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	GCE A LEVEL – October/November 2010	9709	72

1	$0.605 \pm z \times \sqrt{\frac{0.605 \times (1 - 0.605)}{1000}}$ $z = 1.645 \text{ seen}$ $[0.580, 0.630]$	M1 B1 A1 [3]	Allow [0.58, 0.63]. Allow any brackets
2	<b>(i)</b> $e^{-\frac{10}{3}} \times \frac{(\frac{10}{3})^4}{4!}$ $= 0.184 \text{ or } 0.183$	M1 A1 [2]	Allow incorrect $\lambda$
	<b>(ii)</b> $\lambda = 5$ $e^{-5} (1 + 5 + \frac{5^2}{2})$ $= 0.125 \text{ (3 sfs)}$	B1 M1 A1 [3]	Allow incorrect $\lambda$ . Allow one end error OR Combination method scores B1, identifying all 6 possible combinations M1, multiply each combination and add (must use at least 5 combinations) A1
3	<b>(i)</b> B(40 000, 0.0001)	B1 [1]	
	<b>(ii)</b> Po(4) $n = 40\,000 > 50$ , $np = 4 < 5$	B1*B1*dep B1 [3]	B1 for Po. B1 for 4 Accept 40000 large and 0.0001 small
	<b>(iii)</b> $1 - (P(X \leq 3) \text{ or } e^{-4} (1 + 4 + \frac{4^2}{2} + \frac{4^3}{3!}))$ $1 - e^{-4} (1 + 4 + \frac{4^2}{2} + \frac{4^3}{3!})$ $= 0.567 \text{ or } 0.566$	M1 M1 A1 [3]	Allow one end error (any $\lambda$ ) Expression of correct form (any $\lambda$ ), no end errors. (OR Use of normal scores M1, standardising M1, standardising with correct cc A1ft, <b>(ii)</b> 0.599. Award A mark only if normal given in <b>(ii)</b> ) (OR Binomial M1 expression of correct form allow end error, M1 correct form no end error, A1ft 0.567 or 0.566. Award A mark only if Bin given in <b>(ii)</b> ) NB Part <b>(iii)</b> must be Poisson or ft from <b>(ii)</b> for A mark to be awarded. SR If no answer given in <b>(ii)</b> allow BOD for A marks.

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4	(i) $0.5(0.5 + 0.75) \times 0.5$ or $\int_1^{1.5} \frac{x}{2} dx$ $= \frac{5}{16}$ or 0.3125 or 0.313	M1 A1	[2]	Attempt find correct area eg 1 squ + $\frac{1}{4}$ squ or integral with correct limits any $f(x)$
	(ii) $\frac{1}{2}m \times \frac{m}{2}$ or $\int_0^m \frac{x}{2} dx$ $= \frac{1}{2}$ $m = \sqrt{2}$ or 1.41	M1 M1 A1	[3]	Attempt area from 0 to $m$ (or $m$ to 2) their $f(x)$ Expression for area = $\frac{1}{2}$ . Ignore limits
	(iii) $\int_0^2 \frac{x^2}{2} dx$ $= \frac{4}{3}$ oe	M1 A1	[2]	Attempt $\int xf(x)dx$ . Ignore limits
5	(i) $E(F) = 28 + \frac{1}{2} \times 52 = 54$ $\text{Var}(F) = 5.6^2 + \frac{1}{4} \times 12.4^2 = 69.8$	B1 M1 A1	[3]	$\sqrt{69.8}$ or 8.35: M1A0
	(ii) $H_0$ : Grinford mean = 54; $H_1$ : Grinford mean < 54  $\frac{49 - 54}{\sqrt{\frac{69.8}{10}}}$ $= -1.89(3)$ or $-1.89(2)$ allow + Comp with $-1.645$ (or 1.893 with 1.645)  Evidence that Grinford mean lower	B1ft  M1 A1 M1  A1ft	[5]	Allow “ $\mu$ ”, otherwise undefined mean: B0 ft their 54  Standardising must have $\sqrt{10}$  Comp $P(z < -1.893)$ with 0.05 Allow comparison with 1.96 for consistent 2-tail test Allow “Accept Grinford mean lower” No contradictions OR Alt methods $(x - 54)/(\sqrt{(69.8/10)}) = 1.645$ giving $x = 49.65$ compare with 49 scores M1A1M1A1ft. oe. No mixed methods.

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6	(i)	$H_0: P(6) = \frac{1}{6}$ $H_1: P(6) > \frac{1}{6}$ $1 - ((\frac{5}{6})^{10} + 10(\frac{1}{6})(\frac{5}{6})^9 + {}^{10}C_2(\frac{1}{6})^2(\frac{5}{6})^8)$ $= 0.225$ (3 sfs) $0.225 > 0.1$  No evidence that die biased	B1 M1 A1 M1 A1ft [5]	Allow "p"  Allow 1 term omitted or extra or incorrect  Allow correct comparison with 0.9, and recovery of previous then M1A1 possible. Allow Accept die not biased. In context. SR Calc just P(3)max score B1M0A0M1A0
	(ii)	P(4 or more sixes) $= 1 - ((\frac{5}{6})^{10} + 10(\frac{1}{6})(\frac{5}{6})^9 + {}^{10}C_2(\frac{1}{6})^2(\frac{5}{6})^8 + {}^{10}C_3(\frac{1}{6})^3(\frac{5}{6})^7)$ $= 0.0697$ or $0.0698$	M1 M1 A1 [3]	Idea of $1 - \Sigma$ of terms oe compared with 0.1 $1 - \Sigma$ of appropriate no.terms oe compared with 0.1
	(iii)	Concluding die is fair when die is biased	B1 [1]	Must be in context
7 (a)	(i)	Pop too large Not all pop accessible	B1 [1]	Time consuming Or similar
	(ii)	Testing involves destruction	B1 [1]	Or similar
7 (b)	(i)	$\frac{9850}{500} = (19.7)$ $\frac{500}{499}(\frac{194125}{500} - (\frac{9850}{500})^2)$ $= 0.160(32)$ (3 sfs) or $80/499$	B1 M1 A1 [3]	Allow with $\sqrt{\quad}$ . Method must be seen or clearly implied.
	(ii)	$\frac{19.73 - 19.7}{\sqrt{\frac{0.160}{60}}}$ $= 0.580$ or $0.581$ $1 - \Phi("0.580")$ $(= 1 - 0.7191)$ $= 0.281$	M1 A1ft M1 A1 [4]	For standardising  ft their mean and var in (b)(i) Correct tail
	(iii)	"Yes" must be seen or implied to gain mks $X$ not nec'y normal Sample large	B1 B1 [2]	or $\bar{X}$ is approx N (SR Both reasons correct, but wrong or no conclusion scores SR B1)