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1	<p>(i) $(2 - y)^5 = 32 - 80y + 80y^2$</p> <p>(ii) $(2 - (2x - x^2))^5$ “y” = “$2x - x^2$” $\rightarrow 80 + 320 = 400$</p>	<p>B2,1 [2]</p> <p>M1 M1 A1 [3]</p>	<p>-1 for each error. Accept 2^5.</p> <p>Allow for $y = 2x + x^2$ Needs to consider exactly 2 terms. CO – accept $400x^2$, accept full expansion if $400x^2$ is part of it.</p>
2	<p>$f: x \mapsto 3x + a, g: x \mapsto b - 2x$</p> <p>(i) $f^2(x) = 3(3x + a) + a$ $f^2(2) = 18 + 4a = 10 \rightarrow a = -2$</p> <p>$g^{-1}(x) = \frac{b-x}{2} \rightarrow \frac{b-2}{2} = 3 \quad b = 8$ or $g(3) = 2 \rightarrow b - 6 = 2 \quad b = 8$</p> <p>(ii) $fg(x) = 3(b - 2x) + a$ $= 22 - 6x$</p>	<p>B1 B1</p> <p>M1 A1 [4]</p> <p>M1 A1√ [2]</p>	<p>Must be correct – unsimplified ok co</p> <p>Correct method leading to a value for b co</p> <p>Must be fg not gf. √ on a and b ($3b + a - 6x$) must be two term answer.</p>
3	<p>$\vec{OA} = 5\mathbf{i} + \mathbf{j} + 2\mathbf{k}, \vec{OB} = 2\mathbf{i} + 7\mathbf{j} + p\mathbf{k}$</p> <p>(i) $\vec{OA} \cdot \vec{OB} = 10 + 7 + 2p$ $= 0 \rightarrow p = -8\frac{1}{2}$</p> <p>(ii) $\mathbf{AB} = -3\mathbf{i} + 6\mathbf{j} + 2\mathbf{k}$ Modulus = $\sqrt{9+36+4}$ Magnitude 28 $\rightarrow 28 \times$unit vector $\rightarrow -12\mathbf{i} + 24\mathbf{j} + 8\mathbf{k}$.</p>	<p>M1</p> <p>DM1 A1 [3]</p> <p>B1 M1 M1 A1 [4]</p>	<p>Use of $x_1x_2 + y_1y_2 + z_1z_2$</p> <p>....=0 co</p> <p>co (accept negative) For modulus Scales by $\times 28 \div$ modulus. Co – could leave as “$4 \times \dots$”.</p>
4	<p>(i) $y^2 + 2x = 13, 2y + x = 8$ $\rightarrow y^2 - 4y + 3 = 0, x^2 - 8x + 12 = 0$ $\rightarrow (2, 3)$ and $(6, 1)$</p> <p>(ii) Removes $x \rightarrow y^2 + 2(k - 2y) = 13$ Uses $b^2 - 4ac$ on “quadratic = 0” $\rightarrow k = 8\frac{1}{2}$ or $\frac{dy}{dx} = -\frac{1}{2} = \frac{-1}{y} \rightarrow y=2, x=4\frac{1}{2}, k=8\frac{1}{2}$</p>	<p>M1 A1 DM1 A1 [4]</p> <p>M1 DM1 A1 [3]</p>	<p>Complete elimination of x or y co (allow multiples) – needs 3 terms Solution of quadratic = 0 Needs all 4 coordinates.</p> <p>Complete elimination of x or y. Use of discriminant = 0, <0 or >0 Co (M1 equating m of line and curve M1 x to y A1 for k)</p>

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<p>5 (i)</p> <p>(ii) Evidence of $\sin 30 = \cos 60 = 0.5$ Other root is 150°</p> <p>(iii) $0 \leq x < 30$ and $150 < x \leq 180$ ($x < 30$ or $x > 150$ ok)</p>	<p>B1 B1 B1 [3]</p> <p>B1 B1 [2]</p> <p>B1 B1 ✓ [2]</p>	<p>$y = \sin x$ $(0,0)$, $(\pi,0)$ + curve $y = \cos 2x$ One full cycle. $y = \cos 2x$ starts and finishes at $(0, 1)$ and oscillates between -1 and $+1$. Do not penalise graphs from 0 to 360.</p> <p>co co</p> <p>Condone $<$ or \leq throughout</p>
<p>6 (i) D to $AX = 6 \sin \frac{\pi}{3} = 6\sqrt{3} \div 2$ E to $AX = 10 \sin \theta$ Equate these $\rightarrow \theta = \sin^{-1} \frac{3\sqrt{3}}{10}$.</p> <p>(ii) Arc $DX = 6 \cdot \frac{1}{3}\pi = 2\pi$ Arc $EX = 10 \times 0.5464 = 5.464$ Horizontal steps = $6 \cos \frac{1}{3}\pi$ and $10 \cos \theta$ $DE = 10 + 6 - 6 \cos \frac{1}{3}\pi - 10 \cos \theta$ Perimeter = arc DX + arc BX + DE $\rightarrow 16.20$</p>	<p>B1 B1 B1 [3]</p> <p>B1 M1 M1 M1 A1 [5]</p>	<p>co Needs $-\sqrt{3} \div 2$ not just $3\sqrt{3}$. co Correct method. ag. Use of decimals loses this B mark.</p> <p>co Use of $s=r\theta$ radians. Attempt at both steps needed Full method for DE.</p> <p>Co – must be exactly 16.20, not more or less places.</p>
<p>7 $\frac{dy}{dx} = 5 - \frac{8}{x^2}$, Normal $3y + x = 17$</p> <p>(i) Gradient of line = $-\frac{1}{3}$ $\frac{dy}{dx} = 3 \rightarrow x = 2, y = 5$</p> <p>(ii) $y = 5x + 8x^{-1} (+c)$ Uses $(2, 5) \rightarrow c = -9$</p>	<p>B1 M1 DM1 A1 [4]</p> <p>B1 B1 M1 A1 [4]</p>	<p>co Use of $m_1 m_2 = -1$ DM1 solution. A1 co.</p> <p>co.co. doesn't need $+c$. Use of $+c$ following integration. co.</p>

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<p>8 $y = \sqrt{8x - x^2}$</p> <p>(i) $\frac{dy}{dx} = \frac{1}{2}(8x - x^2)^{-\frac{1}{2}} \times (8 - 2x)$ $= 0$ when $x = 4$. $\rightarrow (4, 4)$</p> <p>(ii) $y = 0$ when $x = 0$ or 8 $\text{Vol} = \pi \int (8x - x^2) dx$ $= \pi \left[4x^2 - \frac{x^3}{3} \right]$ $\rightarrow \frac{256\pi}{3}$</p>	<p>B1 B1 M1 A1 [4]</p> <p>B1</p> <p>B2,1</p> <p>B1 [4]</p>	<p>B1 for everything but $\times(8-2x)$ B1 for $\times(8-2x)$, even if B0 Sets to 0 + attempt at solution. Co – A0 if fortuitous because of B0 earlier.</p> <p>Anywhere</p> <p>–1 for each error (not including π)</p> <p>co</p>
<p>9 (i) Gradient of $AC = \frac{1}{2}$ Gradient of $BD = -2$ Eqn of BD is $y - 6 = -2(x - 3)$ Eqn of AC is $y + 1 = \frac{1}{2}(x + 1)$ Sim eqns $\rightarrow M(5, 2)$ Vector move – or midpoint back $\rightarrow D(7, -2)$</p> <p>(ii) Ratio of $AM : MC = \sqrt{45} : \sqrt{20}$ or Vector step $\rightarrow 3 : 2$</p>	<p>B1 M1 M1 M1 A1</p> <p>M1 A1√ [7]</p> <p>M1 A1 [2]</p>	<p>co Use of $m_1 m_2 = -1$ with AC Correct formula for straight line</p> <p>Solution. co</p> <p>Correct method. $\sqrt{\quad}$ on M.</p> <p>Correct distance formula. Looks at the two x or y steps. Must be numerical, 1.5 ok, not as roots</p>
<p>10 (a) $a = -15, n = 25$</p> <p>(i) Use of $S_n \rightarrow d = 3$.</p> <p>(ii) Last term $= a + 24d$ $\rightarrow 57$ (or $525 = \frac{1}{2} \times 25 \times (-15 + l) \rightarrow l = 57$)</p> <p>(iii) Positive terms are 3, 6, ..., 57 Either $a = 0$ or 3, $n = 19$ or 20 Use of S_{19} or S_{20} $\rightarrow 570$</p> <p>(b) $r = 1.05$</p> <p>(i) 11th term $= ar^{10} = \\$6516$ or $\\$6520$</p> <p>(ii) $S_{11} = \frac{4000 \times (1.05^{11} - 1)}{.05}$ $= \\$56800$ or (56827)</p>	<p>M1 A1 [2]</p> <p>M1 A1√ [2]</p> <p>M1 A1 [2]</p> <p>B1</p> <p>B1 [2]</p> <p>M1 A1 [2]</p>	<p>Must be correct formula. co</p> <p>Must be $a + 24d$ $\sqrt{\quad}$ for his d.</p> <p>Correct use of formula for S_n.</p> <p>co</p> <p>In either part (i) or (ii).</p> <p>co</p> <p>Correct sum formula with their r. co</p>