

Question	Answer	Marks	Guidance
1	$0.6 \pm z \sqrt{\frac{0.4 \times 0.6}{100}}$	M1	Recognisable value of z
	$z = 2.326$	B1	2.326 to 2.329
	0.486 to 0.714 (3 sf)	A1	Must be an interval
		3	

Question	Answer	Marks	Guidance
2	$\frac{50}{49} \left(\frac{4361}{50} - \bar{x}^2 \right) = 9.62$	M1	or $\left(\frac{4361}{49} - \frac{(\Sigma x)^2}{50 \times 49} \right) = 9.62$ BOD regarding symbols used
	$\bar{x}^2 = \frac{4361}{50} - 9.62 \times \frac{49}{50} = 77.7924$	A1	$(\Sigma x)^2 = 4361 \times 50 - 9.62 \times 50 \times 49 = 194481$ or $\Sigma x = 441$ (Σx) or (\bar{x}) must be correctly identified
	$\bar{x} = 8.82$ (3 sf)	A1	SC use of 'biased' leading to 8.81 B1
		3	

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3(i)	<i>D</i> more likely to be chosen	B1	oe, e.g. $P(D) > P(A)$ e.g. $P(A)=P(B)=P(C)=1/6$ $P(D)=1/2$ no contradictions
		1	
3(ii)	Reject scores of 5 or 6	B1	or other correct: choose <i>D</i> when the score is 4
		1	

Question	Answer	Marks	Guidance
3(iii)	AB AC AD BC BD CD	B1	
	Allocate as follows: 1: AB; 2: AC; 3: AD; 4: BC; 5: BD 6: CD	B1	or similar
		2	

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4	Total $\sim N(1208, \dots)$	B1	
	Var(total) ($= 10 \times 1.2 + 20 \times 0.7 (+ 0)$) = 26	B1	May be implied by next line
	$\pm \frac{1200 - "1208"}{\sqrt{"26"}} \quad (= -1.569)$	M1	FT their mean and var of total mass, e.g. allow 1200 and 11.24 (from $10 \times 1.2^2 + 20 \times 0.7^2$)
	$1 - \Phi("1.569")$	M1	Correct area consistent with their working
	= 0.0583 (3 sf)	A1	
		5	

Question	Answer	Marks	Guidance
5	H ₀ : Pop mean = 20 H ₁ : Pop mean ≠ 20	B1	Accept μ
	$\frac{\Sigma x}{6}$ (= $\frac{126.9}{6}$ = 21.15)	M1	Attempted or 126.9 and 11.64 attempted
	$\frac{'21.15'-20}{\sqrt{\frac{1.94}{6}}}$	M1	Must have $\sqrt{6}$ or $\frac{120-126.9}{\sqrt{11.64}}$ no mixed method
	= 2.022	A1	
	$2(1 - \phi('2.022')) = 2(1 - '0.9784') = 0.0432$	M1	FT $2 \times (1 - '.9784')$
	$\alpha = 4.32$ (3 sf)	A1	FT Allow 4.3 or 4, if correct working seen, or clearly implied, as far as 0.0216 FT their z, no error seen One-tail test scores maximum 3/6
		6	

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6(i)	$\frac{3}{a^3} \int_0^a x^2 dx$ $\left(= \frac{3}{a^3} \left[\frac{x^3}{3} \right]_0^a \right)$	M1	Attempt to integrate f(x) with limits 0 and a (condone missing $\frac{3}{a^3}$)
	$= \frac{3a^3}{3a^3}$	A1	$\frac{3a^3}{3a^3} - 0$ or better seen
	= 1 Hence f is pdf for all a	A1	Answer = 1 and comment
		3	
6(ii)	$\frac{3}{a^3} \int_0^2 x^2 dx = 0.5$ $\frac{3}{a^3} \left[\frac{x^3}{3} \right]_0^2 = 0.5$	M1	Attempt to integrate f(x)=0.5, limits 0 and 2 oe, condone missing $\frac{3}{a^3}$
	$\frac{3}{a^3} \times \frac{8}{3} = 0.5 \text{ oe}$	A1	$\frac{2^3}{3} - 0$ or better, condone missing $\frac{3}{a^3}$
	$a^3 = 16 \text{ or } a = \sqrt[3]{16}$ $\left(= 2.52 \text{ AG} \right)$	A1	Convincingly obtained Note: Attempt to verify 2.52, M1 as stated except not equated to 0.5. A1 as stated, A1 for evaluation to 0.499..apprx 0.5
		3	

Question	Answer	Marks	Guidance
6(iii)	$\frac{3}{16} \int_0^{2.52} x^3 dx$ $= \frac{3}{16} \left[\frac{x^4}{4} \right]_0^{2.52}$	M1	Attempt integ $xf(x)$, correct limits, condone missing $\frac{3}{a^3}$
	$\text{or } \frac{3}{16} \int_0^a x^3 dx$ $\text{or } \frac{3}{16} \left[\frac{x^4}{4} \right]_0^a$		
	$= \frac{3}{16} \times \frac{40.317}{4}$	A1	$\frac{2.52^4}{4} - 0$ or better, condone missing $\frac{3}{a^3}$
	$= 1.89 \text{ (3 sf)}$	A1	
		3	

Question	Answer	Marks	Guidance
7(i)	Use of Po(2.8)	M1	May be implied
	$1 - e^{-2.8} \left(1 + 2.8 + \frac{2.8^2}{2} \right)$	M1	Any λ allowing one end error
	$= 0.531 \text{ or } 0.53(0) \text{ (3 sf)}$	A1	SC Binomial 0.534 B1
		3	
7(ii)	Use of Po(5.8)	M1	May be implied
	$e^{-5.8} \times \frac{5.8^6}{6!}$	M1	Any λ
	$= 0.16(0) \text{ (3 sf)}$	A1	
		3	

Question	Answer	Marks	Guidance
7(iii)	Use of N(58, 58)	M1	May be implied or N(58, 55.38)
	$\frac{50.5 - '58'}{\sqrt{'58'}} (= -0.985)$	M1	Standardised with their values, allow wrong or incorrect cc
	$\Phi('0.985')$	M1	Correct area consistent with their working or $\Phi('1.008)$
	= 0.838 (3 sf)	A1	or 0.843
		4	

Question	Answer	Marks	Guidance
8(i)	$H_0: p = \frac{1}{4}$ $H_1: p > \frac{1}{4}$	B1	
	${}^{10}C_6 \left(\frac{1}{4}\right)^6 \left(\frac{3}{4}\right)^4 + {}^{10}C_7 \left(\frac{1}{4}\right)^7 \left(\frac{3}{4}\right)^3 + {}^{10}C_8 \left(\frac{1}{4}\right)^8 \left(\frac{3}{4}\right)^2 +$ $10 \left(\frac{1}{4}\right)^9 \left(\frac{3}{4}\right) + \left(\frac{1}{4}\right)^{10}$	M1	Correct terms, allow one term incorrect or omitted or extra or summing all correct terms from 0 to 5 allow one term incorrect or omitted or extra
	= 0.0197	A1	or 0.9803
	comp '0.0197' with 0.01	M1	Valid comparison with 0.01 or valid comparison with 0.99
	No evidence to conclude $p > \frac{1}{4}$	A1	FT No contradictions Use of two-tail test can score BOM1A1M1(comparison with 0.005) A0
		5	
8(ii)	${}^{10}C_7 \left(\frac{1}{4}\right)^7 \left(\frac{3}{4}\right)^3 + {}^{10}C_8 \left(\frac{1}{4}\right)^8 \left(\frac{3}{4}\right)^2 + 10 \left(\frac{1}{4}\right)^9 \left(\frac{3}{4}\right) + \left(\frac{1}{4}\right)^{10}$	M1	Their $P(X \geq 6) - {}^{10}C_6 (0.25)^6 (0.75)^4$
	P(Type I) = 0.00351 (3 sf)	A1	Accept 0.00348 to 0.00351
		2	
8(iii)	C.R is $X \geq 7$ $P(\text{Type II}) = 1 - P(X \geq 7 p = \frac{3}{5}) =$	M1	May be implied
	$1 - ({}^{10}C_7 \left(\frac{3}{5}\right)^7 \left(\frac{2}{5}\right)^3 + {}^{10}C_8 \left(\frac{3}{5}\right)^8 \left(\frac{2}{5}\right)^2 + 10 \left(\frac{3}{5}\right)^9 \left(\frac{2}{5}\right) + \left(\frac{3}{5}\right)^{10})$	M1	Accept $1 - P(X \geq 8 p = \frac{3}{5})$ or $1 - P(X \geq 6 p = \frac{3}{5})$
	= 0.618	A1	
		3	