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1	$6C4 \times [2(x)]^4 \times \left[ \frac{1}{(x^2)} \right]^2$ 240	B2 B1	[3]	B1 for 2/3 terms correct Identified as answer. Allow $240x^0$
2	$\frac{\partial y}{\partial x} = 9x^2 - 12x + 4$ $(3x - 2)^2 \geq 0$	M1A1 A1	[3]	
3	(ii) Correct cosine curve for at least 1 oscillation Exactly 2 complete oscillations in $[0, 2\pi]$ Line $y = \frac{1}{2}$ correct	B1 B1 B1	[3]	Range $-1 \rightarrow 1$ . Ignore labels on $\theta$ axis
	(ii) 4	B1✓	[1]	Ft <i>their</i> graph. Accept $30^\circ$ , $150^\circ$ , $210^\circ$ , $330^\circ$
	(iii) 20	B1✓	[1]	Or $5 \times$ <i>their</i> part (ii)
4	(i) 3	B1	[1]	
	(ii) $f(x) = x^2 - 6x(+c)$ Subst $(3, -4)$ $c = 5 \rightarrow f(x) = x^2 - 6x + 5$	M1A1 M1 A1	[4]	Dependent on $c$ present cao
5	(i) Arc $AB = r\theta$ $OC = r \sin \theta$ or $BC = r \cos \theta$ $r(1 + \theta + \cos \theta + \sin \theta)$ correctly derived	M1 M1 A1	[3]	oe eg $BC = r \sin \frac{\theta}{\tan \theta}$ etc $OC$ & $BC$ reversed loses M1A1
	(ii) Sector $OAB = \frac{1}{2} \times 10^2 \times \frac{\pi}{5}$ ( $= 31.42$ ) $\Delta OCB = \frac{1}{2 \left( 10 \cos \frac{\pi}{5} \right) \left( 10 \sin \frac{\pi}{5} \right)}$ ( $= 23.78$ ) Total area = 55.2	M1 M1 A1	[3]	oe $\Delta$ in terms of $\pi$ and 10  Allow $OC$ & $BC$ reversed (ie max 4/6)
6	(a) $a + 5d = 23$ $5(2a + 9d) = 200$ Attempt solution, expect $d = 6$ $a = -7$ 29	B1 B1 M1 A1	[4]	Solution of 2 linear equations

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	<b>(b)</b> $\frac{1}{1-r} (=) \frac{4}{1-\frac{1}{4}r}$  $r = \frac{4}{5}$ oe $S = 5$	M1  A1A1		Use of $S_{\infty}$ formula twice  [3]
7	<b>(i)</b> $y = \frac{1}{6(48-8x)}$ oe  <b>(ii)</b> $A = 4xy + 2xy$ or $3xy + 3xy = 6xy$ $A = x(48-8x) = 48x - 8x^2$	B1  M1  A1	[1]   [2]	   AG
	<b>(iii)</b> $\frac{\partial A}{\partial x} = 48 - 16x$  $A = 72$ cao  $\frac{\partial^2 A}{\partial x^2} = -16$ ( $< 0$ ) $\Rightarrow$ Maximum	B1  M1A1  B1	   [4]	Attempt to solve derivative = 0 Expect $x = 3$  www Accept other complete methods
8	<b>(i)</b> $(4i + 7j - pk) \cdot (8i - j - pk) = 25 + p^2$	M1A1	[2]	$x_1x_2 + y_1y_2 + z_1z_2$ (Not $25 + (-p)^2$ )
	<b>(ii)</b> $25 + p^2 = 0 \Rightarrow$ no real solutions	B1✓	[1]	Ft provided equation has no real solutions
	<b>(iii)</b> $\cos 60 = \frac{OA \cdot OB}{ OA  OB }$ used  $ OA  = \sqrt{65 + p^2}$ or $ OB  = \sqrt{65 + p^2}$  $\frac{25 + p^2}{65 + p^2} = \frac{1}{2}$ or $\frac{\text{his scalar (i)}}{65 + p^2} = \frac{1}{2}$  $p = \pm 3.87$ or $\pm \sqrt{15}$	M1  M1  A1✓  A1	   [4]	$OA \cdot OB$ must be scalar  Not $\sqrt{65 - p^2}$ unless follows $\sqrt{65 + (-p)^2}$  Scalar product = $25 + p^2$ can score here if not scored in part (i)
9	<b>(i)</b> $x^2 + 3x + 4 = 2x + 6 \Rightarrow x^2 + x - 2 (= 0)$ $(x-1)(x+2) = 0 \rightarrow (1,8), (-2,2)$  $AB = \sqrt{3^2 + 6^2} = 6.71$ or $\sqrt{45}$ or $3\sqrt{5}$  $\left(-\frac{1}{2}, 5\right)$	M1  DM1A1  B1  B1✓	   [5]	3-term simplification  DM1 for attempted solution for x  cao ( $\sqrt{45}$ from wrong points scores B0)  Ft <i>their</i> coordinates

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	<p>(ii) <math>x^2 + (3-k)x + 2k - 6 (= 0)</math></p> <p><math>(3-k)^2 - 4(2k-6) = 0</math></p> <p><math>(3-k)(11-k) = 0</math></p> <p><math>k = 3</math> or <math>11</math></p>	<p>M1</p> <p>DM1</p> <p>DM1</p> <p>A1</p>	<p>[4]</p>	<p>Simplified to 3-term quadratic</p> <p>Apply <math>b^2 - 4ac = 0</math> as function of <math>k</math> only</p> <p>Attempt factorisation or use formula</p> <p>Both correct</p> <p>NB Alternative methods for (ii) possible</p>
10	(i) $B = (0,1)$ $C = (4,3)$	B1, B1	[2]	If B0B0 then SCB1 for both $y = 1$ & $x = 4$
	<p>(ii) <math>\frac{\delta y}{\delta x} = \frac{1}{2} \times 2(1+2x)^{-\frac{1}{2}}</math></p> <p>Grad. of normal <math>= -3</math></p> <p><math>y - 3 = -3(x - 4)</math> or <math>y = -3x + 15</math> oe</p>	<p>M1A1</p> <p>B1</p> <p>B1✓</p>	<p>[4]</p>	<p><math>-\frac{1}{2}</math> required &amp; at least one of <math>\frac{1}{2} \times 2</math> for M1</p> <p>Ft only from <i>their</i> C</p>
	<p>(iii) <math>y^2 = 1 + 2x \Rightarrow x = \frac{1}{2(y^2 - 1)}</math> SOI</p> <p><math>(\pi) \times \frac{1}{4} \times \int (y^4 - 2y^2 + 1) \delta y</math></p> <p><math>(\pi) \times \frac{1}{4} \left[ \frac{y^5}{5} - \frac{2y^3}{3} + y \right]</math></p> <p><math>(\pi) \times \frac{1}{4} \left[ \frac{1}{5} - \frac{2}{3} + 1 \right]</math></p> <p><math>\frac{2}{15} \pi</math></p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>DM1</p> <p>A1</p>	<p>[5]</p>	<p><math>\int x^2 \delta y</math>, square <math>\frac{1}{2}(y^2 - 1)</math> &amp; attempt <math>\text{int}^n</math></p> <p>Apply limits <math>0 \rightarrow \text{their } 1</math> (from <i>their</i> B)</p> <p>cao SCB1 for <math>\int y^2 \delta x \rightarrow \frac{\pi}{4}</math> (scores 1/5)</p>
11	(i) $2(x-2)^2 + 2$	B 1, B1, B1	[3]	For 2, -2, 2
	(ii) $2 \leq f(x) \leq 10$ oe	B1	[1]	Allow < etc. Ignore notation
	(iii) $2 \leq x \leq 10$	B1✓	[1]	Ft from part (ii). Ignore notation
	<p>(iv) <math>f(x)</math>: <math>\approx</math> half parabola from (0,10) to (2,2)</p> <p><math>g(x)</math>: line through 0 at <math>\approx 45^\circ</math></p> <p><math>f^{-1}(x)</math>: reflection of <i>their</i> <math>f(x)</math> in <math>g(x)</math></p> <p>Everything totally correct</p>	<p>B1</p> <p>B1</p> <p>B1✓</p> <p>B1</p>	<p>[4]</p>	<p>Or from int with <math>y</math> axis to int with <i>their</i> <math>y = x</math></p>

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	<p>(v) <math>(x-2)^2 = \frac{1}{2}(y-2)</math></p> <p><math>x = 2 \pm \sqrt{\frac{1}{2}(y-2)}</math></p> <p><math>f^{-1}(x) = 2 - \sqrt{\frac{1}{2}(x-2)}</math></p>	<p>M1</p> <p>M1</p> <p>A1</p>	<p>[3]</p>	<p>Allow <math>+\sqrt{\quad}</math> or <math>-\sqrt{\quad}</math>. Dep on final ans as <math>f^n</math> of <math>x</math></p> <p>cao</p>
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