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	GCE AS/A LEVEL – October/November 2011	9709	23

- 1 Obtain derivative of the form $\frac{k}{5x+1}$, where $k = 1, 5$ or $\frac{1}{5}$ M1
- Obtain correct derivative $\frac{5}{5x+1}$ A1
- Substitute $x = 4$ into expression for derivative and obtain $\frac{5}{21}$ A1✓ [3]
- 2 **EITHER** State or imply non-modular inequality $(2x - 3)^2 \leq (3x)^2$, or corresponding equation or pair of linear equations M1
- Make reasonable solution attempt at a 3-term quadratic, or solve two linear equations M1
- Obtain critical values -3 and $\frac{3}{5}$ A1
- State correct answer $x \leq -3$ or $x \geq \frac{3}{5}$ A1
- OR** State one critical value, e.g. $x = -3$, by solving a linear equation (or inequality) or from a graphical method or by inspection B1
- State the other critical value correctly B2
- State correct answer $x \leq -3$ or $x \geq \frac{3}{5}$ B1 [4]
- 3 Use $2 \ln(x + 3) = \ln(x + 3)^2$ M1
- Use law for addition or subtraction of logarithms M1
- Obtain correct quadratic expression in x A1
- Make reasonable solution attempt at a 3-term quadratic M1
- State $x = 9$ and no other solutions (condone $x = -1$ not deleted) A1 [5]
- 4 (i) State correct expression $\frac{1}{2} + \frac{1}{2} \cos 2x$, or equivalent B1 [1]
- (ii) Integrate an expression of the form $a + b \cos 2x$, where $ab \neq 0$, correctly M1
- State correct integral $\frac{1}{2}x + \frac{1}{4} \sin 2x$, or equivalent A1
- Obtain correct integral (for $\sin 2x$ term) of $-\frac{1}{2} \cos 2x$ B1
- Attempt to substitute limits, using exact values M1
- Obtain given answer correctly A1 [5]
- 5 Use trig identity correctly to obtain a quadratic in $\tan 2\theta$ M1
- Solve the quadratic correctly M1
- Obtain $\tan 2\theta = 1$ or $-\frac{4}{5}$ A1
- Obtain one correct answer A1
- Carry out correct method for second answer from either root M1
- Obtain remaining 3 answers from $22.5^\circ, 112.5^\circ, 70.7^\circ, 160.7^\circ$ and no others in the range A1
- [Ignore answers outside the given range] [6]

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- 6 (i) Substitute $x = 1$ or $x = -2$ and equate to zero M1
 Obtain a correct equation in any form with powers of x values calculated A1
 Obtain a second correct equation in any form A1
 Solve a relevant pair of equations for a or for b M1
 Obtain $a = 3$ and $b = -5$ A1 [5]
- (ii) Attempt division by $x^2 + x - 2$, or equivalent, and reach a partial quotient of $x^2 + kx$ M1
 Obtain partial quotient $x^2 + 2x$ A1
 Obtain $x^2 + 2x - 1$ with no errors seen A1
 S.C. M1A1✓ if 'a' and/or 'b' incorrect [3]
- 7 (i) At any stage, state the correct derivative of $e^{\frac{1}{2}x}$ B1
 Use product rule M1
 Obtain correct derivative in any form A1
 Equate derivative to 3 and obtain given equation correctly A1 [4]
- (ii) Consider sign of $2 + 6e^{-\frac{1}{2}x} - x$, or equivalent M1
 Complete the argument correctly with appropriate calculations A1 [2]
- (iii) Use the iterative formula correctly at least once M1
 Obtain final answer 3.21 A1
 Show sufficient iterations to justify its accuracy to 2 d.p. or show there is a sign change in the interval (3.205, 3.215) B1 [3]
- 8 (i) State $2y \frac{dy}{dx}$ as derivative of y^2 , or equivalent B1
 Equate derivative of LHS to zero and solve for $\frac{dy}{dx}$ M1
 Obtain given answer correctly A1 [3]
- (ii) Equate gradient expression to -1 and rearrange M1
 Obtain $y = 2x$ A1
 Substitute into original equation to obtain an equation in x^2 (or y^2) M1
 Obtain $2x^2 - 3x - 2 = 0$ (or $y^2 - 3y - 4 = 0$) A1
 Correct method to solve their quadratic equation M1
 State answers $(-\frac{1}{2}, -1)$ and $(2, 4)$ A1 [6]