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1	$17\sin 50 - 2g$	B1	Vertical component of velocity
	$v^2 = (17\sin 50 - 2g)^2 + (17\cos 50)^2$	M1	Pythagoras with 2 perpendicular components
	$v = 13(.0) \text{ ms}^{-1}$	A1 [3]	
2	(i) 0.212	B1 [1]	From $(0.6/2)\cos 45$
	(ii) (a) $0.3\cos 45 \times (2 \times 7) = (2 \times 0.6\sin 45) \times F$	M1	Moments about <i>A</i>
	$F = 3.5$	A1 [2]	
3	(ii) (b) $0.3\cos 45 \times (2 \times 7) = 0.6F$	M1	Or Ans (i) / $\cos 45$
	$F = 4.95$	A1 [2]	
	(i) $x = (25\cos 45)t$	B1	
	$y = (25\sin 45)t - gt^2/2$	B1	
	$y = x(25\sin 45)/(25\cos 45) - g[x/(25\cos 45)]^2/2$	M1	Eliminates <i>t</i> between 2 simultaneous equations
	$y = x - 0.016x^2$	A1 [4]	
4	(ii) $2.4 = x - 0.016x^2$	M1	Creates and attempts to solve a quadratic equation ($x = 2.5, 60$)
	Distance = 57.5 m	A1 [2]	
	(i) $0.4\delta v/\delta t = 0.2v^2$	M1	Newton's Second Law with $a = \delta v/\delta t$
	$\int v^{-2}\delta v = -0.5 \int \delta t$	A1	
	$-v^{-1} = -0.5t (+ c)$		
	$t = 0, v = 8, \text{ hence } c = -0.125$	M1	
	$v = 1/(0.125 + 0.5t) = 8/(1 + 4t) \text{ AG}$	A1 [4]	
4	(ii) $\delta x/\delta t = 8/(1 + 4t)$	M1*	
	$x = 8 \int \delta t / (1 + 4t)$		
	$x = \frac{8}{4} \ln(1 + 4t) (+ c)$	A1	Accept $c = 0$ assumed
	$t = 1.5, x = \frac{8}{4} * \ln(1 + 4 \times 1.5)$	D* M1	Or limits used $\frac{8}{4} [\ln(1 + 4t)]_0^{1.5}$
	$OP = 3.89 \text{ m}$	A1	4

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5	(i) $0.2\omega^2 \times 1.2 = 6$ $\omega = 5$	M1 A1 [2]	Uses radial acceleration on R , 1 force
	(ii) $m\omega^2 \times 2 \times 0.4 = 10 - 6$ $m = 0.2 \text{ kg}$	M1 A1 A1 [3]	Uses radial acceleration on Q , 2 forces
	(iii) $0.2 \times (5 \times 1.2)^2/2 = M(5 \times 0.4)^2/2$ $M = 1.8 \text{ kg}$ $1.8 \times 5^2 \times 0.4 = T - 10$ $T = 28 \text{ N}$	M1 A1 DM1 A1 [4]	
6	(i) $\pi 0.6^2 \times 0.6 \times 0.3 - 2\pi 0.6^3/3 \times 3 \times 0.6/8$ $= (\pi 0.6^3 + 2\pi 0.6^3/3)d$ $d = 0.09 \text{ m}$	M1 A1 A1 A1 [4]	Table of moments idea Correct elements Correct composite
	(ii) $\frac{2}{3}\pi 0.6^3 \times \frac{3}{8} \times 0.6 - \pi \times 0.6^3 \times 0.3$ $+ 0.48A \times 0.36 = 0$ $A = 3\pi/16 \text{ m}^2$ OR $[\frac{2}{3}\pi \times 0.6^3 + \pi \times 0.6^3] \times 0.09 = 0.48A \times 0.36$ $A = 3\pi/16$	M1 A1 A1 A1 [4] M1 A1 A1	Table of moments idea (about O) Correct elements Table of moments idea (about O) Correct elements
	(iii) Increase in length $[= 2 \times (0.6 - 0.48)] = 0.24\text{m}$	B1 [1]	Remove cylinder with centre of mass at O

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7 (i)	$0.8g\sin 30 = 20e/0.4$ $e = 0.08 \text{ m}$	M1 A1 [2]	
(ii)	$0.8v^2/2 + 20 \times 0.08^2/(2 \times 0.4)$ $= 0.8g(0.4 + 0.08)\sin 30$ $v = 2.1(0) \text{ ms}^{-1}$	M1 A1 A1 A1 [4]	Conservation of KE, PE, EE Correct start terms, signs accurate Correct final term, sign accurate
(iii)	$0.8gd\sin 30 = 20(d - 0.4)^2/(2 \times 0.4)$ $25d^2 - 24d + 4 = 0$ $d = 0.745 \text{ m}$	M1* A1 D* M1 A1 [4]	$4d = 25(d - 0.4)^2$ Obtains and solves a 3 term quadratic equation.