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<p>1 $50 = a + b \times 54$</p> <p>$100 = b^2 \times 144$ or $10 = b \times 12$</p> <p>$b = \frac{5}{6}$ oe</p> <p>$a = 5$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1 [4]</p>	<p>Solving two simultaneous equations</p> <p>Both correct</p>
<p>2 $2 \times z \times \sqrt{\frac{0.35 \times 0.65}{n}} = 0.157$</p> <p>$z = 2.326$</p> <p>$n = 4 \times 2.326^2 \times 0.35 \times 0.65 \div 0.157^2$ (=199.738...)</p> <p>$n = 200$</p>	<p>M1</p> <p>M1</p> <p>B1</p> <p>M1</p> <p>A1 [5]</p>	<p>For $\sqrt{(pq/n)}$ in equation For equation of the form $2 \times z \times f(n) = 0.157$</p> <p>Rearrange to form $n = \dots$ from a correct equation in n, but allow any z and/or factor of “2” errors</p> <p>cao</p>
<p>3 (i) Number all members</p> <p>Explain the selection of 3-digit random numbers</p> <p>Omit repeats OR omit nos. over 750 (until have 8 nos.)</p>	<p>B1</p> <p>B1</p> <p>B1 [3]</p>	
<p>(ii) Est (μ) = 20</p> <p>Est (σ^2) = $\frac{8}{7} \left(\frac{3636}{8} - 20^2 \right)$</p> <p>= $\frac{436}{7}$ or 62.3 (3 sfs)</p>	<p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>$1/7 \times (3636 - 160^2/8)$</p> <p>$(7.89\dots)^2$ M1A1, but 7.89... only M1A0</p>
<p>(iii) Amounts spent last week in café by all club members</p>	<p>B1 [1]</p>	
<p>4 (i) $\int_0^1 ke^{-x} dx = 1$</p> <p>$[-ke^{-x}]_0^1 = 1$</p> <p>(= $-ke^{-1} - (-ke^0)$)</p> <p>= $k \times \frac{e-1}{e} = 1$ or $k(e-1) = e$</p> <p>$k = \frac{e}{e-1}$ AG</p>	<p>M1</p> <p>A1</p> <p>A1 [3]</p>	<p>Int = 1, ignore limits</p> <p>Correct integral & limits, & = 1</p> <p>Correctly obtained, no errors seen</p>

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<p>(ii) $\frac{e}{e-1} \int_0^1 xe^{-x} dx$</p> $= \frac{e}{e-1} ([x(-e^{-x})]_0^1 - \int_0^1 (-e^{-x}) dx)$ $= \frac{e}{e-1} ([-xe^{-x}]_0^1 - [e^{-x}]_0^1)$ $(= \frac{e}{e-1} (-e^{-1} - 0 - (e^{-1} - 1)))$ $= \frac{e}{e-1} (1 - \frac{2}{e}) \text{ or } \frac{e-2}{e-1} \text{ oe}$	<p>M1</p> <p>M1*</p> <p>M1dep*</p> <p>A1</p> <p>[4]</p>	<p>Attempt $\int xf(x)dx$, ignore limits</p> <p>Attempt integration by parts the correct way round, ignore limits</p> <p>Attempt second integral of the form $\pm \int e^{-x} dx$, ignore limits</p> <p>Accept k instead of $\frac{e}{e-1}$ throughout except ans</p>
<p>5 (i) Assume pop sd same (105)</p> <p>H_0: Pop mean = 1150 H_1: Pop mean < 1150</p> $\frac{\frac{21800}{20} - 1150}{\frac{105}{\sqrt{20}}}$ <p>= ± 2.556 or 2.56</p> <p>Compare with $z = \pm 2.326$ (for a clear 2 tail test compare with ± 2.576)</p> <p>Evidence that mean distance decreased</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1ft</p> <p>[6]</p>	<p>Allow “μ” but not just “mean”</p> <p>Allow $\div \frac{105}{20}$. (Accept “totals” method)</p> <p>Or 0.0053 if prob/area comparison used</p> <p>Correct comparison of z or prob/area consistent with their test</p> <p>In context. Allow mean dist decreased ft their z and/or clear 2 tail test</p>
<p>(ii) 0.01</p> <p>Concluding there has been a decrease when there has not.</p>	<p>B1</p> <p>B1</p> <p>[2]</p>	<p>In context</p>

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6 (i)	$E(\text{Tot}) = 2 \times 36 + 55$	$(= 127)$	B1	(Or ± 13) For standardising with their mean and var. Allow without $\sqrt{\quad}$ or with false cc, but their mean and variance must involve parameters from both given distributions
	$\text{Var}(\text{Tot}) = 2 \times 3.5^2 + 5.2^2$	$(= 51.54)$	B1	
	$\frac{140 - 127}{\sqrt{51.54}}$	$(= 1.811)$	M1	
	$\Phi(1.811)$ $= 0.965$ (3 sfs)		A1 [4]	
(ii)	$E(RM) = 36 + 1.5 \times 55$	$(= 118.5)$	B1	(Or ± 18.5) For standardising with their mean and var. Allow without $\sqrt{\quad}$ or with false cc, but their mean and variance must involve parameters from both given distributions
	$\text{Var}(RM) = 3.5^2 + 1.5^2 \times 5.2^2$	$(= 73.09)$	B1	
	$\frac{100 - 118.5}{\sqrt{73.09}}$	$(= -2.164)$	M1	
	$1 - \Phi(-2.164) = \Phi(2.164)$ 0.985 (3 sfs)		A1 [4]	
7 (i) (a)	$\frac{1 - e^{-1.2}(1 + 1.2)}{1 - e^{-1.4}}$	$(= 0.3374)$ $(= 0.7534)$	M1 A1	M1 for Poisson either P(0 or 1) or P(0) with $\lambda = 1.2$ or 2.4 or 1.4 or 2.8, accept one end error Both expressions fully correct Their Poisson P(0 or 1) \times P(0)
	$(1 - e^{-1.2}(1 + 1.2)) \times (1 - e^{-1.4})$		M1	
	$= 0.254$ (3 sfs)		A1 [4]	
(i) (b)	$\lambda = 2.6$ seen		B1	Poisson $1 - P(0, 1, 2)$, allow $1 - P(0, 1, 2, 3)$, with attempt at combined λ for M and W. Accept combination method: at least 4 correct terms and "1 -" M1; all terms correct B1
	$1 - e^{-2.6}(1 + 2.6 + 2.6^2 \div 2)$		M1	
	$= 0.482$ (3 sfs)		A1 [3]	

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<p>(ii) $N(52, 52)$</p> $\frac{60.5 - 52}{\sqrt{52}} \quad (= 1.179)$ $1 - \Phi("1.179")$ $ (= 1 - 0.8808)$ $ = 0.119 \text{ (3 sfs)}$	B1	Seen or implied
	M1	Standardising with $N(\lambda, \lambda)$ with $\lambda = 10 \times 5.2$ or 10×2.6 Allow with wrong or no cc or no $\sqrt{\quad}$
	M1	Their correct area
	A1 [4]	