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<b>1</b>	M1 $R + 2000\cos 15^\circ = 400g$ A1 $F = 2000\sin 15^\circ$ B1 $[2000\sin 15^\circ = \mu(400g - 2000\cos 15^\circ)]$ M1 Coefficient is 0.25 A1	For resolving forces vertically (3 terms required)      For using $F = \mu R$	<b>[5]</b>
	SR(max. 4/5) for candidates who either: have sin and cos interchanged or have angle $15^\circ$ above the horizontal  M1 $R + 2000\sin 15^\circ = 400g$ and $F = 2000\cos 15^\circ$ A1 $[2000\cos 15^\circ = \mu(400g - 2000\sin 15^\circ)]$ M1 Coefficient is 0.55 A1	For resolving forces vertically   For using $F = \mu R$	
<b>2</b>	Driving force = 400/4  B1 M1 $DF - 80g \sin 2^\circ = 80a$ (i) or A1 $DF + 80g \sin 2^\circ = 80a$ (ii) A1 Acceleration is $0.9 \text{ ms}^{-2}$ (i) or A1 Acceleration is $1.6 \text{ ms}^{-2}$ (ii) A1 Acceleration is $1.6 \text{ ms}^{-2}$ (ii) and B1ft Acceleration is $0.9 \text{ ms}^{-2}$ (i)	For using Newton's second law (either case) – 3 terms needed   Accept 0.90 or 0.901 and 1.60  ft Ans (i) + (ii) = 2.5	<b>[5]</b>
	SR(max. 3/5) for candidates who have sin and cos interchanged Driving force = 400/4  B1 M1 $a = -8.74$ (i) and $a = 11.2$ (ii) A1	For using Newton's second law (either case) – 3 terms needed	
<b>3</b>	M1 $6\cos\alpha^\circ + 5\cos(90^\circ - \alpha^\circ) = F$ and A1 $6\sin\alpha^\circ - 5\sin(90^\circ - \alpha^\circ) = F$ DM1 $[6\cos\alpha^\circ + 5\sin\alpha^\circ = 6\sin\alpha^\circ - 5\cos\alpha^\circ$ $\rightarrow 11\cos\alpha^\circ = \sin\alpha^\circ]$ A1 $\alpha = 84.8$ DM1 $[F = 6\cos 84.8^\circ + 5\sin 84.8^\circ; F = 6\sin 84.8^\circ - 5\cos 84.8^\circ]$ A1 $F = 5.52$	For resolving forces in i and j directions (3 terms in at least one of the equations)   For attempting to solve for $\alpha^\circ$ . Dependent on 1 <sup>st</sup> M1  For substituting to find F; dependent on the 1 <sup>st</sup> M1	<b>[6]</b>

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First alternative scheme			
$[2F^2 = 25 + 36]$	M1		For using '(resultant of forces of magnitude F) <sup>2</sup> = (resultant of forces of magnitudes 5 and 6) <sup>2</sup> ,
$F = 5.52$	A1		
	M1		For using 'resultant of forces of magnitudes 5 and 6 makes angle 45° with x-axis'
	M1		For using relevant trigonometry
$\tan(\alpha^\circ - 45^\circ) = 5/6$ or $\tan(135^\circ - \alpha^\circ) = 6/5$ or $\cos(\alpha^\circ - 45^\circ)$ or $\sin(135^\circ - \alpha^\circ) = 6/\sqrt{61}$ or $\sin(\alpha^\circ - 45^\circ)$ or $\cos(135^\circ - \alpha^\circ) = 5/\sqrt{61}$	A1		
$\alpha = 84.8$	A1		
Second alternative scheme			
$[6\cos\alpha^\circ + 5\cos(90^\circ - \alpha^\circ)$ $= 6\sin\alpha^\circ - 5\sin(90^\circ - \alpha^\circ)]$	M1		For using $R_x = R_y$
$[11\cos\alpha^\circ - \sin\alpha^\circ = 0]$	M1		For attempting to solve for $\alpha^\circ$
$\alpha = 84.8$	A1		
For $F = 6\cos\alpha^\circ + 5\cos(90^\circ - \alpha^\circ)$ or $F = 6\sin\alpha^\circ - 5\sin(90^\circ - \alpha^\circ)$	B1		
	M1		For substituting for $\alpha$
$F = 5.52$	A1		
<b>4 (i)</b> $[1/2 \cdot 20(2.5^2 - 1.5^2), 20 \times 10 \times 10 \sin 4.5^\circ]$	M1		For using KE loss = $1/2 m(u^2 - v^2)$ or PE gain = $mg(L\sin\alpha)$
KE loss = 40 J or PE gain = 157 J	A1		
PE gain = 157 J or KE loss = 40 J	B1	<b>[3]</b>	
<b>(ii)</b> $[WD = 157 - 40 + 50]$	M1		For using WD by pulling force = PE gain – KE loss + WD against resistance
Work done is 167 J	A1ft	<b>[2]</b>	ft incorrect PE gain + 10, even if –ve
<b>(iii)</b> $[167 = Fx10\cos15^\circ]$ Magnitude is 17.3 N	M1 A1ft	<b>[2]</b>	For using $WD = FL\cos 15^\circ$
SR (max. 1/2) for candidates who (implicitly) make the unjustifiable assumption that acceleration is constant and apply Newton's second law For magnitude is 17.3 N from $F\cos 15^\circ - 20g\sin 4.5^\circ - 50/10 = 20 \times (-0.2)$	B1		

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<b>5</b>	<b>(i)</b> [ $15 = 20t - 5t^2 \rightarrow 5(t^2 - 4t + 3) = 0$ ] $t = 1, 3$ Duration is 2 s (accept $1 < t < 3$ )	M1 A1 B1ft	For use of $h = ut - \frac{1}{2}gt^2$  [3] ft $t_2 - t_1$
	<b>(ii)</b>  $20t - 5t^2 = 25(t - 0.4) - 5(t - 0.4)^2$ (or $20(t + 0.4) - 5(t + 4)^2 = 25t - 5t^2$ or $(20 \times 0.4 - 5 \times 0.4^2) + 16t - 5t^2 = 25t - 5t^2$ ) $t = 1.2$ (or $t = 0.8$ ) [ $v_P = 20 - 10 \times 1.2$ ; $v_Q = 25 - 10 \times (1.2 - 0.4)$ ] (or $v_P = 20 - 10 \times (0.8 + 0.4)$ ; $v_Q = 25 - 10 \times 0.8$ ) Velocities are $8 \text{ ms}^{-1}$ and $17 \text{ ms}^{-1}$	M1  A1 A1 M1  A1	For using $h_P = h_Q$ at time $t$ after P's (or Q's) projection    For using $v = u - gt$ for both $v_P$ and $v_Q$  [5]
<b>6</b>	<b>(i)</b> [ $\frac{1}{2} 2.5(\text{speed}_{\max}) = 4$ ] Greatest speed is $3.2 \text{ ms}^{-1}$	M1 A1	For using area property for distance  [2]
	SR (max. 1/2) for candidates who (implicitly) make the unjustifiable assumption that $\text{speed}_{\max}$ occurs when $t = 1.25$ Greatest speed is $3.2 \text{ ms}^{-1}$ from $2 \times \frac{1}{2} 1.25(\text{speed}_{\max})v = 4$	B1	
<b>(ii)</b>	[ $V = 3 \times 2$ ]  $V = 6$	M1  A1	For using $a = (V - 0)/(4.5 - 2.5)$ or $V = 0 + at$  [2]
	<b>(iii)</b>  $\frac{1}{2} 6(12 + T) = 48$ or $\frac{1}{2} 6 \times 2 + 6T + \frac{1}{2} 6(10 - T) = 48$ or $\frac{1}{2} 6 \times 2 + 6(10 - \tau) + \frac{1}{2} 6\tau = 48$ $t = 8.5$	M1  A1ft A1	For using area property for distance from $t = 2.5$ to $t = 14.5$   [3] from $4.5 + T$ or $14.5 - \tau$
<b>(iv)</b>	Deceleration is $1 \text{ ms}^{-2}$	M1 A1ft	For using $a = (0 - V)/(14.5 - 8.5)$ or $0 = V + a(14.5 - 8.5)$  [2]

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7	(i) $a(t) = 0.006t^2 - 0.24t + 1.8$	B1	
	$[0.006(t^2 - 40t + 300) = 0]$	M1	For solving $a(t) = 0$
	$T_1 = 10, T_2 = 30$	A1	
		M1	For integrating $v(t)$
	$s(t) = 0.0005t^4 - 0.04t^3 + 0.9t^2 + 5t + (C)$	A1	
	$[405 - 1080 + 810 + 150]$	M1	For using limits 0 to $T_2$ or equivalent
	Distance is 285 m	A1	[7]
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	(ii) Velocity is $5 \text{ ms}^{-1}$	B1	
	For curve with $v$ increasing from a +ve value at $t = 0$ to a maximum	B1	
	Then decreases to a +ve minimum and thereafter increases	B1	[3]