| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1(i) | Mean $=115$ | B1 |  |
|  | $\mathrm{SD}=40$ | B1 |  |
|  |  | 2 |  |
| 1(ii) | Mean $=15 \times 115{ }^{\prime}=1725$ | B1ft |  |
|  | $15 \times{ }^{\text {' } 40{ }^{\prime 2}} \quad(=24000)$ | M1 | or SD $=\sqrt{ } 15 \times$ '40'. ft their (i) |
|  | $\begin{aligned} & \mathrm{SD}=\sqrt{ } 24000 \\ & \mathrm{SD}=155 \text { (cents) }(3 \mathrm{sf}) \end{aligned}$ | A1 | Accept $\sqrt{ } 24000$ SC: Allow correct answers in dollars |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2(i) | Assume sd still 4.8 or is unchanged | B1 | or Assume the 150 times can be treated as a random sample / are independent |
|  | $\begin{aligned} & \mathrm{H}_{0}: \text { Pop mean }=26.5 \\ & \mathrm{H}_{1}: \text { Pop mean }>26.5 \end{aligned}$ | B1 | Allow ' $\mu$ ' but not just 'mean' |
|  | $\frac{27.5-26.5}{\frac{4.8}{\sqrt{150}}}$ | M1 | Standardise, with $\sqrt{ }$ Accept CV method |
|  | $=2.552$ | A1 |  |
|  | Comp with $z$-value ' 2.552 ' > 2.326 | M1 | $\begin{aligned} & \text { or comp } 1-\Phi\left({ }^{( } 2.552^{\prime}\right) \text { with } 0.01 \\ & 1-0.9946=0.0054<0.01 \end{aligned}$ |
|  | There is evidence time has increased | A1ft | oe No contradictions <br> ( 2 tail test scores max. B1 B0 M1 A1 M1 (for comparison with 2.576) A0 no ft) |
|  |  | 6 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 2 2(ii) | No because pop is normal so distr of $\bar{X}$ is <br> normal | $\mathbf{B 1}$ | Condone just 'No because pop is normal' |
|  |  | $\mathbf{1}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3(i) | $\begin{aligned} & \mathrm{H}_{0}: \mathrm{P}(6)=\frac{1}{6} \\ & \mathrm{H}_{1}: \mathrm{P}(6)<\frac{1}{6} \end{aligned}$ | B1 |  |
|  | $\left(\frac{5}{6}\right)^{30}+30\left(\frac{1}{6}\right) \times\left(\frac{5}{6}\right)^{29}+{ }^{30} \mathrm{C}_{2}\left(\frac{1}{6}\right)^{2} \times\left(\frac{5}{6}\right)^{28}$ | M1 | Allow one term incorrect, omitted or extra |
|  | $=0.103$ | A1 |  |
|  | ${ }^{\prime} 0.103 '>0.05$ | M1 |  |
|  | No evidence (at 5\% level) that die biased | A1ft | oe No contradictions |
|  |  | 5 |  |
| 3(ii) | $\left(\frac{5}{6}\right)^{30}+30\left(\frac{1}{6}\right) \times\left(\frac{5}{6}\right)^{29}$ | M1 |  |
|  | $\mathrm{P}($ Type I$)=0.0295$ | A1 |  |
|  |  | 2 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(a)(i) | $0.5 \times 1 / \mathrm{a}=\left(\frac{0.5}{a}\right)$ | M1 | Or attempt to integrate $\mathrm{f}(x)(=1 / \mathrm{a})$ between 0 and 0.5 |
|  | $=\frac{1}{2 a}$ oe | A1 | Accept 0.5/a for A1 |
|  |  | 2 |  |
| 4(a)(ii) | $\frac{a}{2}$ | B1 |  |
|  |  | 1 |  |
| 4(a)(iii) | $\int_{0}^{a} \frac{x^{2}}{a} \mathrm{~d} x-\left({ }^{\left(\frac{a}{2}\right.}{ }^{\prime}\right)^{2}$ | M1 | Integ their $x^{2} \mathrm{f}(x)$ from 0 to $a$ and sub their mean ${ }^{2}$ |
|  | $\begin{aligned} & \operatorname{Var}(X)=\frac{a^{2}}{3}-\frac{a^{2}}{4} \\ & \left(\operatorname{Var}(X)=\frac{a^{2}}{12} \quad \mathbf{A G}\right) \end{aligned}$ | A1 | Must see this line oe |
|  |  | 2 |  |
| 4(b) | $\int_{2}^{b} \frac{3}{2(t-1)^{2}} \mathrm{dt}$ | M1 | Attempt integ $\mathrm{g}(t)$ ignore limits |
|  | $\left[-\frac{3}{2(t-1)}\right]_{2}^{b}$ | A1 | Correct integral |
|  | $\begin{aligned} & -\frac{3}{2}\left(\frac{1}{(b-1)}-1\right)=\frac{3}{4} \\ & \left(1-\frac{1}{(b-1)}=\frac{1}{2}\right) \end{aligned}$ | M1 | Attempt subst correct limits in their integ and $=\frac{3}{4}$ |
|  | $b=3$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(a)(i) | $\mathrm{e}^{-2.3}\left(\frac{2.3^{2}}{2}+\frac{2.3^{3}}{3!}+\frac{2.3^{4}}{4!}\right.$ | M1 | Allow one end error |
|  | $=0.585$ | A1 |  |
|  |  | 2 |  |
| 5(a)(ii) | $(\lambda)=4.6$ | B1 |  |
|  | $1-\mathrm{e}^{-4.6}\left(1+4.6+\frac{4.6^{2}}{2}\right)$ | M1 | any $\lambda$, Allow one end error |
|  | $=0.837(3 \mathrm{sf})$ | A1 |  |
|  |  | 3 |  |
| 5(a)(iii) | $S \sim \mathrm{~N}(115,115)$ | B1 | May be implied |
|  | $\frac{110.5-115}{\sqrt{115}} \quad(=-0.420)$ | M1 | Allow with wrong or no cc OR no $V$ |
|  | $1-\Phi\left({ }^{\prime} 0.420\right.$ ' $) \quad(=1-0.663)$ | M1 |  |
|  | $=0.337$ | A1 | Accept alternative method using $\mathrm{N}(2.3,2.3)$ no mixed methods. |
|  |  | 4 |  |
| 5(b) | $\mathrm{e}^{-\lambda} \times \frac{\lambda^{3}}{3!}=\mathrm{e}^{-\lambda} \times \frac{\lambda^{5}}{5!}$ | M1 |  |
|  | $\lambda^{3}=\frac{\lambda^{5}}{4 \times 5}$ or $\lambda^{2}=20$ oe | A1 | any correct simplification without $\mathrm{e}^{-\lambda}$ or ! |
|  | $\lambda=\sqrt{ } 20$ or $2 \sqrt{ } 5$ or $4.47(3 \mathrm{sf})$ | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(i) | Biased towards people who like tennis Excludes people who don't like tennis | B1 | or other sensible |
|  |  | 1 |  |
| 6(ii) | Obtain a list of all people in the town | B1 |  |
|  | Use random numbers | B1 | or, e.g. pick numbers from a hat or other sensible |
|  |  | 2 |  |
| 6(iii) | $\operatorname{Var}(p)=\frac{\frac{47}{350}\left(1-\frac{47}{350}\right)}{350}(=0.000332152)$ | M1 |  |
|  | $z=1.645$ | B1 |  |
|  | $\frac{47}{350} \pm z \sqrt{\frac{\frac{47}{350}\left(1-\frac{47}{350}\right)}{350}}$ | M1 | Must be a $z$ value |
|  | 0.104 to 0.164 (3 sf) | A1 | Must be an interval |
|  |  | 4 |  |
| 6(iv) | $1.25 \times 1.645 \quad(=2.056)$ | M1 | or $1.25 \times$ their width $\div 2 \div$ their $\sqrt{\frac{\frac{47}{350}\left(1-\frac{47}{350}\right)}{350}}$ (Complete method) |
|  | $\Phi\left({ }^{\prime} 2.056\right) \quad(=0.980)$ | M1 | Attempt $\Phi($ their $z$ ) |
|  | $x=96 \quad(2 \mathrm{sf})$ | A1 | Allow 0.96 (2 sf) CWO |
|  |  | 3 |  |

