

Question	Answer	Marks	Guidance
1(i)	0.0842 (3 sf)	<b>B1</b>	
		<b>1</b>	
1(ii)	$e^{-5} \times \frac{5^n}{n!} = e^{-5} \times \frac{5^{n+1}}{(n+1)!}$	<b>B1</b>	or $\frac{5^n}{n!} = \frac{5^{n+1}}{(n+1)!}$ or better ISW
		<b>1</b>	
1(iii)	$1 = \frac{5}{n+1}$  $n = 4$	<b>B1</b>	
		<b>1</b>	

Question	Answer	Marks	Guidance
2(i)	Normal with mean 372	<b>B1</b>	
		<b>M1</b>	or variance = $\frac{54^2}{36}$ M1
		<b>A1</b>	(= 81) A1
		<b>3</b>	
2(ii)	Pop normal	<b>B1</b>	Allow $X$ is normal
		<b>1</b>	

Question	Answer	Marks	Guidance
3(i)	Est( $\mu$ ) = 1.85	<b>B1</b>	
	Est( $\sigma^2$ ) = $\frac{50}{49} \left( \frac{175.25}{50} - '1.85'^2 \right)$	<b>M1</b>	Allow $\sqrt{\frac{50}{49} \left( \frac{175.25}{150} - '1.85'^2 \right)}$ or 0.0290 for M1
	= 0.0842 (3 sf) or $\frac{33}{392}$	<b>A1</b>	Cao If $\frac{50}{49}$ omitted (giving var = 0.0825 or sd = 0.287) M0A0
		<b>3</b>	
3(ii)	H <sub>0</sub> : Pop mean time = 1.9 (h) H <sub>1</sub> : Pop mean time < 1.9 (h)	<b>B1</b>	Allow ' $\mu$ ' but not just 'mean'
	$\pm \frac{1.85 - 1.9}{\sqrt{\frac{0.0842}{50}}}$	<b>M1</b>	$\pm \frac{1.85 - 1.9}{\frac{0.290}{\sqrt{50}}}$ Accept totals method (92.5–95) / $\sqrt{4.21}$
	= -1.22	<b>A1</b>	= -1.22
	comp $z = -1.645$	<b>M1</b>	Or other valid comparison 0.888 or 0.889 < 0.95 OR 0.111 or 0.112 > 0.05
	No evidence that mean time < 1.9 h	<b>A1</b>	<b>FT</b> their z. Correct conclusion. No contradictions If $\frac{50}{49}$ not used in (1): var = 0.8225, sd = 0.907, cr = 1.17 can score all marks in (ii) Note- 2 tail test can score B0 M1 A1 M1 (comparison with 1.96) A0 (no ft) max3/5
		<b>5</b>	

Question	Answer	Marks	Guidance
4	Use of $1.5X_1 - X_2$ or similar	<b>B1</b>	
	$E(1.5X_1 - X_2) = 1.5(110) - 110 (= 55)$	<b>B1</b>	or $E(X_1 - 1.5X_2) = 110 - 1.5(110) (= -55)$
	$\text{Var}(1.5X_1 - X_2) = 1.5^2 \times 1050 + 1050$ (or 3412.5)	<b>M1</b>	Correct expression or result
	$\frac{0-55}{\sqrt{3412.5}}$ or $\frac{0-(-55)}{\sqrt{3412.5}}$ ( $= \pm 0.942$ )	<b>M1</b>	Their '55'. Allow incorrect var (dep > 0 and $\neq 1050$ )
	$1 - \Phi('0.942')$	<b>M1</b>	Area consistent with their working
	$= 0.173$	<b>A1</b>	
	Ans 0.346 (3 sf)	<b>B1</b>	<b>FT</b> double their prob (must be <1)
		<b>7</b>	

Question	Answer	Marks	Guidance
5(i)	$H_0: p = 0.1$ $H_1: p < 0.1$	<b>B1</b>	
		<b>1</b>	
5(ii)	B(40, 0.1) stated or implied by use of	<b>B1</b>	e.g. by ${}^{40}C_x$ or $0.9^p \times 0.1^q$ ( $p + q = 40$ )
	$0.9^{40} + 40 \times 0.9^{39} \times 0.1$	<b>M1</b>	Correct working (if seen). If working not seen, M1 may be implied by 0.0805
	$= 0.0805$	<b>A1</b>	
		<b>3</b>	

Question	Answer	Marks	Guidance
5(iii)	$z = 1.645$	<b>B1</b>	seen
	$\frac{6}{80} \pm z \sqrt{\frac{\frac{6 \times (80-6)}{80}}{80}}$	<b>M1</b>	Formula of correct form. Must be a 'z'
	= 0.0266 to 0.123 (3 sfs)	<b>A1</b>	Allow 0.03 to 0.12 or better Must be an interval
		<b>3</b>	
5(iv)	10% (or manufacturer's claim) is within CI Hence no reason to question claim	<b>B1</b>	<b>FT</b> Allow '10% is within CI, accept claim' oe Must include both parts. No contradictions. <b>FT</b> their CI Note if CI is centred on 0.1 allow ft 0.075 is within CI, accept claim
		<b>1</b>	

Question	Answer	Marks	Guidance
6(i)	$a \int_1^b \frac{1}{x^2} dx = 1$	<b>M1</b>	Attempt int f(x) and = 1, ignore limits
	$a \left[ -\frac{1}{x} \right]_1^b = 1$	<b>A1</b>	correct integ and limits = 1
	$a \left[ 1 - \frac{1}{b} \right] = 1$ or $a \times \frac{b-1}{b} = 1$ $b = \frac{a}{a-1}$ <b>AG</b>	<b>A1</b>	No errors seen
		<b>3</b>	

Question	Answer	Marks	Guidance
6(ii)	$a \int_1^{\frac{3}{2}} \frac{1}{x^2} dx = \frac{1}{2}$ $a \left[ -\frac{1}{x} \right]_1^{\frac{3}{2}} = \frac{1}{2}$	<b>M1</b>	Attempt int f(x) with limits 1 to $\frac{3}{2}$ and $= \frac{1}{2}$
	$a \left[ 1 - \frac{2}{3} \right] = \frac{1}{2}$	<b>A1</b>	oe correct equn in a
	$a = \frac{3}{2}, b = 3$	<b>A1</b>	Both
		<b>3</b>	
6(iii)	$\frac{3}{2} \int_1^3 \frac{1}{x} dx$	<b>M1</b>	Attempt int xf(x), ignore limits – condone missing a
	$= \frac{3}{2} [\ln x]_1^3$	<b>A1</b>	<b>FT</b> Correct integ and <i>their</i> limits 1 to b – condone missing a
	$= \frac{3}{2} \ln 3$ or 1.65 (3 sf)	<b>A1</b>	<b>FT</b> <i>their</i> a and b (valid b i.e. >1)
		<b>3</b>	

Question	Answer	Marks	Guidance
7(i)	Max no. of passengers plane can take oe	<b>B1</b>	oe e.g. No of passengers who bought tickets
		<b>1</b>	

Question	Answer	Marks	Guidance
7(ii)	$\lambda = 3.2$	<b>B1</b>	
	$e^{-3.2} \left( \frac{3.2^3}{3!} + \frac{3.2^4}{4!} + \frac{3.2^5}{5!} \right)$	<b>M1</b>	Any $\lambda$ . Allow one end error
	$= 0.5146 = 0.515$ (3 sfs)	<b>A1</b>	SR Use of Bin(640,0.005) scores B1 (only) for 0.516
		<b>3</b>	
7(iii)	$n > 50$	<b>B1</b>	Accept n is large
	$np = 1.6$ , which is $< 5$ or $p=0.005$ which is $< 0.1$	<b>B1</b>	Allow $np = 3.2$
		<b>2</b>	
7(iv)	$H_0$ : Pop mean (for 5 days) = 8 $H_1$ : Pop mean (for 5 days) $< 8$	<b>B1</b>	or Pop mean (for 1 day) = 1.6 Pop mean (for 1 day) $< 1.6$ Allow $\lambda$ or $\mu$ but not just 'mean'
	$e^{-8} \left( 1 + 8 + \frac{8^2}{2!} \right)$	<b>M1</b>	Any $\lambda$ ( $\neq 1.6$ ) No end errors. Accept use of Bin(1600,0.005) $P(0,1,2)=0.0136$
	$= 0.0138$	<b>A1</b>	
	Comp 0.025	<b>M1</b>	Valid comparison
	Evidence that mean no. failing to arrive has decreased	<b>A1</b>	<b>FT</b> their '0.0138' or '0.0136'. No contradictions
		<b>5</b>	