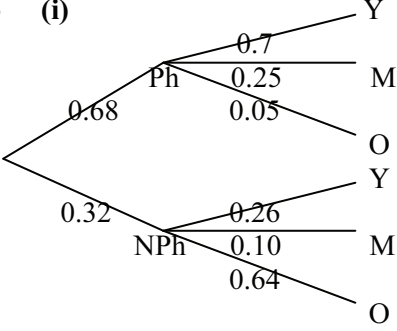


Page 4	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE A LEVEL – October/November 2010	9709	63

<p>1 Normal mean 60 kg, variance 90 kg²</p>	<p>B1 B1 [2]</p>	<p>Any sensible values (mean 40–80 kg, variance 16–225 kg²), could give s.d. 4–15 kg</p>												
<p>2 (i)</p> <table border="1" data-bbox="245 450 724 524"> <tr> <td>x</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>Prob</td> <td>k</td> <td>$2k$</td> <td>$3k$</td> <td>$4k$</td> <td>$5k$</td> </tr> </table> <p>$15k = 1$ $k = 1/15$ (0.0667)</p>	x	1	2	3	4	5	Prob	k	$2k$	$3k$	$4k$	$5k$	<p>M1 M1 A1 [3]</p>	<p>1, 2, 3, 4, 5 seen, together with some probabilities involving k but not x summing probs involving k to 1 correct answer</p>
x	1	2	3	4	5									
Prob	k	$2k$	$3k$	$4k$	$5k$									
<p>(ii) $E(X)$ $= k + 4k + 9k + 16k + 25k$ $= 55k = 11/3$ (3.67)</p>	<p>M1 A1ft [2]</p>	<p>using Σpx no dividing correct answer, ft on $55k$, $0 < k < 1$</p>												
<p>3 (i)</p> 	<p>M1 A1 [2]</p>	<p>Y = young, M = middle-aged, O = old Correct shape with Ph, NPh first All probabilities and correct</p>												
<p>(ii) $P(\text{Ph} \text{M}) = \frac{0.68 \times 0.25}{0.68 \times 0.25 + 0.32 \times 0.1}$ $= 0.842$ (170/202)</p>	<p>B1 M1 A1 [3]</p>	<p>For correct numerator using cond prob formula with numerator < denominator For attempt at $P(35 - 60 \text{ years old})$, involving the sum of two 2-factor probs, seen anywhere Correct answer</p>												
<p>4 (i) $\bar{x} = 60 + 245/70$ $= 63.5$</p>	<p>M1 A1 [2]</p>	<p>245/70 seen Correct answer</p>												
<p>(ii) $\Sigma(x - 50) = \Sigma x - \Sigma 50$ $= 245 + 70 \times 60 - 70 \times 50$ $= 945$</p>	<p>M1 A1 [2]</p>	<p>Any valid method, involving 70 Correct answer</p>												
<p>(iii) coded mean $= 945/70 = 13.5$ $\frac{\Sigma(x - 50)^2}{70} - \left(\frac{945}{70}\right)^2 = 10.6^2$ $\Sigma(x - 50)^2 = 20623$ (20600)</p>	<p>M1 A1 [2]</p>	<p>Using variance formula with coded mean Correct answer</p>												

Page 5	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE A LEVEL – October/November 2010	9709	63

5 (i) <table border="1" style="margin-left: 20px;"> <tr> <td>2 to 4</td> <td>4 to 6</td> <td>6 to 7</td> <td>7 to 8</td> <td>8 to 10</td> <td>10 to 16</td> </tr> <tr> <td>20</td> <td>44</td> <td>34</td> <td>30</td> <td>30</td> <td>36</td> </tr> </table>	2 to 4	4 to 6	6 to 7	7 to 8	8 to 10	10 to 16	20	44	34	30	30	36	M1 A1 A1 [3]	Using fd to evaluate freqs Any four correct All correct
	2 to 4	4 to 6	6 to 7	7 to 8	8 to 10	10 to 16								
	20	44	34	30	30	36								
(ii) mid-points 3, 5, 6.5, 7.5, 9, 13 $E(X) = (3 \times 20 + 5 \times 44 + 6.5 \times 34 + 7.5 \times 30 + 9 \times 30 + 13 \times 36) / 194 = 1464/194$ $= 7.55$	M1 A1ft [2]	5 or 6 correct mid-points Correct answer, ft on 6 correct mid-points and the frequencies in their table												
(iii) $p = 60/194$ (0.309) $P(1) = 2 \times (60/194)(134/193)$ $= 8040/18721$ (0.429)	B1ft M1 A1 [3]	60/194 seen, ft on (their 30 + their 30) / their total multiplying a probability by 2 Correct answer												
6 (i) ${}^{14}P_{12}$ $= 4.36 \times 10^{10}$	M1 A1 [2]	${}^{14}P_{12}$ seen oe Correct answer												
(ii) business people $3! = 6$ students $5! = 120$ married couples ${}^3P_2 \times 2 \times 2 = 24$ total ways = 17280	B1 B1 B1 B1 [4]	3! oe seen, not in denominator 5! oe seen, not in denominator 24 oe seen, not in denominator correct final answer												
(iii) Mrs Brown 3 Mrs Lin 10 Student 5 Prob = $3 \times 10 \times 5 \times {}^{11}P_9$ / (i) $= 0.0687$ OR ₁ $3/14 \times 10/13 \times 5/12 = 150/2184$ (0.0687) OR ₂ $1 - 3/14 = 11/14$ $1 - 11/14 \times 5/13 = 127/182$ $8/14(4/13 \times 12/12 + 9/13 \times 7/12) +$ $3/14(3/13 \times 12/12 + 10/13 \times 7/12)$ $= 1206/2184$ $1 - (1524 + 1716 - 1206)/2184 = 150/2184$	B1 B1 M1 A1 [4] B1 B1 M1 A1 B1 B1 M1 A1	any 2 of 3, 10, 5 oe seen, not in denominator ${}^{11}P_9$ seen multiplied dividing by their (i) correct answer any 2 of numerators 3, 10, 5 oe seen denominators 14, 13, 12 of 3 fractions multiplying 3 separate fractions correct answer $1 - 3/14$ seen $1 - 11/14 \times 5/13$ seen attempt to find P(Mrs Lin not behind a student and Mrs Brown not in front row), involving $8/14 \times \text{prob} + 3/14 \times \text{prob}$ correct answer												

Page 6	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE A LEVEL – October/November 2010	9709	63

<p>7 (i) $z = 0.807$</p> $0.807 = \frac{10 - 8.2}{\sigma}$ $s = 2.23$	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>0.807 seen</p> <p>standardising, must have σ, no sq rt, no cc and a z-value</p> <p>correct answer</p>
<p>(ii) $P(> 1 \text{ min from mean}) = P(\text{mod } z > \frac{1}{2.23})$</p> $= P(z > 0.4484)$ $= (1 - 0.6729) \times 2$ $= 0.654$	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>standardising, their sd, no cc and adding two areas</p> <p>using $1 - \Phi(z)$</p> <p>correct answer</p>
<p>(iii) $P(> 2 \text{ longer}) = 1 - P(0, 1, 2 \text{ longer})$</p> $= 1 - \{(0.79)^6 + {}^6C_1(0.21)(0.79)^5 + {}^6C_2(0.21)^2(0.79)^4\}$ $= 0.112$	<p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p>	<p>binomial term ${}^6C_x p^x (1-p)^{6-x}$</p> <p>correct unsimplified answer</p> <p>correct answer</p>
<p>(iv) $\mu = 35 \times 0.5 = 17.5$</p> $\sigma^2 = 35 \times 0.5 \times 0.5 = 8.75$ $P(X < 16) = \Phi\left(\frac{15.5 - 17.5}{\sqrt{8.75}}\right)$ $= 1 - \Phi(0.676)$ $= 1 - 0.7505$ $= 0.2495 \text{ (0.249 or 0.250)}$ <p>OR ${}^{35}C_0 0.5^0 0.5^{35} + {}^{35}C_1 0.5^1 0.5^{34} + {}^{35}C_2 0.5^2 0.5^{33} + \dots$</p> $= 8582372584/2^{35} = 0.250$	<p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[5]</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>17.5 and 8.75 or $\sqrt{8.75}$ seen</p> <p>standardising, with or without cc, must have sd in denom</p> <p>continuity correction 15.5 or 16.5 only, seen</p> <p>using $1 - \Phi(z)$</p> <p>correct answer</p> <p>binomial term ${}^{35}C_x 0.5^x 0.5^{35-x}$</p> <p>at least 2 correct terms ($x \geq 0$) seen</p> <p>summing 16 or 17 terms</p> <p>correct expression</p> <p>correct answer</p>