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1	(i) $2mx0.45 + mx0.3 = 3mv$	M1	Table of values idea
	$v = 0.4m$ (from AB)	A1	
	$2mx0.45 + mx(0.9+0.3) = 3mh$	M1	Table of values idea
	$h = 0.7m$ (from AD)	A1 [4]	
	(ii) $\tan \alpha = 0.4/0.7$	M1	
	$\alpha = 29.7^\circ$	A1ft [2]	Accept 0.519 radians
2	(i) $\tan \alpha = 5/(26\cos30^\circ)$	M1	
	$\alpha = 12.5^\circ$ (0.219rad) below the horizontal	A1	Accept $77.5^\circ/1.35\text{rad}$ with downward vertical
	$5^2 = (26\sin30^\circ)^2 - 2gs$	M1	
	$s = 7.2m$	A1 [4]	
	(ii) $-(26\sin30^\circ) = (26\sin30^\circ) - gT$	M1	Or time to greatest height if later doubled
	$T = 2.6s$	A1	
	$OA = (26\cos30^\circ) \times 2.6 = 58.5m$	A1 [3]	Or B1 for $OA = 26^2\sin(2 \times 30^\circ)/10 = 58.5$
	3	(i) $T_{PQ} = (0.4g) = 4N$	B1
	$T_{BQ} = 0.4 \times 5^2 \times 0.3$	M1	Uses $F = m\omega^2r$
	$T_{BQ} = 3N$	A1 [3]	
	(ii) $T\cos \alpha = 0.8g + 4$	M1	Attempts to find either component of T
	$T\sin \alpha = 0.8 \times 5^2 \times 0.3$	A1	Both components correct
	$T^2 = 12^2 + 6^2$	M1	Or any equivalent method to find T
	$T_{AP} = 13.4N$ ($= 6\sqrt{5}N$)	A1	
	$\alpha^\circ = \tan^{-1}(6/12) = \tan^{-1}(1/2) = 26.6^\circ$	B1ft	
	OR	$T\cos \alpha = 0.8g + 4$	M1
	$T\sin \alpha = 0.8 \times 5^2 \times 0.3$	A1	Both components correct
	$\tan \alpha = 6/12$	M1	
	$\alpha = 26.6$	A1	
	$T_{AP} = 13.4N$	B1ft [5]	

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4	(i)	M1	Moments about A
	$Fx1.2\sin60^\circ = 15 \times 0.6\cos60^\circ$	A1	
	$F = 4.33\text{N}$ AG	A1 [3]	
	(ii) $F\cos30^\circ + Fr = 15\cos60^\circ$	M1	Resolving parallel to the plane
	$Fr = 3.75\text{N}$	A1	
OR	$15 \times 0.6\cos60^\circ = 1.2Fr$	M1	Moments about B
	$Fr = 3.75\text{N}$	A1	
OR	$F\cos30^\circ \times 0.6 = Fr \times 0.6$	M1	Moments about centre of rod
	$Fr = 3.75\text{N}$	A1 [2]	
	(iii) $R = 15\cos30^\circ + 4.33\cos60^\circ$	M1	
	$R = 15.2$	A1	$R = 15.155\dots$ Accept 15.1
	$\mu (= 3.75/15.2) = 0.247$	B1ft [3]	From their F and R found but not $R=W$
5	(i) $T = \lambda(\sqrt{1.2^2 + 0.5^2} - 1)/1$	B1	$T = 0.3 \lambda$ or $T = 0.3 \times 26$
	$2 \times T \times 0.5 / 1.3 = 6$	B1	
	$T = 0.3 \lambda = 7.8$	M1	
	$\lambda = 26$ AG	A1 [4]	
	(ii) $EE_1 = 2 \times 26 \times 0.3^2 / 2 \times 1$	M1	(= 2.34) Use of EPE formula, either
	$EE_2 = 2 \times 26(\sqrt{1.2^2 + 0.9^2} - 1)^2 / 2 \times 1$	A1	(= 6.5) Both expressions correct
		M1	Conservation of energy (including KE/GPE/EPE)
	$0.6v^2/2 + 0.6 \times 10 \times (0.9 - 0.5) = 6.5 - 2.34$	A1	
	$V = 2.42\text{ms}^{-1}$	A1 [5]	

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6	(i)	M1	N2L with 3 force terms
	$0.2dv/dt = -0.5v - 0.2g\sin 30^\circ - 0.2g\cos 30^\circ / (2\sqrt{3})$	A1	$dv/dt = -2.5v - 5 - (5\sqrt{3}) / (2\sqrt{3})$
	$dv/dt = -2.5(3 + v)$ AG	A1 [3]	
	(ii) $\int dv / (3 + v) = -2.5 \int dt$	M1	Separates variables and integrates
	$\ln(3 + v) = -2.5t (+ c)$	A1	
	$t = 0, v = 2$, hence $c = \ln 5$		Or equivalent use of limits
	$\ln 3 = 2.5T + \ln 5$	M1	$[\ln(3 + v)]_2^0 = [-2.5]_0^T$
	$T = 0.204$	A1 [4]	$T = 0.4\ln(5/3)$
	(iii) $0.2dv/dt = 0.2g\sin 30^\circ - 0.2g\cos 30^\circ / (2\sqrt{3}) - 0.5v$	M1	$dv/dt = 5 - 2.5v - (5\sqrt{3}) / (2\sqrt{3})$
	$\int dv / (1 - v) = 2.5 \int dt$	A1	
	$-\ln(1 - v) = 2.5t (+ c)$		
	$t = 0, v = 0$, hence $c = 0$	B1	Or equivalent
	$-\ln(1 - v) = 2.5 \times 0.4\ln(5/3)$	M1	Uses $t = T$
	$v = 0.4\text{ms}^{-1}$	A1 [5]	