

Page 4	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2012	9709	13
1	$7C3 \times 2^4 \times \left(-\frac{x}{2}\right)^3$ powers 4 and 3 35 seen or implied -70	M1 B1 A1 [3]	
2	$f'(x) = -3x^{-4} - 3x^2$ $< 0 \Rightarrow$ decreasing function	B1 B1 B1 [3]	Dependent upon minus signs & even powers
3	$7 \cos x + 5 = 2(1 - \cos^2 x)$ $(2 \cos x + 1)(\cos x + 3) = 0$ $\cos x = -0.5$ $x = 120^\circ, 240^\circ$	M1 A1 A1 A1 $\checkmark$ [4]	Use of $c^2 + s^2 = 1$ ft for $360 - 1^{\text{st}}$ solution
4	area $\Delta = 2\sqrt{3}$ $\tan A = \frac{2\sqrt{3}}{2} \Rightarrow A = \frac{\pi}{3}$ Area sector $= \frac{1}{2} \times 2^2 \times \frac{\pi}{3} = \frac{2\pi}{3}$ Shaded area $= 2\sqrt{3} - \frac{2\pi}{3}$	B1 B1 M1 A1 [4]	Accept $60^\circ$ Use of $\frac{1}{2}r^2\theta$ with $\theta$ in radians cao
5	(i) $2\frac{1}{4} = 5\frac{1}{3}r^3$ $r^3 = \frac{9}{4} \times \frac{3}{16} = \frac{27}{64}$ $r = \frac{3}{4}$ or 0.75  (ii) $S_\infty = \frac{5\frac{1}{3}}{1 - \frac{3}{4}} = \frac{64}{3}$ (or $21\frac{1}{3}$ or 21.3)	M1 A1 A1 [3] M1 A1 [2]	cao
6	(i) $\cos\left(\frac{1}{2}x + \frac{\pi}{6}\right) (= 1)$ $x = -\frac{\pi}{3}$  (ii) $\frac{1}{2}\cos x + \frac{\pi}{6} = 1$ $\cos x = 0.9528$ $x = \pm 0.31$	B1 B1 [2] B1 B1 B1 B1 $\checkmark$ [4]	cao $\checkmark$ for negative of first answer
7	(i) $11 - x^2 = 5 - x \Rightarrow x^2 - x - 6 (= 0)$ $(x + 2)(x - 3)$ $p = 3; q = 2$  (ii) $f^{-1}(x) = \begin{cases} \sqrt{11 - x} & \text{for } 2 \leq x \leq 11 \\ 5 - x & \text{for } x < 2 \end{cases}$	B1 B1 B1 [3] B1 B1 B1 B1 B1 [5]	oe cao

Page 5	Mark Scheme	Syllabus	Paper
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<p>8 (i) <math>f''(x)=[9] \times [(3x+4)^{\frac{1}{2}}] - [6]</math></p> <p>(ii) <math>f'(-1) = 2 + 6 - 8 = 0</math> hence stat value at <math>x = -1</math>  <math>f''(-1) = 9 - 6 = 3 &gt; 0</math> hence minimum</p> <p>(iii) <math>y = [\frac{4}{15} \text{ oe}] \times [(3x+4)^{\frac{5}{2}}] - [3x^2 + 8x] + (c)</math>  Sub <math>(-1, 5) \rightarrow \frac{4}{15} - 3 + 8 + c = 5 \rightarrow c = -\frac{4}{15}</math></p>	<p>B2,1,0 [2]</p> <p>B1 B1 [2]</p> <p>B1 B1 B1 M1 A1 [5]</p>	<p>1 each error</p> <p>AG</p> <p>allow unsimplified <math>\frac{4}{15}</math>  Dependent on <math>c</math> present cao</p>	
<p>9 (i) <math>p = 2</math>  Unit vector <math>\frac{1}{\sqrt{6}} \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix}</math> or <math>\frac{1}{\sqrt{24}} \begin{pmatrix} 4 \\ 2 \\ 2 \end{pmatrix}</math> oe</p> <p>(ii) <math>\overrightarrow{AB} = \begin{pmatrix} 4 \\ 2 \\ p \end{pmatrix} - \begin{pmatrix} p \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 4-p \\ 1 \\ p-1 \end{pmatrix}</math>  <math>\overrightarrow{OA} \cdot \overrightarrow{AB} = 0 \Rightarrow 4p - p^2 + 1 + p - 1 = 0</math>  <math>5p - p^2 = 0 \Rightarrow p = 0</math> or <math>5</math></p> <p>(iii) <math>\overrightarrow{OC} = \overrightarrow{OB} - \overrightarrow{OA} = \begin{pmatrix} 4 \\ 2 \\ 3 \end{pmatrix} - \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix}</math> oe <math>= \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}</math></p>	<p>B1 M1 A1 <math>\checkmark</math> [3]</p> <p>M1 A1 M1 A1 <math>\checkmark</math> A1 [5]</p> <p>M1 A1 [2]</p>	<p>ft for <i>their p</i></p> <p>ft from <i>their AB</i>  cao</p>	
<p>10 (i) <math>-2x + k = \frac{2}{x-3} \Rightarrow 2x^2 - (6+k)x + 2 + 3k = 0</math></p> <p>(ii) <math>(6+k)^2 - (4)(2)(2+3k) = 0</math>  <math>k^2 - 12k + 20 (=0)</math>  <math>(k-10)(k-2) = 0</math>  <math>k = 2</math> or <math>10</math></p> <p>(iii) <math>k = 2 \Rightarrow 2(x-2)^2 = 0</math>  <math>x = 2, y = -2</math> or <math>(2, -2)</math>  <math>k = 10 \Rightarrow 2(x-4)^2 = 0</math>  <math>x = 4, y = 2</math> or <math>(4, 2)</math>  AB: <math>y - 2 = 2(x - 4)</math> or <math>y + 2 = 2(x - 2)</math></p>	<p>B1 [1]</p> <p>M1 A1 A1 [3]</p> <p>M1 A1 M1 A1 M1 A1 [6]</p>	<p>AG</p> <p>Apply <math>b^2 - 4ac</math></p> <p>cao</p> <p><math>(y = 2x - 6)</math></p>	

Page 6	Mark Scheme	Syllabus	Paper
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<p><b>11 (i)</b> <math>a = 2</math></p> <p><b>(ii)</b> <math>y = x^3 - 4x^2 + 4x</math>  <math>\frac{dy}{dx} = 3x^2 - 8x + 4</math>  <math>(x - 2)(3x - 2) = 0</math>  <math>b = \frac{2}{3}</math></p> <p><b>(iii)</b> area = <math>\int y \, dx = \left[ \frac{x^4}{4} - \frac{4x^3}{3} + 2x^2 \right]</math>  <math>4 - \frac{32}{3} + 8</math>  <math>\frac{4}{3}</math></p> <p><b>(iv)</b> <math>\frac{d^2y}{dx^2} = 6x - 8 = 0 \Rightarrow x = \frac{4}{3}</math>  When <math>x = \frac{4}{3}</math>, <math>\frac{dy}{dx}</math> (or <math>m</math>) = <math>-\frac{4}{3}</math></p>	<p>B1 [1]</p> <p>B1 B2, 1, 0 ✓</p> <p>B1 [4]</p> <p>B2, 1, 0</p> <p>M1 A1 [4]</p> <p>M1 A1 DM1 A1 [4]</p>	<p>-1 for eeo</p> <p>cao</p> <p>-1 for eeo</p> <p>Apply limits <math>0 \rightarrow 2</math> – fit <i>their a</i> from <b>(i)</b> cao</p> <p>Attempt <math>\frac{d^2y}{dx^2}</math> and set = 0 cao</p>
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