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1 $\mu = 250 \times 0.86 = 215$ $\sigma^2 = 250 \times 0.86 \times 0.14 = 30.1$ $P(X > 210) = 1 - \Phi\left(\frac{210.5 - 215}{\sqrt{30.1}}\right)$ $= \Phi(0.820)$ $= 0.794$	B1	250 × 0.86 and 250 × 0.86 × 0.14 seen o.e	
	M1	Standardising, with or without cc, must have sq rt in denom	
	M1	Continuity correction 210.5 or 209.5 only	
	M1	Correct region (> 0.5) ft their mean	
	A1 [5]	Correct answer	
2 (i) $133/n + 25 = 28.325$ $n = 40$ $3762/40 - 3.325^2 = 82.99$ standard deviation = 9.11	M1	Equation involving 133, 25 and 28.325	
	A1	Correct answer for n	
	M1	Using coded mean in variance formula	
	A1 [4]	Correct answer	
(ii) $82.99 = \sum x^2/40 - 28.325^2$ $\sum x^2 = (82.99 + 28.325^2) \times 40$ $= 35412$ (35400) OR $\sum (x - 25)^2 = \sum x^2 - 50\sum x + 40 \times 25^2$ $\sum x^2 = 3762 + 50 \times 1133 + 25000$ $= 35412$	M1	Using uncoded material in variance formula	
	A1	Correct answer	
	M1	Expanding and substituting for $\sum x$	
	A1 [2]	Correct answer	
3 (i) $P(X = 1) = P(\text{GBBB}) 4 \times C_1$ $= 5/8 \times 3/7 \times 2/6 \times 1/5 \times 4 = 1/14$ $P(X = 2) = P(\text{GGBB}) \times {}_4C_2 = 3/7$ $P(X = 3) = P(\text{GGGB}) \times {}_4C_3 = 3/7$ $P(X = 4) = P(\text{GGGG}) \times {}_4C_4 = 1/14$ OR $P(1) = {}_5C_1 / {}_8C_4 = 1/14$ $P(2) = {}_3C_2 \times {}_5C_2 / {}_8C_4 = 3/7$ $P(3) = {}_3C_1 \times {}_5C_3 / {}_8C_4 = 3/7$ $P(4) = {}_5C_4 / {}_8C_4 = 1/14$	M1	Considering values of X of 1, 2, 3, 4	
	M1	Attempting to find the probability of at least 2 values of X	
	A1	One correct probability	
	A1	All correct	
	M1	Considering values of X of 1, 2, 3, 4	
	M1	Dividing by ${}_8C_4$	
	A1	One correct probability	
	A1 [4]	All correct	
	(ii) $\text{Var}(X) = 1/14 + 12/7 + 27/7 + 16/14 - (5/2)^2$ $= 15/28$ (0.536)	M1	Using a variance formula correctly with mean ² subtracted numerically, no extra division
		A1 [2]	Correct final answer

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<p>4 (i) History: lowest 27, highest 57, LQ = 33 med = 39 UQ = 50</p> <p>Physics</p> <p>History</p> <p>10 20 30 40 50 60 70 marks</p>	M1	<p>Attempt to find history quartiles and median by putting in order or stem and leaf (can be implied if the answer is reasonable)</p> <p>Correct history median and quartiles</p> <p>Uniform scale and labels</p> <p>Correct history graph fit their quartiles line not through box</p> <p>Correct physics graph</p>	[1]
(ii) Physics marks are more spread out than History marks	B1	Any sensible comment	[1]
<p>5 (i) $z = 1.882$ or 1.881</p> <p>$1.882 = (32 - 20) / \sigma$</p> <p>$\sigma = 6.38$</p>	B1	± 1.882 or ± 1.881 seen	
	M1	Equation using their z (must be a z -value) 32, 20 and s	
	A1	Correct answer	[3]
<p>(ii) $P(x > 13) = P\left(z > \frac{13 - 20}{6.376}\right)$</p> <p>$= P(z > -1.0978)$</p> <p>$= 0.864$</p>	M1	Standardising	
	M1	Correct area > 0.5	
	A1	Correct answer	[3]
<p>(iii) $P(\text{at least } 2) = 1 - P(0, 1)$</p> <p>$= 1 - (0.97)^7 - (0.03)(0.97)^6 {}_7C_1$</p> <p>$= 0.0171$</p>	M1	Using 0.03 and 0.97 or 0.06 and 0.94 in a binomial expression powers summing to 7	
	M1	Correct unsimplified binomial expansion	
	A1	Correct answer	[3]
<p>6 (a) (i) $\frac{12!}{2!3!2!} = 19958400$ (20,000,000)</p>	M1	Dividing by 2! 3! 2!	
	A1	Correct answer	[2]
<p>(ii) $\frac{4!}{2!} \times \frac{9!}{2!3!} = 362880$</p>	B1	4! seen multiplied	
	B1	9! or $9 \times 8!$ seen multiplied	
	B1	Correct final answer	[3]
<p>(b) (i) $3876 \times 4!$</p> <p>$= 93024$</p>	M1	Multiplying by 4!	
	A1	Correct answer	[2]
<p>(ii) $(3!)^4 \times 4!$</p> <p>$= 31104$</p>	M1	3! or 6 or 4! seen	
	A1	Correct final answer	[2]

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7 (i)	$P(2, N2, 2) = 1/4 \times 1 \times 1/7 = 1/28$	M1	Considering at least two options of 2s and 8s
	$P(8, 8, N8) = 1/4 \times 2/5 \times 3/7 = 3/70$	M1	Considering three options for the 8s
	$P(8, N8, 8) = 1/4 \times 3/5 \times 4/7 = 3/35$	M1	Summing their options if more than 3 in total
	$P(N8, 8, 8) = 3/4 \times 2/5 \times 4/7 = 6/35$	B1	One option correct
	$\Sigma = 47/140 (0.336)$	A1 [5]	Correct answer
(ii)	$P(2, 2 \text{ given same}) = \frac{1/28}{47/140}$	M1	1/28 in numerator of a fraction
	$= 5/47 (0.106)$	A1 [2]	Correct answer
(iii)	$P(X) = 47/140$	M1	Attempt to compare $P(A \text{ and } B)$ with $P(A) \times P(B)$ or using conditional probabilities
	$P(Y) = 1/4$		
	$P(X \text{ and } Y) = 1/28 \neq 47/140 \times 1/4$ Not independent	A1 [2]	Legitimate correct answer