

Question	Answer	Marks
1	State or imply non-modular inequality $(2x - 1)^2 > 3^2(x + 2)^2$ , or corresponding quadratic equation, or pair of linear equations	<b>B1</b>
	Make reasonable attempt at solving a 3-term quadratic, or solve two linear equations for $x$	<b>M1</b>
	Obtain critical values $x = -7$ and $x = -1$	<b>A1</b>
	State final answer $-7 < x < -1$	<b>A1</b>
<b>Alternative method for question 1</b>		
	Obtain critical value $x = -1$ from a graphical method, or by solving a linear equation or linear inequality	<b>B1</b>
	Obtain critical value $x = -7$ similarly	<b>B2</b>
	State final answer $-7 < x < -1$ [Do not condone $\leq$ for $<$ in the final answer.]	<b>B1</b>
		<b>4</b>

Question	Answer	Marks
2	Commence integration and reach $a(2-x)e^{-2x} + b \int e^{-2x} dx$ , or equivalent	<b>M1*</b>
	Obtain $-\frac{1}{2}(2-x)e^{-2x} - \frac{1}{2} \int e^{-2x} dx$ , or equivalent	<b>A1</b>
	Complete integration and obtain $-\frac{1}{2}(2-x)e^{-2x} + \frac{1}{4}e^{-2x}$ , or equivalent	<b>A1</b>
	Use limits correctly, having integrated twice	<b>DM1</b>
	Obtain answer $\frac{1}{4}(3 - e^{-2})$ , or exact equivalent	<b>A1</b>
		<b>5</b>

Question	Answer	Marks
3(a)	Remove logarithms correctly and state $1 + e^{-x} = e^{-2x}$ , or equivalent	<b>B1</b>
	Show equation is $u^2 + u - 1 = 0$ , where $u = e^x$ , or equivalent	<b>B1</b>
		<b>2</b>
3(b)	Solve a 3-term quadratic for $u$	<b>M1</b>
	Obtain root $\frac{1}{2}(-1 + \sqrt{5})$ , or decimal in $[0.61, 0.62]$	<b>A1</b>
	Use correct method for finding $x$ from a positive root	<b>M1</b>
	Obtain answer $x = -0.481$ only	<b>A1</b>
		<b>4</b>

Question	Answer	Marks
4(a)	Use the product rule	<b>M1</b>
	State or imply derivative of $\tan^{-1}\left(\frac{1}{2}x\right)$ is of the form $k/(4 + x^2)$ , where $k = 2$ or $4$ , or equivalent	<b>M1</b>
	Obtain correct derivative in any form, e.g. $\tan^{-1}\left(\frac{1}{2}x\right) + \frac{2x}{x^2 + 4}$ , or equivalent	<b>A1</b>
		<b>3</b>
4(b)	State or imply $y$ -coordinate is $\frac{1}{2}\pi$	<b>B1</b>
	Carry out a complete method for finding $p$ , e.g. by obtaining the equation of the tangent and setting $x = 0$ , or by equating the gradient at $x = 2$ to $\frac{\frac{1}{2}\pi - p}{2}$	<b>M1</b>
	Obtain answer $p = -1$	<b>A1</b>
		<b>3</b>

Question	Answer	Marks
5	Use $\tan 2A$ formula to express RHS in terms of $\tan \theta$	M1
	Use $\tan (A \pm B)$ formula to express LHS in terms of $\tan \theta$	M1
	Using $\tan 45^\circ = 1$ , obtain a correct horizontal equation in any form	A1
	Reduce equation to $2 \tan^2 \theta + \tan \theta - 1 = 0$	A1
	Solve a 3-term quadratic and find a value of $\theta$	M1
	Obtain answer $\theta = 26.6^\circ$ and no other	A1
		6

Question	Answer	Marks
6(a)	Sketch a relevant graph, e.g. $y = x^5$	B1
	Sketch a second relevant graph, e.g. $y = x + 2$ and justify the given statement	B1
		2
6(b)	State a suitable equation, e.g. $x = \frac{4x^5 + 2}{5x^4 - 1}$	B1
	Rearrange this as $x^5 = 2 + x$ or commence working <i>vice versa</i>	B1
		2
6(c)	Use the iterative formula correctly at least once	M1
	Obtain final answer 1.267	A1
	Show sufficient iterations to 5 d.p. to justify 1.267 to 3 d.p., or show there is a sign change in the interval (1.2665, 1.2675)	A1
		3

Question	Answer	Marks
7(a)	State or imply the form $\frac{A}{2x-1} + \frac{B}{2x+1}$ and use a relevant method to find $A$ or $B$	<b>M1</b>
	Obtain $A = 1, B = -1$	<b>A1</b>
		<b>2</b>
7(b)	Square the result of part (a) and substitute the fractions of part (a)	<b>M1</b>
	Obtain the given answer correctly	<b>A1</b>
		<b>2</b>
7(c)	Integrate and obtain $-\frac{1}{2(2x-1)} - \frac{1}{2}\ln(2x-1) + \frac{1}{2}\ln(2x+1) - \frac{1}{2(2x+1)}$ , or equivalent	<b>B3, 2, 1, 0</b>
	Substitute limits correctly	<b>M1</b>
	Obtain the given answer correctly	<b>A1</b>
		<b>5</b>

Question	Answer	Marks	
8(a)	State or imply $\overline{AB}$ or $\overline{AD}$ in component form	<b>B1</b>	
	Use a correct method for finding the position vector of $C$	<b>M1</b>	
	Obtain answer $4\mathbf{i} + 3\mathbf{j} + 4\mathbf{k}$ , or equivalent	<b>A1</b>	
	Using the correct process for the moduli, compare lengths of a pair of adjacent sides, e.g. $AB$ and $AD$	<b>M1</b>	
	Show that $ABCD$ has a pair of unequal adjacent sides	<b>A1</b>	
	<b>Alternative method for question 8(a)</b>		
	State or imply $\overline{AB}$ or $\overline{AD}$ in component form	<b>B1</b>	
	Use a correct method for finding the position vector of $C$	<b>M1</b>	
	Obtain answer $4\mathbf{i} + 3\mathbf{j} + 4\mathbf{k}$ , or equivalent	<b>A1</b>	
	Use the correct process to calculate the scalar product of $\overline{AC}$ and $\overline{BD}$ , or equivalent	<b>M1</b>	
	Show that the diagonals of $ABCD$ are not perpendicular	<b>A1</b>	
		<b>5</b>	
	8(b)	Use the correct process to calculate the scalar product of a pair of relevant vectors, e.g. $\overline{AB}$ and $\overline{AD}$	<b>M1</b>
Using the correct process for the moduli, divide the scalar product by the product of the moduli of the two vectors and evaluate the inverse cosine of the result		<b>M1</b>	
Obtain answer $100.3^\circ$		<b>A1</b>	
		<b>3</b>	



Question	Answer	Marks
8(c)	Use a correct method to calculate the area, e.g. calculate $AB \cdot AC \sin \angle BAD$	<b>M1</b>
	Obtain answer 11.0 ( <b>FT</b> on angle BAD)	<b>A1 FT</b>
		<b>2</b>

Question	Answer	Marks
9(a)	Eliminate $u$ or $w$ and obtain an equation $w$ or $u$	<b>M1</b>
	Obtain a quadratic in $u$ or $w$ , e.g. $u^2 - 2iu - 6 = 0$ or $w^2 + 2iw - 6 = 0$	<b>A1</b>
	Solve a 3-term quadratic for $u$ or for $w$	<b>M1</b>
	Obtain answer $u = \sqrt{5} + i$ , $w = \sqrt{5} - i$	<b>A1</b>
	Obtain answer $u = -\sqrt{5} + i$ , $w = -\sqrt{5} - i$	<b>A1</b>
		<b>5</b>
9(b)	Show the point representing $2 + 2i$	<b>B1</b>
	Show a circle with centre $2 + 2i$ and radius 2 ( <b>FT</b> is on the position of $2 + 2i$ )	<b>B1 FT</b>
	Show half-line from origin at $45^\circ$ to the positive $x$ -axis	<b>B1</b>
	Show line for $\operatorname{Re} z = 3$	<b>B1</b>
	Shade the correct region	<b>B1</b>
		<b>5</b>

Question	Answer	Marks
10(a)	State or imply $\frac{dV}{dt} = -k\sqrt{h}$	B1
	State or imply $\frac{dV}{dh} = 2\pi rh - \pi h^2$ , or equivalent	B1
	Use $\frac{dV}{dt} = \frac{dV}{dh} \cdot \frac{dh}{dt}$	M1
	Obtain the <b>given answer</b> correctly	A1
		4
10(b)	Separate variables and attempt integration of at least one side	M1
	Obtain terms $\frac{4}{3}rh^{\frac{3}{2}} - \frac{2}{5}h^{\frac{5}{2}}$ and $-Bt$	A3, 2, 1, 0
	Use $t = 0, h = r$ to find a constant of integration $c$	M1
	Use $t = 14, h = 0$ to find $B$	M1
	Obtain correct $c$ and $B$ , e.g. $c = \frac{14}{15}r^{\frac{5}{2}}, B = \frac{1}{15}r^{\frac{5}{2}}$	A1
	Obtain final answer $t = 14 - 20\left(\frac{h}{r}\right)^{\frac{3}{2}} + 6\left(\frac{h}{r}\right)^{\frac{5}{2}}$ , or equivalent	A1
		8