

Page 4	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – October/November 2012	9709	73

1	Normal with mean 28 Var = $0.12^2 \times 8$ = 0.115 (3 sfs)	B1 M1 A1	[3]	Both square & \times by 8 or sd = $0.12 \times \sqrt{8}$ or sd = 0.339 (3 sfs) clearly stated var / sd
Total			[3]	
2 (i)	μ $\frac{\sigma^2}{n}$	B1 B1	[2]	(as an expression) (as an expression) SC If B0B0 scored, $N(\mu, \frac{\sigma^2}{n})$ scores B1
(ii)	$\frac{176-177.8}{6.1}$ (= -1.022) $\frac{1}{\sqrt{12}}$	M1		Standardise with $\sqrt{12}$ Accept 'totals' method. No mixed methods. (2112 – 2133.6) / $\sqrt{(6.1^2 \times 12)}$
	$\Phi(-1.022) = 1 - \Phi(1.022)$ = 0.153 (3 sfs)	M1 A1	[3]	Correct area (consistent with working)
(iii)	No; X norm distr'd or pop norm distr'd Or hts norm distr'd Or original dist normal	B1	[1]	Need 'No' stated or implied AND correct reason NB 'No, because small sample' scores B0 NB 'it is normally distr'd' scores B0
Total			[6]	
3 (i)	$\left(\frac{5}{6}\right)^{25} + 25\left(\frac{5}{6}\right)^{24}\left(\frac{1}{6}\right)$ = 0.0629 final answer Sig level = 6.29%	M1 A1 B1ft	[3]	Allow end errors, but just P(2) implies M0 Accept p/q mix ft their $P(X \leq 1)$ with Binomial used. Allow 6.3% or 6%
(ii)	Var (p) $\approx \frac{0.09 \times 0.91}{100}$ (= 0.000819) $z = 1.96$ $0.09 \pm z\sqrt{\frac{0.09 \times 0.91}{100}}$ = 0.034 to 0.146 (3 dps)	M1 B1 M1 A1	[4]	For pq /100 seen (any p/q) (must be probs) For correct form of C.I. (any p/q) (must be probs)
Total			[7]	

Page 5	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – October/November 2012	9709	73

4	<p>Use of $X_1 - 2X_2$ or similar $E(X_1 - 2X_2) = 180 - 360 (= -180)$</p> <p>$\text{Var}(X_1 - 2X_2) = 5 \times 1550$ or 7750</p> <p>$\frac{0 - (-180)}{\sqrt{7750}}$ or $\frac{0 - 180}{\sqrt{7750}}$ $(= \pm 2.045)$</p> <p>$1 - \Phi('2.045')$ $= 0.0205$ or 0.0204</p> <p>Ans 0.041 (2 sf)</p>	<p>B1</p> <p>M1 A1</p> <p>M1</p> <p>M1 A1</p> <p>B1ft</p>	[7]	<p>Or use of $\frac{1}{2} X_1 - X_2$ $E(2X_1 - X_2) = 360 - 180 (= 180)$ Or $E(\frac{1}{2} X_1 - X_2) = 90 - 180 = (-90)$ for $1550 + 4 \times 1550$ or $\frac{1}{4} \times 1550 + 1550$ 7750 or 1937.5</p> <p>Allow incorrect var (dep > 0 & $\neq 1550$), no $\sqrt{\quad}$ Standardising – no mixed methods Or $\pm (0 - -90) / \sqrt{1937.5}$</p> <p>For finding correct area (consistent with working)</p> <p>Allow double their prob</p>
Total			[7]	
5 (i)	<p>Est(μ) = 2.3</p> <p>Est(σ^2) = $\frac{200}{199} \left(\frac{1636}{200} - \left(\frac{460}{200} \right)^2 \right)$</p> <p>= 2.90 (3 sf) or 2.91 or 578/199</p>	<p>B1</p> <p>M1</p> <p>A1</p>	[3]	<p>Allow $\sqrt{\frac{200}{199} \left(\frac{1636}{200} - \left(\frac{460}{200} \right)^2 \right)}$ or 1.7043 for M1 Or $1/199 (1636 - 460^2/200)$</p>
(ii)	<p>H_0: Pop mean wt loss = 2 kg H_1: Pop mean wt loss > 2 kg</p> <p>$\frac{2.3 - 2}{\sqrt{\frac{2.9045}{200}}}$</p> <p>= 2.489 or ± 2.49 or 0.0064 / 0.9936 for area comparison or $x_{\text{crit}} = 2.28(03)$</p> <p>comp $z = 2.326$</p> <p>Evidence that mean wt loss > 2 kg</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1ft</p>	[5]	<p>Allow 'μ' but not just 'mean'</p> <p>$\frac{2.3 - 2}{\sqrt{\frac{1.7043}{200}}}$ Stand'ise with $\sqrt{200}$. Accept sd/var mixes Or $x_{\text{crit}} = 2 + 2.326\sqrt{(2.9045/200)}$</p> <p>For valid comparison (z or area or x_{crit})</p> <p>No contradictions Reject H_0 / accept H_1 only if H_0 / H_1 correctly defined If $\frac{200}{199}$ not used in (i): var = 2.89, sd = 1.7, cr $z = 2.496$ can score all marks</p>
Total			[8]	

Page 6	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – October/November 2012	9709	73

6 (i)	$f(x) \geq 0$ for all x defined	B1		
	$\int_0^a \frac{2}{a^2} x dx$	M1		Attempt $\int f(x) dx$ with limits $0, a$. Must be a .
	$\left(= \left[\frac{2x^2}{2a^2} \right]_0^a \right)$ $= 1$	A1	[3]	Or equivalent methods (e.g. by areas)
(ii)	$\int_0^a \frac{2}{a^2} x^2 dx (= 8)$	M1		Attempt $\int xf(x) dx$, ignore limits
	$\frac{2}{a^2} \left[\frac{x^3}{3} \right]_0^a (= 8)$	A1		Correct integrand and limits
	$\left(\frac{2a}{3} = 8 \right)$ $a = 12$	A1	[3]	
(iii)	$1 - \int_0^6 \frac{2}{144} x dx$ or $\int_6^{12} \frac{2}{144} x dx$	M1		Correct expr'n incl limits; ft their ' a '
	$= 1 - 1 - \frac{1}{72} \left[\frac{x^2}{2} \right]_0^6$ or	A1ft		Correct integrand and limits; ft their ' a '
	$\frac{1}{72} \left[\frac{x^2}{2} \right]_6^{12}$ $= \frac{3}{4}$	A1ft	[3]	ft their ' a ', dep $0 < \text{ans} < 1$
Total			[9]	

Page 7	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – October/November 2012	9709	73

7 (i)	$n > 50$	B1		Accept n large
	$np = 0.8$, which is < 5	B1	[2]	Accept p small
(ii)	$\lambda = 9.6$	B1		
	$e^{-9.6} \left(\frac{9.6^3}{3!} + \frac{9.6^4}{4!} + \frac{9.6^5}{5!} \right)$	M1		Any λ Accept end errors.
	$= 0.0800$ (3 sfs)	A1	[3]	Allow 0.08
(iii)	H_0 : Pop mean for 10 days = 8 H_1 : Pop mean for 10 days < 8	B1		or Pop mean for 1 day = 0.8 Pop mean for 1 day < 0.8 Allow λ or μ but not just 'mean'
	$e^{-8} \left(1 + 8 + \frac{8^2}{2!} \right)$	M1		Any λ . Accept end errors. NB P(2) only used scores M0M0 Accept CR method
	$= 0.0138$ or 0.0137	A1		CR = 0, 1, 2 all working must be shown
	Compare 0.02 Evidence that mean number of absentees has decreased	M1 A1ft		Valid comparison with 0.02 or CR No contradictions Reject H_0 / accept H_1 only if H_0 / H_1 correctly defined
			[5]	
Total			[10]	
	Total for paper		[50]	