working</p>

Page 5	Mark Scheme	Syllabus	Paper
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<p>6 (i) $r(2\pi - \alpha) + 2r\alpha + 2r$ $2\pi r + r\alpha + 2r$</p> <p>(ii) $\frac{1}{2}(2r)^2\alpha + \pi r^2 - \frac{1}{2}r^2\alpha$ $\frac{3r^2\alpha}{2} + \pi r^2$</p> <p>(iii) $\pi r^2 - \frac{1}{2}r^2\alpha = 2r^2\alpha$ $\alpha = \frac{2}{5}\pi$</p>	<p>B1B1 B1^h [3]</p> <p>B1B1 B1 [3]</p> <p>M1 A1 [2]</p>	<p>fit for $r\alpha$ instead of $2r\alpha$ or omission $2r$ SC1 for $2r\alpha + 4r$. (Plate = shaded part)</p> <p>Either B1 can be scored in (iii)</p> <p>For equating <i>their</i> 2 parts from (ii)</p>	
<p>7 (i) mid-point = (3, 4) Grad. $AB = -\frac{1}{2} \rightarrow$ grad. of perp., = 2 $y - 4 = 2(x - 3)$ $y = 2x - 2$</p> <p>(ii) $q = 2p - 2$ ^h $p^2 + q^2 = 4$ oe $p^2 + (2p - 2)^2 = 4 \rightarrow 5p^2 - 8p = 0$ {OR $\frac{1}{4}(q + 2)^2 + q^2 = 4 \rightarrow 5q^2 + 4q - 12 = 0$ } (0, -2) and $\left(\frac{8}{5}, \frac{6}{5}\right)$</p>	<p>B1 M1 M1 A1 [4]</p> <p>B1^h B1 M1 A1A1 [5]</p>	<p>soi For use of $-1/m$ soi fit on <i>their</i> (3, 4) and 2</p> <p>fit for 1st eqn. Attempt substn (linear into quadratic) & simplify</p>	
<p>8 (i) $A = 2xr + \pi r^2$ $2x + 2\pi r = 400 (\Rightarrow x = 200 - \pi r)$ $A = 400r - \pi r^2$</p> <p>(ii) $\frac{dA}{dr} = 400 - 2\pi r$ $= 0$ $r = \frac{200}{\pi}$ oe $x = 0 \Rightarrow$ no straight sections AG $\frac{d^2A}{dr^2} = -2\pi (< 0)$ Max</p>	<p>B1 B1 M1A1 [4]</p> <p>B1 M1 A1 A1 B1 [5]</p>	<p>Subst & simplify to AG (www)</p> <p>Differentiate Set to zero and attempt to find r</p> <p>Dep on -2π, or use of other valid reason</p>	

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<p>9 (a) $\frac{10}{2}(2a+9d) = 400$ oe $\frac{20}{2}(2a+19d) = 1400$ OR $\frac{10}{2}[2(a+10d)+9d] = 1000$ $d = 6$ $a = 13$</p> <p>(b) $\frac{a}{1-r} = 6$ $\frac{2a}{1-r^2} = 7$ $\frac{12(1-r)}{1-r^2} = 7$ or $\frac{1-r^2}{1-r} = \frac{12}{7}$ $r = \frac{5}{7}$ or 0.714 $a = \frac{12}{7}$ or 1.71(4)</p>	<p>B1</p> <p>B1</p> <p>M1A1A1 [5]</p> <p>B1B1</p> <p>M1</p> <p>A1</p> <p>A1^h [5]</p>	<p>$\rightarrow 2a + 9d = 80$</p> <p>$\rightarrow 2a + 19d = 140$ or $2a + 29d = 200$</p> <p>Solve sim. eqns both from S_n formulae</p> <p>Substitute or divide</p> <p>Ignore any other solns for r and a</p>
<p>10 (i) $\frac{dy}{dx} = [3(3-2x)^2] \times [-2]$ At $x = \frac{1}{2}$, $\frac{dy}{dx} = -24$ $y - 8 = -24\left(x - \frac{1}{2}\right)$ $y = -24x + 20$</p> <p>(ii) Area under curve = $\left[\frac{(3-2x)^4}{4}\right] \times \left[-\frac{1}{2}\right]$ $-2 - \left(-\frac{81}{8}\right)$ Area under tangent = $\int(-24x + 20)$ $= \left -12x^2 + 20x\right$ or 7 (from trap) $\frac{9}{8}$ or 1.125</p>	<p>B1B1</p> <p>M1</p> <p>DM1</p> <p>A1 [5]</p> <p>B1B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1 [6]</p>	<p>OR $-54 + 72x - 24x^2$ B2,1,0</p> <p>OR $27x - 27x^2 + 12x^3 - 2x^4$ B2,1,0</p> <p>Limits $0 \rightarrow \frac{1}{2}$ applied to integral with intention of subtraction shown or area trap = $\frac{1}{2}(20 + 8) \times \frac{1}{2}$</p> <p>Could be implied</p> <p>Dep on both M marks</p>