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1		M1	For using $WD = Fd \cos \alpha$
	$WD = 45 \times 25 \cos 14^\circ$	A1	
	Work done is 1090 J (1.09 kJ)	A1	3
2	(i) $[0.6 = 0 + 0.3a]$	M1	For using $v = 0 + at$
	Acceleration is 2 ms^{-2}	A1	2
	(ii) $[mg - T = 2m, T - (1 - m)g = 2(1 - m)]$	M1	For applying Newton's 2 nd law to A or to B
	$[m = T/8 \rightarrow T - (10 - 1.25T) = 2 - 0.25T]$ or $T = 8m \rightarrow 8m - (10 - 10m) = 2 - 2m]$	M1	For eliminating or evaluating m
	$T + 1.25T + 0.25T = 10 + 2$ or $m = 0.6$ and $T = 8m$	A1	
	$m = 0.6$ and tension is 4.8 N	A1	4
Alternative for part (ii)			
	$[\{m + (1 - m)\} \times 2 = \{m - (1 - m)\} \times g]$	M1	For using $(m_A + m_B)a = (m_A - m_B)g$
	$m = 0.6$	A1	
	$[mg - T = 2m$ or $T - (1 - m)g = 2(1 - m)]$	M1	For applying Newton's 2 nd law to A or to B, substituting for m and solving for T
	Tension is 4.8 N	A1	

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3		M1	For using $s = ut + \frac{1}{2}at^2$ for AB or AC
	$55 = 5u + 12.5a$	A1	
	$(55 + 65) = 10u + 50a$ or $65 = 5v_B + 12.5a$ and $v_B = u + 5a$	A1	
		M1	For solving for a or u
	$a = 0.4$ (or $u = 10$)	A1	
	$u = 10$ (or $a = 0.4$)	A1ft	6
Alternative			
	$v_B = (55 + 65) \div (5 + 5)$	M1	For calculating the speed at B as the mean speed for the motion from A to C .
	$v_B = 12\text{ms}^{-1}$	A1	
	For calculating the speed at X , where X is the point where the car passes 2.5 s after passing through A , as $55 \div 5 = 11\text{ms}^{-1}$	B1	
	$[a = (12 - 11) \div 2.5]$	M1	For using $a = (v_B - v_X) \div 2.5$
	$a = 0.4$	A1	
	$u = v_X - a \times 2.5 = 11 - 0.4 \times 2.5 = 10$	B1	
4	(i) $[Y_1^2 = 68^2 - (-60)^2, Y_3^2 = 100^2 - 96^2$ $Y_1 = 68\sin 28.1^\circ, Y_3 = 100\sin 16.3^\circ]$	M1	For using $Y^2 = F^2 - X^2$ or for finding the angles (say α and β) between the forces of magnitudes 68 and 100, respectively, and the x -axis. Then find the two relevant magnitudes from $68\sin\alpha$ and $100\sin\beta$
	For correct magnitudes (32, 75, 28)	A1	Can be scored by implication if the final A1 is scored for the correct answer to part (i)
	Components are -32, 75 and -28	A1ft	3
	(ii) $[R^2 = (-60 + 0 + 96)^2 + (-32 + 75 - 28)^2]$	M1	For using $R^2 = X^2 + Y^2$
	Magnitude is 39 N	A1	
$[\theta = \tan^{-1}\{(-32 + 75 - 28) \div (-60 + 0 + 96)\}]$	M1	For using $\theta = \tan^{-1}(Y/X)$	
Direction is 22.6° (or 0.395rad^c) anticlockwise from +ve x -axis.	A1	4	Accept just '22.6 from x -axis' or just ' $\theta = 22.6$ '

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5	(i) Acceleration for $t < 0.8$ is $4/0.8$	B1		
	$[5 = 10\sin \theta]$	M1	For using $a = g\sin \theta$	
	$\theta = 30^\circ$	A1		3
Alternative for part (i)				
(i)	$[mgh = \frac{1}{2} m4^2$ and $s = \{(0 + 4) \div 2\} \times 0.8]$	M1	For using PE loss = KE gain and $s \div t = (u + v) \div 2$ (A to B)	
	$\sin\theta = 0.8/1.6$	A1		
	$\theta = 30^\circ$	A1		
(ii)	Acceleration for $0.8 < t < 4.8$ is			
	$-4/(4.8 - 0.8)$	B1		
	$[mg\sin 30^\circ - F = m(-1)]$	M1	For using Newton's second law	
		M1	For using $\mu = F / R$	
	$\mu = \frac{mg \sin 30^\circ + m}{mg \cos 30^\circ}$	A1ft	ft following a wrong answer for θ in part (i)	
	Coefficient is 0.693	A1		5 Accept 0.69

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6	(i)			For using $DF = 30000/v$
		$[30000/v - 1000 - 1250g \times 30/500 = 1250a]$	M1	For using Newton's 2 nd law
		$v_{\text{bottom}} = 30000/(1250 \times 4 + 1000 + 750)$ and $v_{\text{top}} = 30000/(1250 \times 0.2 + 1000 + 750)$	M1 A1	
		$[\frac{1}{2} 1250(15^2 - 4.44\dots^2)]$	M1	For using KE gain = $\frac{1}{2} m(v_{\text{top}}^2 - v_{\text{bottom}}^2)$
		Increase in KE is 128000 J (128 kJ)	A1	5
Alternative for part (i)				
	(i)	$[F - 1000 - 1250g \times 30/500 = 1250a]$	M1	For using Newton's second law to find the driving force at the bottom and the top
		$F_{\text{bottom}} = 1250 \times 4 + 1000 + 750 = 6750$ and $F_{\text{top}} = 1250 \times 0.2 + 1000 + 750 = 2000$	A1	
		$[v_{\text{bottom}} = 30000/6750 \text{ and } v_{\text{top}} = 30000/2000]$	M1	For using $DF = 30000/v$ to find v_{bottom} and v_{top}
		$[\frac{1}{2} 1250(15^2 - 4.44\dots^2)]$	M1	For using KE gain = $\frac{1}{2} m(v_{\text{top}}^2 - v_{\text{bottom}}^2)$
		Increase in KE is 128000 J (128 kJ)	A1	
	(ii)	PE gain = $1250g \times 30$ and WD against resistance = 1000×500	B1	
		$[WD_{\text{car}} = 128000 + 375000 + 500000]$	M1	For using WD by car's engine = KE gain + PE gain + WD against resistance
		Work done is 1000 000 J (1000 kJ)	A1ft	3 ft incorrect answer in (i)
<u>Special Ruling</u> applying to part (i) for candidates who omit the weight component in applying Newton's second law. (Max 3 out of 5)				
	(i)	$v_{\text{bottom}} = 30000/(1250 \times 4 + 1000)$ and $v_{\text{top}} = 30000/(1250 \times 0.2 + 1000)$	B1	
		$[\frac{1}{2} 1250(24^2 - 5^2)]$	M1	For using KE gain = $\frac{1}{2} m(v_{\text{top}}^2 - v_{\text{bottom}}^2)$
		Increase in KE is 344000 J (344 kJ)	A1	

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7	(i)	$dv/dt = k(120t - 3t^2)$	B1		
		$[v(40) = k(60 \times 40^2 - 40^3) = 6.4]$	M1		For finding v_{\max} as the value of v when $dv/dt = 0$ and $t \neq 0$ and equating with 6.4
		$k = 0.0002$	A1	3	AG
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	(ii)	$t = 60$ at A	B1		
			M1		For integrating $v(t)$ to find $s(t)$
		$s(t) = 0.0002(20t^3 - t^4/4) + C$	A1		
		$[OA = 0.0002 \times (20 \times 60^3 - 60^4/4)]$	M1		For using limits 0 to 60 or evaluating $s(t)$ when $t = 60$ with $C = 0$ (which may be implied by its absence)
		Distance is 216 m	A1	5	
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	(iii)	$[dv/dt = 0.0002(120 \times 60 - 3 \times 60^2)]$	M1		For evaluating dv/dt when $t = 60$
		Magnitude of acceleration is 0.72 ms^{-2}	A1	2	Accept $a = -0.72 \text{ ms}^{-2}$
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	(iv)	$[20t^3 - 0.25t^4 = 0,$ $v = 0.0002(60 \times 80^2 - 80^3)]$	M1		For attempting to solve $s(t) = 0$ for non-zero t and substituting into $v(t)$.
		Speed is 25.6 ms^{-1}	A1	2	