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1 (i)	$(12 + 8)OG =$ $\pm [8 \times 0.6/(\pi/2) - 12 \times (2 \times 0.6)/(3\pi/2)]$ $OG = 0 \text{ m}$	M1 A1 A1	[3]	Table of values or equates moments Signs either way round
(ii)	$(12 + 8) \times 0.6\sin 30 = F(0.6 + 0.6\cos 30)$ $F = 5.36$	M1 A1 A1	[3]	Moments about A
2 (i)	$[60 \times 2^2/(2 \times 2)] + 0.6v^2/2 =$ $0.6g(6 - 2 \times 2) + [60 \times 2^2/(2 \times 2)]$ $v = 6.32 \text{ ms}^{-1}$	M1 A1	[2]	PE/KE(/EE) balance (EE terms may be omitted or wrong but equal) ($v = \sqrt{40}$)
(ii)	$60e/2 = 60(2-e)/2 \pm 0.6g$ Upper ext = 1.1, Lower ext = 0.9 Distance from $A = 3.1 \text{ m}$ $0.6g \times 1.1 + 60(2^2 - 0.9^2)/4$ $= 60 \times 1.1^2/4 + \text{KE}$ KE = 36.3 J OR $\text{KE} - 0.6(6.32)^2/2 = 60 \times 2^2/4$ $- 60 \times 1.1^2/4 - 60 \times 0.9^2/4 - 0.6g \times 0.9$ KE = 36.3 J	M1 A1 A1 M1 A1 \checkmark A1 M1 A1ft A1	[6]	Attempt to find equilibrium position Energy balance, descent from A . \checkmark cv upper and lower ext Energy balance, descent from A . \checkmark cv upper and lower ext, answer (i)

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3 (i)	$t = 2/(25\cos 70) (= 0.234)$ $y = (25\sin 70) \times 0.234 - g \times 0.234^2 / 2$ $y = 5.22$ OR $y = x \tan 70 - gx^2 / 2(25\cos 70)^2$ $y = 2 \tan 70 - g2^2 / 2(25\cos 70)^2$ $y = 5.22$	B1 M1 A1 B1 M1 A1	[3]	$s = ut + gt^2 / 2$ Award if seen in (i)
(ii)	$1.2 = (25\sin 70)t - gt^2 / 2$ $5t^2 - 23.5t + 1.2 = 0$ $t = 4.65 \text{ s}$	B1 M1 A1	[3]	Solves 3 term quadratic for larger root
(iii)	$R = 15^2 \sin 2\alpha / 10 = 20$ $\alpha = 31.4^\circ$	M1 A1	[2]	Or solves $(15\sin \alpha)t - 5t^2 = 0$ and $20 = (15\cos \alpha)t$ for α
4 (i)	$(0.9/2)/r = \tan 45$ $r = 0.45 \text{ m}$	M1 A1	[2]	
(ii)	$(\pi 0.9^2 \times 0.9 + \pi 0.45^2 h)OG$ $= \pi 0.9^2 \times 0.9(h + 0.45) + \pi 0.45^2 h \times h/2$ $OG = \frac{0.9^3 h + 0.9^3 \times 0.45 + 0.45^2 h^2}{2}$ $OG = (25h^2 + 180h + 81)/(50h + 180)AG$	M1 A1 \checkmark A1	[3]	Take moments about A \checkmark cv(0.45)
(iii)	$0.45/OG = \frac{1}{2}$ $0.9 = (25h^2 + 180h + 81)/(50h + 180)$ $h = 0.545$	M1 DM1 A1	3	

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5 (i)	(a) $T \cos 60 = 7 \cos 60 - 0.2g$ $T = 3 \text{ N}$	M1 A1	[2]	Resolves vertically for B
	(b)	M1		Newton's Second Law with 2 forces resolved horizontally
	$7 \sin 60 + 3 \sin 60 = 0.2v^2 / 0.6$ $v = 5.1(0) \text{ ms}^{-1}$	A1 $\sqrt{\quad}$ A1	[3]	$\sqrt{\quad} \text{ cv}(3)$
5 (ii)	$T_P \cos 60 - T_Q \cos 60 = 0.2g$	B1		Resolves vertically for B
	$T_P \sin 60 + T_Q \sin 60 = 0.2 \times 7^2 \times 0.6$	B1		or RHS = $0.2 \times (7 \times 0.5)^2 / 0.5$
	$T_P - T_Q = 4$ and $T_P + T_Q = 6.78(96..)$	M1		Solves 2 SE for T_Q
	$T_Q = 1.39 \text{ N}$	A1	[4]	
6 (i)	$0.4 \text{ dv}/\text{dt} = T - 0.4g \times 0.5 - 0.9v$	B1		Not awarded for N2L round corner
	$0.2 \text{ dv}/\text{dt} = 0.2g - T - 0.9v$	B1		Not awarded for N2L round corner
	$0.6 \text{ dv}/\text{dt} = 0.2g - 0.4g \times 0.5 - 1.8v$	M1		Awarded for N2L round corner
	$\text{dv}/\text{dt} = -3v$ AG	A1	[4]	
6 (ii)	$\int \text{dv}/v = \int -3 \text{ dt}$	M1		Separates variables, integrates
	$\ln v = -3t (+ c)$	A1		Accurate integrals
	$c = \ln 5$	B1		Or $[\ln v]_5^{2.5} = [-3t]_0^t$ implied
	$t = 0.231$	A1		$(\ln 2)/3$
	$\int \text{dx} = \int e^{-3t} \text{ dt}$	M1		Attempts integration of $v(t)$
	$x = -[e^{-3t}]_0^{0.231} / 3$	A1		Correct integral and limits
	$x = 0.833 \text{ m}$	A1	[7]	5/6 m
	OR			
	$v \text{ dv}/\text{dx} = -3v, \text{ dv}/\text{dx} = -3$	M1		Attempts integration
	$\int \text{dv} = \int -3 \text{ dx}$			
$[v]_5^{2.5} = [-3x]_0^x$	A1		Correct integral and limits	
$x = 0.833 \text{ m}$	A1		Accept 5/6m	