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<p><b>1 (i)</b> Mean = 2.6</p> <p>Var = <math>4 \times 1.3</math></p> <p>= 5.2</p>	<p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>M1 for either <math>4 \times</math>, or for <math>\text{Var}(X) = 1.3</math> implied</p>
<p><b>(ii)</b> Var <math>\neq</math> mean or <math>2X</math> does not take all integer values</p>	<p>B1 [1]</p>	<p><math>X</math> and <math>X</math> are not independent oe</p>
<p><b>2</b> <math>H_0: P(\text{correct}) = \frac{1}{5}</math> <math>H_1: P(\text{correct}) &gt; \frac{1}{5}</math> <math>B(100, \frac{1}{5}) \approx N(20, 16)</math></p> <p><math>\frac{26.5 - 20}{4} = 1.625</math></p> <p>comp <math>z = 1.645</math></p> <p>Claim not justified</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1ft [5]</p>	<p>Accept p Accept <math>H_0: \mu = 20</math> <math>H_1: \mu &gt; 20</math></p> <p>Allow wrong or no cc or denom = 16 For <math>\pm 1.625</math></p> <p>Valid comparison of <math>z</math> or areas (<math>0.0521 &gt; 0.05</math>)</p> <p>In context. No contradictions. Ft their <math>z</math>.</p>
<p><b>3</b> <math>\text{Var}(\text{Tot}) = 0.02^2 + 0.03^2 + 0.01^2 = 0.0014</math></p> <p>Mean(Tot) = 0.37 Tot <math>\sim N(0.37, 0.0014)</math></p> <p><math>\frac{0.30 - 0.37}{\sqrt{0.0014}} (= -1.871)</math></p> <p><math>\Phi(-1.871) = 1 - \Phi(1.871)</math></p> <p>= 0.0306 or 0.0307</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1 [5]</p>	<p>Allow without <math>\sqrt{\quad}</math>. No cc</p> <p>Correct area</p>
<p><b>4 (i)</b> <math>\text{Est}(\mu) = 331(.125)</math></p> <p><math>\text{Est}(\sigma^2) = \frac{8}{7} \left( \frac{877179}{8} - 331.125^2 \right)</math></p> <p>= 4.125 or 4.13</p>	<p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>Allow their <math>\Sigma x^2</math></p>
<p><b>(ii)</b> <math>z = 2.326</math></p> <p><math>331 \pm z \times \sqrt{\frac{4.2}{50}}</math></p> <p>= 330 to 332 (3 sfs)</p>	<p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>Allow incorrect <math>z</math> (<math>\neq 1, 0</math>), not a prob</p> <p>Ignore brackets, if given. CWO</p>
<p><b>(iii)</b> No, because 333 is not within CI</p>	<p>B1ft [1]</p>	

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<p><b>5 (i)</b> <math>\pm 1.645</math> used</p> $\frac{\bar{x} - 22}{\frac{3.5}{\sqrt{12}}} > 1.645$ <p><math>\bar{x} &gt; 23.66(20)</math>  <math>\bar{x} &gt; 23.7</math> <b>AG</b></p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>Accept '='          (standardising using 23.7 scores M1A0)          or <math>\bar{x} = 23.66(20)</math></p>
<p><b>(ii)</b> <math>P(\bar{x} &lt; 23.7 \mid \mu = 25.8)</math></p> $\frac{23.662 - 25.8}{\frac{3.5}{\sqrt{12}}} = -2.116$ <p><math>\Phi(' -2.116') = 1 - \Phi('2.116')</math>          (= <math>1 - 0.9828</math>)</p> <p>= 0.0172 (3 sfs)</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>For attempt type II error and standardising</p> $\frac{23.7 - 25.8}{\frac{3.5}{\sqrt{12}}} = -2.078$ <p><math>\Phi(' -2.078') = 1 - \Phi(' -2.078')</math>          (= <math>1 - 0.9812</math>)</p> <p>= 0.0188</p>
<p><b>6 (i)</b> Customers arrive independently or randomly</p>	<p>B1</p> <p>[1]</p>	<p>In context. Allow "singly"</p>
<p><b>(ii)</b> <math>e^{-6} \times \frac{6^5}{5!}</math></p> <p>= 0.161 (3 sfs)</p>	<p>M1</p> <p>A1</p> <p>[2]</p>	<p>Poisson P(5), allow any mean</p>
<p><b>(iii)</b> <math>\lambda = 2.4</math></p> $e^{-2} \left( 1 + 2.4 + \frac{2.4^2}{2!} \right)$ <p>= 0.570 (3 sfs)</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>Poisson P(0, 1, 2), allow their mean          allow one end error</p>
<p><b>(iv)</b> N(24, 24)</p> $\frac{295 - 24}{\sqrt{24}} (= 1.123)$ <p><math>\Phi('1.123')</math></p> <p>= 0.869 (3 sfs)</p>	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>Stated or implied</p> <p>Allow with wrong or no cc and/or no <math>\sqrt{\quad}</math>          Correct area</p>

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7 (i) (a) $X$ or 5	B1 [1]	
(b) $V$ or 3  Higher and lower values more likely or there are more higher and lower values or more prob at both extremes	B1  B1dep [2]	Should mention values or prob Not just graph or spread eg not “More spread”
(ii) $\frac{2+1}{2} \times 0.5$ or $\int_0^{0.5} (2-2x)dx$  $= 0.75$	M1  A1 [2]	(‘or’ method requires linear function and correct limits)  CWO
(iii) (a) $\int_0^1 ax^n dx = 1$  $\left[ \frac{ax^{n+1}}{n+1} \right]_0^1 = 1$  $\frac{a}{n+1} = 1$  ( $a = n + 1$ AG)	M1  A1  A1  [3]	Attempt integ of correct form = 1 (ignore limits)  Correct integrand & limits  No errors seen
(b) $\int_0^1 ax^{n+1} dx = \frac{5}{6}$ oe  $\left[ \frac{ax^{n+2}}{n+2} \right]_0^1 = \frac{5}{6}$ oe  $\frac{a}{n+2} = \frac{5}{6}$ ( $6a = 5n + 10$ )  $a = 5, n = 4$	M1*  A1  M1dep  A1 [4]	Integral of form $\int xf(x)dx = \frac{5}{6}$ , ignore limits  Correct integrand & limits  Attempt to use $a = n + 1$ within 2 <sup>nd</sup> equ to get an equ in $n$ (or $a$ )