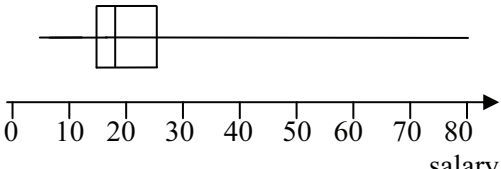


Page 4	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2011	9709	63

<b>1 (i)</b> $z = 0.38$ $\pm \frac{25 - \mu}{\mu/3} = 0.38$ $\mu = 22.2, \sigma = 7.40$	B1	$\pm 0.38(0)$ seen or implied
	M1	Standardising attempt resulting in $z =$ some $\mu/\sigma$ both, no continuity correction
	M1	Substituting to eliminate $\mu$ or $\sigma$ and attempt to solve linear equation
	A1 [4]	Both correct
<b>(ii)</b> $P(4) = {}^6C_4(0.352)^4(0.648)^2$ $= 0.0967$	M1	${}^6C_r \times (p)^r \times (1-p)^{6-r}$ , $r = 2$ or $4$
	A1 [2]	Correct answer
<b>2 (i)</b> $P(F) = \frac{12}{30}$ (0.4) or $P(W) = \frac{16}{30}$ (0.533) or $P(M \cap W') = \frac{5}{30}$ (0.167) $(F \text{ or } W) = \frac{13}{30} + \frac{3}{30} + \frac{9}{30}$ or $1 - \frac{5}{30}$ or $\frac{12}{30} + \frac{16}{30} - \frac{3}{30}$ $= \frac{5}{6}$ (0.833)	B1	$\frac{12}{30}$ or $\frac{16}{30}$ or $\frac{5}{30}$ seen
	M1	Valid attempt to find $P(F \text{ or } W)$
	A1	Correct unsimplified expression
	A1 [4]	Correct answer
<b>(ii)</b> $P(M) = 18/30$ (0.6), $P(W) = 16/30$ (0.533), $P(M) \times P(W) = 8/25$ (0.32) $P(M \text{ and } W) = 13/30$ (0.433) $\neq 8/25$ (0.32) not independent OR $P(M W) = \frac{P(M \text{ and } W)}{P(W)} = \frac{13/30}{16/30} = \frac{13}{16}$ (0.813) $\neq \frac{18}{30} = P(M)$ , not independent OR $P(W M) = \frac{P(M \text{ and } W)}{P(M)} = \frac{13/30}{18/30} = \frac{13}{18}$ $\neq \frac{16}{30} = P(W)$ , not independent	M1	Valid attempt to find $P(M)$ , $P(W)$ and $P(M) \times P(W)$
	A1	$P(M \text{ and } W) = 13/30 \neq 8/25$ and correct conclusion
	M1	Valid attempt to find $P(M \text{ and } W)$ , $P(W)$ and $P(M \text{ and } W) \div P(W)$
	A1	$\frac{13}{16} \neq \frac{18}{30} = P(M)$
	M1	Valid attempt to find $P(M \text{ and } W)$ , $P(M)$ and $P(M \text{ and } W) \div P(M)$
	A1	$\frac{13}{16} \neq \frac{16}{30} = P(W)$
	[2]	

Page 5	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2011	9709	63

<p><b>3 (i)</b> <math>P(3m) = 4/5</math> (0.8) <math>P(5m) = 1/5</math> (0.2)</p> <p><math>E(X) = 17/5</math> (3.4)</p> <p><math>\text{Var}(X) = 16/25</math> (0.64)</p>	<p>B1</p> <p>B1 M1</p> <p>A1 [4]</p>	<p><math>P(3m) = 4/5</math> or <math>P(5m) = 1/5</math> seen or implied</p> <p>Correct <math>E(X)</math></p> <p>Subtract their mean<sup>2</sup> numerically from <math>\sum x^2 p</math>, no extra dividing</p> <p>Correct answer</p>
<p><b>(ii)</b> <math>P(3, 5) + P(5, 3) = 0.8 \times 0.2 + 0.2 \times 0.8</math></p> <p><math>= 8/25</math> (0.32)</p>	<p>M1</p> <p>A1√ [2]</p>	<p>Summing two 2-factor terms</p> <p>Correct answer, ft on <math>2 \times p \times (1 - p)</math>, their <math>p</math></p>
<p><b>(iii)</b> <math>P(11) = P(3, 3, 5) + P(3, 5, 3) + P(5, 3, 3)</math></p> <p><math>= (4/5 \times 4/5 \times 1/5) \times 3</math></p> <p><math>= 48/125</math> (0.384)</p>	<p>M1</p> <p>M1</p> <p>A1 [3]</p>	<p>Mult 2 probs for 3 with 1 prob for 5</p> <p>Multiplying probs for 11 by 3 or summing 3 options</p> <p>Correct final answer</p>
<p><b>4 (i)</b> <math>3! \times 4! \times 8! \times 3!</math></p> <p><math>= 34\,836\,480</math> (34 800 000)</p>	<p>M1</p> <p>M1</p> <p>A1 [3]</p>	<p>Multiplying 3 factorials together</p> <p>Multiplying by 3!</p> <p>Correct answer</p>
<p><b>(ii)</b> <math>{}^3C_2 \times {}^4C_2 \times {}^8C_2</math></p> <p><math>= 504</math></p>	<p>M1</p> <p>A1 [2]</p>	<p>Multiplying (only) 3 combinations together</p> <p>Correct answer</p>
<p><b>(iii)</b> Fr Fa H</p> <p><math>{}^3C_1 \times {}^2C_1 \times {}^8C_2 = 1008</math></p> <p><math>{}^3C_2 \times {}^1C_1 \times {}^8C_1 = 672</math></p> <p><math>{}^4C_1 \times {}^3C_1 \times {}^4C_1 = 840</math></p> <p>total ways = 2520</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1 [4]</p>	<p>Multiplying 3 combinations, only</p> <p>Summing 3 options</p> <p>3 correct combination answers</p> <p>Correct answer</p>
<p><b>5 (i)</b> LQ = 15, Median = 18, UQ = 26</p> 	<p>B1</p> <p>B1</p> <p>B1√</p> <p>B1√</p> <p>[4]</p>	<p>LQ = 15, Median = 18, and UQ = 26</p> <p>Linear scale and labels</p> <p>Quartiles and median box, ft on their values, but <math>M - LQ &lt; UQ - M</math></p> <p>Whiskers from 5 to LQ and UQ to 80, ft on their values</p>
<p><b>(ii)</b> most (3/4) are earning less than 26K, not many earning high salaries, etc</p>	<p>B1 [1]</p>	<p>Any sensible answer</p>
<p><b>(iii) (a)</b> IQ range = 11</p> <p>high outlier is above <math>26 + 1.5 \times 11</math></p> <p><math>= 42500</math> euros</p>	<p>B1</p> <p>M1</p> <p>A1 [3]</p>	<p>IQR = 11</p> <p>Their UQ + <math>1.5 \times</math> their IQ range</p> <p>Correct answer</p>
<p><b>(b)</b> Low outlier is below <math>15 - 1.5 \times 11 = -1.5</math></p>	<p>B1√ [1]</p>	<p>Correct reason, must involve subtraction, ft on their LQ and <math>1.5 \times</math> their IQR</p>

Page 6	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2011	9709	63

<p><b>6 (i)</b> <math>P(O \text{ given } +) = \frac{0.37}{0.83}(0.4458)</math></p> $P(0, 1, 2) = (0.4458)^0(0.5542)^9 + {}^9C_1(0.4458)^1(0.5542)^8 + {}^9C_2(0.4458)^2(0.5542)^7$ $= 0.156$	<p>B1 A1  M1 M1  A1 A1 [6]</p>	<p>0.83 seen or implied Attempt to find <math>P(O \text{ given } +)</math> using conditional probability fraction Binomial term <math>{}^9C_r p^r (1-p)^{9-r}</math>, <math>r \neq 0</math> or <math>9</math> Binomial expression <math>P(0, 1, 2)</math> or <math>P(0, 1, 2, 3)</math> powers summing to 9 any <math>0 &lt; p &lt; 1</math> Correct unsimplified expression Correct final answer</p>
<p><b>(ii)</b> <math>\mu = 150 \times 0.35 = 52.5,</math></p> $\sigma^2 = 150 \times 0.35 \times 0.65 = 34.125$ $P(> 60.5) = P\left(z > \pm \frac{60.5 - 52.5}{\sqrt{34.125}}\right)$ $= 1 - \Phi(1.369)$ $= 0.0854 \text{ or } 0.0855$	<p>B1  M1 M1  M1  A1 [5]</p>	<p><math>150 \times 0.35</math> (52.5) and <math>150 \times 0.35 \times 0.65</math> (34.125) seen Standardising, using sd not variance Using continuity correction, 59.5 or 60.5 correct area (<math>&lt; 0.5</math>, for mean <math>&lt;</math> their 60)  correct value</p>