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	GCE AS/A LEVEL – October/November 2010	9709	13

1	9C_6 or 9C_3 used $\left(\frac{1}{x^2}\right)^3$ seen -84	M1 B1 A1	[3]	Correct answer only \Rightarrow 3marks
2	(i) $(3\frac{1}{2}, 2)$ (ii) $m = \frac{-1-5}{5-2} = -2$ $y - 6 = \frac{-1}{m}(x - 8)$ $x - 2y + 4 = 0$	B1 B1 M1 A1	[1] [3]	Use of $m_1m_2 = -1$ and $y - k = m(x - h)$ Accept any form
3	$15\cos^2x + \cosx - 2 = 0$ $(5\cosx + 2)(3\cosx - 1) = 0$ 113(.6), 70.5	M1 M1 A1A1	[4]	$1 - \cos^2x = \sin^2x$ & attempt simplify Attempt to solve 3-term quadratic for \cosx SC 1.98, 1.23 scores 1/2
4	(i) Correct sine curve (ii) Required line $y = 1 - \frac{x}{\pi}$ Line through $(0, 1), (\pi, 0)$ drawn 3 roots	B1 B1 B1 B1 \sqrt	[1] [3]	2 shown or implied SC B1 for correct graphs without 1 or 2 marked fit on trig curve and line
5	(i) $\frac{dy}{dx} = \frac{-1}{(x-3)^2} + 1$ $\frac{d^2y}{dx^2} = \frac{2}{(x-3)^3}$ (ii) $(x-3)^2 = 1 \Rightarrow x-3 = \pm 1$ $x = 4, 2$ $y = 5, 1$ When $x = 4$ $\frac{d^2y}{dx^2} > 0 (= 2) \Rightarrow$ min When $x = 2$ $\frac{d^2y}{dx^2} < 0 (= -2) \Rightarrow$ max	B1 B1 M1 A1 A1 M1 A1	[2] [5]	oe oe Set $\frac{dy}{dx} = 0$ & reasonable attempt to solve Investigate signs of f'' at a point or other method

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6	(i) $(3x + 5)(x - 1) > 0$ $-5/3, 1$ $x < -5/3, x > 1$	M1 A1 A1	[3]	Attempt at factorisation Both required Ignore any words between answers Condone < >
	(ii) $f(x) = x^3 + x^2 - 5x + c$ $3 = 1 + 1 - 5 + c$ $f(x) = x^3 + x^2 - 5x + 6$	M1 A1 M1 A1		
7	(i) Range is $0 < f(x) < 4$, 0 to 4	B1	[1]	Accept in two parts. Condone <
	(ii) $y = x$ drawn or implied Correct sketch of f^{-1}	B1 B1	[2]	SC if f missing, (2, 2) (4, 6) must be shown
	(iii) $(x \mapsto) \sqrt{2x}$ for $0 < x < 2$ $(x \mapsto) 2x - 2$ for $2 < x < 4$	B1B1 B1B1	[4]	Condone < <
8	(i) $1/2 \times 5^2 \times 1.2$ $1/2 \times 5^2 \times \sin 1.2$ $2[1/2 \times 5^2 \times 1.2 - 1/2 \times 5^2 \times \sin 1.2]$ 6.70	B1 B1 M1 A1	[4]	Subtraction and multiplication by 2 Accept 6.7 or anything rounding to 6.70
	(ii) $5 \cos 0.6$ $5 - "5 \cos 0.6"$ $10(1 - \cos 0.6)$ 1.75	M1 M1 M1 A1	[4]	Subtraction from 5 Multiplication by 2
9	(a) $\frac{100}{1-r} = 2000$ $r = 19/20$ $ar = 95$	M1 A1 A1 $\sqrt{\quad}$	[3]	Correct formula and attempt to solve For $100 \times r$
	(b) (i) $a + 2d = 90, a + 4d = 80$ $d = -5, a = 100$	B1B1	[2]	
	(ii) $a + md = 0$ $m = 20$	M1 A1	[2]	Or use correct sum formula $m = 20$ with no working scores 2
	(iii) $\frac{n}{2}[200 + (n-1)(-5)] = 0$ $n = 41$	M1 A1	[2]	$n = 41$ with no working scores 2 Do not penalise $n = 0$

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10	<p>(i) $\overrightarrow{OA} \cdot \overrightarrow{OB} = -6 + 2 + 12 = 8$</p> $\cos AOB = \frac{8}{\sqrt{14}\sqrt{29}}$ $AOB = 66.6^\circ$ <p>(ii) $3\mathbf{i} - 2\mathbf{j} + 4\mathbf{k} + p(2\mathbf{i} + \mathbf{j} - 3\mathbf{k})$</p> <p>(iii) $\overrightarrow{BC} = \mathbf{i}(3 + 2p) + \mathbf{j}(-2 + p) + \mathbf{k}(4 - 3p)$ Their $\overrightarrow{BC} \cdot [2\mathbf{i} + \mathbf{j} - 3\mathbf{k}] = 0$ $2(3 + 2p) + (p - 2) - 3(4 - 3p) = 0$ $p = 4/7 \quad 0.571$</p>	M1 M1 M1 A1 B1 M1 M1 A1√ A1	 [4] [1] [4]	Use of $x_1x_2 + y_1y_2 + z_1z_2$ Mod worked correctly for either one Division of "8" by product of mods In any unsimplified form Scalar product = 0 used ft from their BC cao
11	<p>(i) $9 - x^3 = \frac{8}{x^3}$</p> $x^6 - 9x^3 + 8 = 0$ $(X - 1)(X - 8) = 0 \rightarrow X = 1 \text{ or } 8$ $a = 1, b = 2$ <p>(ii) $\int_1^2 \left[(9 - x^3) - \frac{8}{x^3} \right] dx$</p> $\left[9x - \frac{x^4}{4} \right] \cdot \left[\frac{-4}{x^2} \right]$ $18 - 4 + 1 - \left(9 - \frac{1}{4} + 4 \right)$ $2 \frac{1}{4}$ <p>(iii) $\frac{dy}{dx} = \frac{-24}{x^4}, \frac{dy}{dx} = -3x^2$</p> $\frac{-24}{c^4} = -3c^2$ $c^6 = 8$ $c = \sqrt{2} \text{ or } 8^{1/6} \text{ or } 1.41(4\dots)$	M1 A1 M1 A1 M1 B1 B1 M1 A1 B1, B1 M1 A1	 [4] [5] [4]	Together with attempt to mult by x^3 AG completely correct working Attempt to solve quadratic in X or x^3 Intention to integrate the difference $y_1 - y_2$ not $\pi(y_1 - y_2)$ Correct use of their limits once cao Equating and solution Accept x or c