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- 1 EITHER:** State or imply non-modular inequality $(x+1)^2 > (x-4)^2$, or corresponding equation or pair of linear equations M1
- Obtain critical value $\frac{3}{2}$ A1
- State correct answer $x > \frac{3}{2}$ A1
- OR:** State a correct linear equation for the critical value, e.g. $x+1 = -x+4$, or corresponding correct linear inequality, e.g. $x+1 > -(x-4)$ M1
- Obtain critical value $\frac{3}{2}$ A1
- State correct answer $x > \frac{3}{2}$ A1 [3]
- 2** Use law for the logarithm of a product, a quotient or a power M1*
- Obtain $x \log 5 = (2x+1)\log 2$, or equivalent A1
- Solve for x , via correct manipulative technique(s) M1(dep*)
- Obtain answer $x = 3.11$. Allow $x \in [3.10, 3.11]$ A1 [4]
- 3** Integrate and obtain $\frac{1}{2}e^{2x}$ term B1
- Obtain $2e^x$ term B1
- Obtain x B1
- Use limits correctly, allow use of limits $x = 1$ and $x = 0$ into an incorrect form M1
- Obtain given answer A1 [5]
- S. R. Feeding limits into original integrand, 0/5
- 4 (i)** State $\frac{dx}{dt} = \frac{1}{t-2}$ or $\frac{dy}{dt} = 1 - 9t^{-2}$ B1
- Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$ M1
- Obtain given answer correctly A1 [3]
- (ii)** Equate derivative to zero and solve for t M1
- State or imply that $t = 3$ is admissible c.w.o., and note $t = -3, 2$ cases A1
- Obtain coordinates (1, 6) and no others A1 [3]
- 5** Use correct trig identity to obtain a quadratic in $\cot \theta$ or $\tan \theta$ M1
- Solve the quadratic correctly A1
- Obtain $\tan \theta = \frac{1}{2}$ or $-\frac{2}{3}$ A1√
- Obtain answer 26.6° or 146.3° A1
- Carry out correct method for second answer from either root M1
- Obtain remaining 3 answers from $26.6^\circ, 146.3^\circ, 206.6^\circ, 326.3^\circ$ and no others in the range A1 [6]
- [Ignore answers outside the given range]

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- 6 (i) Consider sign of $\frac{6}{x^2} - x - 1$ at $x = 1.4$ and $x = 1.6$, or equivalent M1
Complete the argument correctly with appropriate calculations A1 [2]
- (ii) State $\frac{6}{x^2} = x + 1$ B1
Rearrange equation to given equation or *vice versa* B1 [2]
- (iii) Use the iterative formula correctly at least once M1
Obtain final answer 1.54 A1
Show sufficient iterations to justify its accuracy to 2 d.p. or show there is a sign change in the interval (1.535, 1.545) B1 [3]
- 7 (i) Substitute $x = 1$, equate to zero and obtain a correct equation in any form B1
Substitute $x = 2$ and equate to 10 M1
Obtain a correct equation in any form A1
Solve a relevant pair of equations for a or for b M1
Obtain $a = -17$ and $b = 12$ A1 [5]
- (ii) At any stage, state that $x = 1$ is a solution B1
EITHER: Attempt division by $x - 1$ and reach a partial quotient of $3x^2 + 5x$ M1
Obtain quotient $3x^2 + 5x - 12$ A1
Obtain solutions $x = -3$ and $x = \frac{4}{3}$ A1
OR: Obtain solution $x = -3$ by trial and error or inspection B1
Obtain solution $x = \frac{4}{3}$ B2
- [If an attempt at the quadratic factor is made by inspection, the M1 is earned if it reaches an unknown factor of $3x^2 + 5x + \lambda$ and an equation in λ] [4]
- 8 (i) Use product rule M1
Obtain correct derivative in any form A1
Substitute $x = \frac{1}{2}\pi$, and obtain gradient of -1 for normal A1√
from $y' = \sin x - x \cos x$ ONLY
- Show that line through $\left(\frac{1}{2}\pi, \frac{1}{2}\pi\right)$ with gradient -1 passes through $(\pi, 0)$ M1
A1 [5]
- (ii) Differentiate $\sin x$ and use product rule to differentiate $x \cos x$ M1
Obtain $x \sin x$, or equivalent A1 [2]
- (iii) State that integral is $\sin x - x \cos x (+ c)$ B1
Substitute limits 0 and $\frac{\pi}{2}$ correctly M1
Obtain answer 1 A1 [3]
S. R. Feeding limits into original integrand, 0/3