9709 w10 ms 73

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| 1 | Normal <br> 31 for mean <br> $\sqrt{31}$ or 5.57 for sd | $\begin{array}{\|l} \mathrm{B} 1 \\ \mathrm{~B} 1 \\ \mathrm{~B} 1 \\ \hline \end{array}$ | [3] | For mean Must be sd |
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| 2 | (i) Only the more committed or less busy etc Only readers of that particular issue | B1 B1 | [2] | Any sensible category of readers who will not respond implied |
|  | (ii) Three randomly generated 4-digit numbers given <br> 49753952 (0)386 | B1 B1dep |  | Starting with 4975 <br> Accept 497502395203 and 497552036088 SC alternative consistent methods producing a set of 3 randomly generated 4 digit numbers can score B1 for the first number and B1dep for all three numbers, all <=7302 |
| 3 | $\text { (i) } \begin{aligned} & 29.6 \pm z \times^{1.0} / /_{65} \\ & 29.6 \pm 2.576 \times 1.0 / \sqrt{65} \\ & (29.6 \pm 0.3195) \\ & (29.3,29.9)(3 \mathrm{sfs}) \end{aligned}$ | M1 <br> A1 | [3] | Allow any value of $z$ <br> For 2.576 seen <br> Allow any brackets or none, but cwo. |
|  | (ii) CI does not include 30 <br> Claim not supported or not justified or probably not true | B1ft <br> B1ft |  | 30 seen or implied |
|  | (iii) CI is a variable oe | B1 | [1] | Allow "Sample mean diff" ( not population mean ). |
| 4 | $\begin{aligned} & \mathrm{E}(V)=46+53+2 \times 25=149 \\ & \operatorname{Var}(V)=19^{2}+23^{2}+4 \times 10^{2} \\ & =1290 \\ & \frac{93-149}{\sqrt{1290^{\prime}}} \\ & =-1.559 \\ & 1-\Phi\left({ }^{{fb1fec35a-7995-4a18-9afb-32eb7ddb84c3}} 1.559^{`}\right) \\ & =0.9405 \end{aligned}$ | B1 M1 A1 M1 A1ft M1 A1 | [7] | or $\sqrt{ }\left(19^{2}+23^{2}+4 \times 10^{2}\right)$ <br> or $\sqrt{ } 1290$ or 35.9 <br> With their mean and their variance. <br> ft their mean and variance providing 3 random variables used, allow $+/$-. <br> Area consistent with their mean <br> Accept 0.940 or 0.941 or 0.94 |
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| 5 | $\text { (i) } \begin{align*} & \int_{2}^{4} \frac{x^{2}}{6} \mathrm{~d} x \quad\left(=\left[\frac{x^{3}}{18}\right]_{2}^{4}\right) \\ & =\frac{4^{3}}{18}-\frac{2^{3}}{18} \\ & =\frac{28}{9} \tag{3} \end{align*}$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | Attempt integ $x \mathrm{f}(x)$, ignore limits <br> Subst correct limits in $\frac{x^{3}}{n}$ <br> oe |
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|  | (ii) | M1 M1 A1 | Attempt integ $\mathrm{f}(x)$ and $=0.5$ (ignore limits). <br> Attempt integ $\mathrm{f}(x)$, limits 2 to unknown or unknown to 4 . Or by areas. <br> $\sqrt{ } 10$ or $3.16(3 \mathrm{sfs})$ |
|  | $\text { (iii) } \begin{aligned} & \int_{3}^{4} \frac{x}{6} \mathrm{~d} x \quad\left(=\left[\frac{x^{2}}{12}\right]_{3}^{4}=7 / 12\right) \\ &\left({ }^{(67} / 12{ }^{2}\right)^{2} \\ &= 49 / 144 \text { or } 0.340(3 \mathrm{sfs}) \end{aligned}$ | $\begin{aligned} & \text { M1* } \\ & \text { M1*dep } \\ & \text { A1 } \end{aligned}$ | Attempt integ $\mathrm{f}(x)$, one limit must be 3 . <br> Square their ${ }^{* 7 / 12 "}$ |
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| 6 | (i) $\begin{aligned} & \bar{x}=43.5 / 100=0.435 \\ & s=\sqrt{\frac{100}{99}} \times \sqrt{\frac{31.56}{100}-0.435^{2}}(=0.3573) \\ & \text { or } \operatorname{Var}(=0.128) \text { or } 1 / 99\left(31.56-(43.5)^{2} / 100\right) \\ & \mathrm{H}_{0}: \text { Pop mean }(\text { for } \mathrm{B})=0.336 \\ & \mathrm{H}_{1}: \text { Pop mean }(\text { for } \mathrm{B}) \neq 0.336 \\ & \frac{0.435-0.336}{\frac{\mathrm{n}_{0} .3573^{\prime \prime}}{\sqrt{100}}} \\ & =2.77(3 \text { sfs) } \\ & \mathrm{Z}_{\text {crit }}=2.576 \\ & \text { (or } 2.326 \text { consistent with 1-tail test ) } \\ & \text { Valid comparison with } z \text {-value } \end{aligned}$ <br> Evidence that B amounts diff from A | B1 <br> M1 <br> B1 <br> M1 <br> A1 <br> B1 <br> M1 <br> A1ft |  | $\begin{aligned} & s=\sqrt{\frac{31.56}{100}-0.435^{2}} \\ & (=0.3555), \text { or } \operatorname{Var}(=0.126) \end{aligned}$ <br> Undefined mean: B0, but allow just " $\mu$ " $\frac{0.435-0.336}{\frac{\overbrace{0.3555 "}^{\sqrt{100}}}{}} \mathrm{M} 1$ <br> Or $\mathrm{X}_{\text {crit }}=$ $0.336+/=" 2.576 " \sqrt{ }(0.12765 / 100)$ <br> Or $\mathrm{x}_{\text {crit }}=(0.244)$ or 0.428 A 1 $\mathrm{z}=2.785(3 \mathrm{sfs}) \mathrm{A} 0$ <br> Or use of area - correct 0.005 (2-tail) or 0.01 (1-tail) <br> Valid comp $\mathrm{P}(z>2.77)$ with 0.005 or 0.01 <br> Or comp 0.435 with " 0.428 " <br> No errors seen. Conclusion consistent with their $\mathrm{H}_{0} / \mathrm{H}_{1}$.No contradictions. |
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|  | (ii) Must state or imply "No" to score these marks <br> $n$ large <br> $\bar{X}$ approx normally distr or CLT applies |  | [2] | B0 for "No" with invalid (or no) reason <br> SR both reasons correct but wrong conclusion scores SR B1. |
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| 7 |  | $\begin{aligned} & \mathrm{H}_{0}: \text { mean no. sales }=2.4 \\ & \mathrm{H}_{1}: \text { mean no. sales }>2.4 \\ & \mathrm{P}(X \geq 5) \\ & =1-\mathrm{e}^{-2.4}\left(1+2.4+\frac{2.4^{2}}{2!}+\frac{2.4^{3}}{3!}+\frac{2.4^{4}}{4!}\right. \\ & (=1-0.9041) \\ & =0.0959 \end{aligned}$ <br> Comp with 0.05 <br> No evidence to believe mean sales incr | B1 <br> M1* <br> A1 <br> A1 <br> M1* <br> A1ft dep [6] | Or "= 0.8 per week" <br> Accept $\lambda, \operatorname{not} \mu$. <br> Attempted with or without "1-". <br> Allow one end error. <br> Allow incorrect $\lambda$ in otherwise correct expression. <br> Indep M. (Allow recovery of above 3 marks at this point if comparison with 0.95 done.) Conclusion, no contradictions. SC: $\mathrm{e}^{-2.4} \times \frac{2.4^{5}}{5!}=0.0602>0.05$ : $\max$ B1M0A0A0M1A0 |
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|  |  | Need $1^{\text {st }} x$ such that $\mathrm{P}(X \geq x)<0.05$ $\begin{aligned} & \mathrm{P}(X \geq 6)=1-\mathrm{e}^{-2.4}\left(1+2.4+\ldots+\frac{2.4^{5}}{5!}\right) \\ & (=1-0.9643) \\ & =0.0357 \end{aligned}$ | M1* M1*dep <br> A1 | Attempt sum of at least 3 relevant Poisson terms, with comparison with 0.05 (can be implied). <br> Can be implied, e.g. by $\mathrm{P}(X \leq 5)=0.9643$ identified. |
|  | (iii) | Mean sales still 0.8 per week, but $\geq 6$ sales in 3 weeks, so reject 0.8 . | B1 [1] | Conclude mean sales have increased when not true |
|  | (iv) | Value of true (new, changed) mean oe | B1 [1] |  |

