# Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

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| Question | Answer   | Marks | Guidance  |
|----------|--|-------|---|
| 1        | $P(S) = \frac{1}{2}$   | B1    |   |
|          | $P(T) = \frac{16}{36} \left(\frac{4}{9}\right)$  | B1    |   |
|          | $P(S \cap T) = \frac{10}{36} \left(\frac{5}{18}\right)$  | M1    | $P(S \cap T)$ found by multiplication scores M0<br>M1 awarded if <i>their</i> value is identifiable in their sample space diagram <b>or</b><br>Venn diagram <b>or</b> list of terms <b>or</b> probability distribution table (oe) |
|          | $P(S) P(T) \neq P(S \cap T)$ so not independent  | A1    | 8/36, 10/36 P(S) × P(T) and P( $S \cap T$ ) seen in workings and correct conclusion stated, www   |
|          | Alternative method for question 1  |       |   |
|          | $P(S) = \frac{1}{2}$   | B1    |   |
|          | $P(T) = \frac{16}{36} \left(\frac{4}{9}\right)$  | B1    |   |
|          | $P(S \cap T) = \frac{10}{36} \left(\frac{5}{18}\right)$  | M1    | $P(S \cap T)$ found by multiplication scores M0<br>M1 awarded if <i>their</i> value is identifiable in their sample space diagram <b>or</b><br>Venn diagram <b>or</b> list of terms <b>or</b> probability distribution table (oe) |
|          | $P(S T) = \frac{10}{16} \text{ or } P(T S) = \frac{10}{18}$ $P(S T) \neq P(S) \text{ or } P(T S) \neq P(T) \text{ so not independent}$ | A1    | <b>Either</b> 18/36, 10/16,P(S) and P( $S T$ ) seen in workings and correct conclusion stated, www<br><b>Or</b> 16/36, 10/18, P(T) and P(T S) seen in workings and correct conclusion stated, www                                 |
|          |  | 4     |   |

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| Question | Answer  | Marks | Guidance  |
|----------|---|-------|---|
| 2        | $P(<28.9) = P\left(z < \frac{28.9 - 30}{1.5}\right)$  | B1    | Using ± standardising formula, no continuity correction, not $\sigma^2$ or $\sqrt{\sigma}$ ,  |
|          | = P(z < -0.733) = 1 - 0.7682  | M1    | Appropriate area $\Phi$ from standardisation formula P(z <) in final probability solution,<br>Must be a probability, e.g. 1 – 0.622 is M0 |
|          | = 0.2318  | A1    | Correct final probability rounding to 0.232.<br>(Only requires M1 not B1 to be awarded  |
|          | Number of cartridges is <i>their</i> $0.2318 \times 8$<br>= 1.85, so 2 (Also accept 1 but not both) | B1    | <b>FT</b> using <i>their</i> 4 SF (or better) value, ans. rounded or truncated to integer, no approximation indicated.                    |
|          |   | 4     |   |

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| Question | Answer   | Marks | Guidance  |
|----------|--|-------|---|
| 3(i)     | $P(\text{at most 7}) = 1 - P(8, 9, 10) = 1 - {}^{10}\text{C8}(0.35)^8 (0.65)^2 - {}^{10}\text{C}_9(0.35)^9 (0.65)^1 - (0.35)^{10}$ | M1    | Use of normal approximation M0<br>Binomial term of form ${}^{10}C_x p^x (1-p)^{10-x}$ $0  any p, x \neq 10,0$   |
|          | [= 1 - 0.004281 - 0.0005123 - 0.00002759]  | A1    | Correct unsimplified (or individual terms evaluated) answer seen<br>Condone $1 - A + B + C$ leading to correct solution   |
|          | = 0.995  | B1    | B1 not dependent on previous marks.   |
|          | Alternative method for question 3(i)   |       |   |
|          | P(at most 7) = P(0,1,2,3,4,5,6,7)  | M1    | Binomial term of form ${}^{10}C_x p^x (1-p)^{10-x}$ $0  any p, x \neq 10, 0$  |
|          | $= (0.65)^{10} + {}^{10}\text{C1}(0.35)^1(0.65)^9 + \ldots + {}^{10}\text{C}_7(0.35)^7(0.65)^3$                                    | A1    | Correct unsimplified answer or individual terms evaluated seen  |
|          | = 0.995  | B1    |   |
|          |  | 3     |   |
| 3(ii)    | $ \begin{array}{l} 1 - (0.65)^n > 0.99 \\ 0.01 > (0.65)^n \end{array} $  | M1    | Equation or inequality with $(0.65)^n$ and $0.01$ or $(0.35)^n$ and $0.99$ only (Note $1 - 0.99$ is equivalent to 0.01 etc.)  |
|          | <i>n</i> > 10.69   | M1    | Solving their $a^n = c$ , $0 < a, c < 1$ using logs <b>or</b> Trial and Error<br>If answer inappropriate, at least 2 trials are required for Trial and Error M mark |
|          | smallest $n = 11$  | A1    | САО   |
|          |  | 3     |   |

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| Question | Answer   | Marks | Guidance  |
|----------|--|-------|---|
| 4        | $z = 0.842 = \left(\frac{121 - \mu}{\sigma}\right)$ so $0.842\sigma = 121 - \mu$ | B1    | $\pm$ 0.842 seen but B0 if 1 $\pm$ 0.842 oe seen  |
|          |  | M1    | One appropriate standardisation equation with a <i>z</i> -value, $\mu$ , $\sigma$ and 121 or 102, condone continuity correction. Not 0.158, 0.42,             |
|          | $z = -0.58 = \left(\frac{102 - \mu}{\sigma}\right)$ so $-0.58\sigma = 102 - \mu$ | B1    | $\pm 0.58(0)$ seen but B0 if $1 \pm 0.58$ oe seen   |
|          | Solving  | M1    | Correct algebraic elimination of $\mu$ or $\sigma$ from <i>their</i> two simultaneous equations to form an equation in one variable, condone 1 numerical slip |
|          | $\sigma = 13.4  \mu = 110$   | A1    | If M0A0 scored (i.e. no algebraic elimination seen), <b>SC B1</b> can be awarded for both answers correct   |
|          |  |       | Consistent use of $\sigma^2$ or $\sqrt{\sigma}$ throughout apply <b>MR</b> penalty to A mark or SC B mark.  |
|          |  | 5     |   |

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| Question | Answer   | Marks | Guidance  |
|----------|--|-------|---|
| 5(i)     | 5/9 T  | B1    | First pair of branches labels and probs correct (6/7 and 1/7 or rounding to 0.857 and 0.143)                                  |
|          | Т  |       | (Labelling must be logicallye.g. (T and T) or (T and Not T) would be acceptable)  |
|          | 6/7 4/9 C  | B1    | Either of second top pair or bottom of branches labels and probs correct  |
|          | 1/7 C 6/9 T  |       |   |
|          | 3/9 C  | B1    | Both second pairs of branches labels and probs correct. No additional / further branches.                                     |
|          |  | 3     |   |
| 5(ii)    | No of toffees  | B1    | P(1) correct  |
|          | taken ( $T$ ) 0 1 2  | B1    | P(0) or P(2) correct  |
|          | prob $\begin{vmatrix} \frac{3}{63} \\ 0.0476(2) \end{vmatrix}$ $\begin{vmatrix} \frac{30}{63} \\ 0.476(2) \end{vmatrix}$ $\begin{vmatrix} \frac{30}{63} \\ 0.476(2) \end{vmatrix}$ $\begin{vmatrix} \frac{30}{63} \\ 0.476(2) \end{vmatrix}$ | B1    | <b>FT</b> Correct values in table, any additional values of <i>T</i> have stated probability of zero. For FT $\Sigma p = 1$ , |
|          |  | 3     |   |
| 5(iii)   | $E(X) = \frac{90}{63}  (\frac{10}{7}) \ (1.43)$  | B1    | Not FT  |
|          |  | 1     |   |

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|      |      |      |    |    |

| Question | Answer   | Marks | Guidance   |
|----------|--|-------|--|
| 5(iv)    | 5(iv)<br>$P(1^{st} C   2^{nd} T) = \frac{P(C \cap T)}{P(T)} = \frac{\frac{1}{7} \times \frac{6}{9}}{\frac{1}{7} \times \frac{6}{9} + \frac{6}{7} \times \frac{5}{9}} = \frac{\frac{6}{63}}{\frac{36}{63}}$ | B1    | $P(C \cap T)$ attempt seen as numerator of a fraction, consistent with <i>their</i> tree diagram or correct        |
|          |  | M1    | Summing 2 appropriate two-factor probabilities, consistent with <i>their</i> tree diagram or correct seen anywhere |
|          |  | A1    | $\frac{36}{63}$ oe or correct unsimplifed expression seen as numerator or denominator of a fraction                |
|          | $\frac{1}{6}$ oe   | A1    | Final answer   |
|          |  | 4     |  |

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| Question | Answer   | Marks | Guidance   |
|----------|--|-------|--|
| 6(i)     | Advantage: comment referring to spread or range or shape             | B1    | Comments referring to quartiles, IQR, Range, median, shape, skewness,<br>data distribution, spread score B1<br>Any comments with reference to mean or standard deviation or any other<br>'disadvantage' will score B0<br>Comments referring to '5-value plot', comparison with another data set,<br>overview or ease of drawing/plotting/reading require an appropriate<br>advantage statement.  |
|          | Disadvantage: comment referring to limited data information provided | B1    | Comments referring to no individual data, no information about the<br>number of values, unable to calculate mean, standard deviation, variance<br>and mode score B1<br>Any comments with reference to median, shape or any other 'advantage'<br>will score B0<br>Comments referring to 'size of data set' or 'average' require an<br>appropriate disadvantage statement.<br>Comments referring to outliers are ignored in all cases (as outliers are not<br>in the syllabus content) unless supported by an appropriate advantage /<br>disadvantage statement.<br>If comments not clearly identified, assume first comment is the advantage. |
|          |  | 2     |  |

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| Question  | Answer  | Marks | Guidance  |
|-----------|---|-------|---|
| 6(ii)     | Not mean as data skewed by one large value  | B1    | Comment which identifies 768 (or 'a very large number') as the problem.<br>Condone the use of 'outlier'                                       |
|           | Not mode as frequencies all the same  | B1    | Comment which indicates that no mode exists<br>(e.g. all the data is different, there is no repeated number, all the values are<br>different) |
|           | Median  | B1    | Median identified as choice, dependent upon statements for mean and mode being given, even if incorrect or very general.                      |
|           | SC: Mean is identified as most suitable   |       |   |
|           | Not mode as frequencies all the same  | SCB1  | Comment which indicates that no mode exists   |
|           | Not median as not all values used   | SCB1  | Comment which indicates limitation of median e.g. median is not in middle of range.   |
|           |   | 3     |   |
| 6(iii)(a) | LQ = 256 or 256.5 Med = 280 UQ = 329<br>Min 190 max 375<br>$150 \ 200 \ 250 \ 300 \ 350 \ 400$ time minutes | B1    | Median, UQ and LQ values seen, may not be identified or identified correctly. (Not read from box plot unless value stated)                    |
|           |   | B1    | FT Median and quartiles plotted in box on graph, linear scale   |
|           |   | B1    | Correct end points, whiskers from ends of box but not through box, not at top or bottom of box  |
|           |   | B1    | Uniform scale from 190 to 375 (need at least 3 linear identified points min) and labelled 'time' and 'minutes' (can be in title)              |
|           |   |       | No time axis or time axis with no scale attempt, Max B1B0B0B0   |
|           |   | 4     |   |

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| Question  | Answer   | Marks | Guidance   |
|-----------|--|-------|--|
| 6(iii)(b) | IQR = <i>their</i> 329 – <i>their</i> 256 = 73 or 72.5 | B1    | <b>FT Must</b> follow through only from <i>their</i> stated values (condone if correct quartiles stated here), not reading from graph. |
|           |  | 1     |  |

| Question | Answer  | Marks | Guidance  |
|----------|---|-------|---|
| 7(a)     | ${}^{6}C_{3} \times {}^{3}C_{2} \times {}^{1}C_{1}$   | M1    | ${}^{6}C_{a} \times {}^{6-a}C_{b} \times {}^{6-a-b}C_{6-a-b}$ seen oe ${}^{6-a-b}C_{6-a-b}$ can be implied by 1 or omission, condone use of permutations, |
|          | $=20 \times 3$  | A1    | Any correct method seen no addition/additional scenarios  |
|          | = 60  | A1    | Correct answer  |
|          | Alternative method for question 7(a)  |       |   |
|          | $\frac{{}^{6}P_{6}}{{}^{3}P_{3} \times {}^{2}P_{2} \times {}^{1}P_{1}} = \frac{6!}{3! \times 2!}$ | M1    | ${}^{6}P_{6} / ({}^{n}P_{n} \ge k)$ with $3 \ge n > 1$ and $6 \ge k$ an integer $\ge 1$ , not $6!/1$  |
|          |   | A1    | Correct method with no additional terms   |
|          | = 60  | A1    | Correct answer  |
|          |   | 3     |   |
| 7(b)(i)  | $\frac{4!}{3!} \times \frac{3!}{2!} \times 2$   | M1    | A single expression with either $4!/3! \times k$ or $3!/2! \times k$ , k a positive integer seen oe (condone 2 identical expressions being added)         |
|          |   | M1    | Correctly multiplying <i>their</i> single expression by 2 or 2 identical expressions being added.   |
|          | = 24  | A1    | Correct answer  |
|          |   | 3     |   |

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|----------|---|-------|---|
| 7(b)(ii) | Total no of arrangements = $\frac{7!}{2!3!}$ = 420 (A)    | B1    | Accept unsimplified   |
|          | No with 2s together = $\frac{6!}{3!}$ = 120 (B)           | B1    | Accept unsimplified   |
|          | With 2s not together: <i>their</i> (A) – <i>their</i> (B) | M1    | Subtraction indicated, possibly by <i>their</i> answer, no additional terms present     |
|          | = 300 ways  | A1    | Exact value www   |
|          | Alternative method for question 7(b)(ii)                  |       |   |
|          | 3_7_7_8_  |       |   |
|          | $5! \times \frac{6 \times 5}{2}$                          | B1    | $k \ge 5!$ in numerator, $k$ a positive integer   |
|          | 3! 2  | B1    | $m \ge 3!$ In denominator, $m$ a positive integer                                       |
|          |   | M1    | <i>Their</i> 5!/3! multiplied by <sup>6</sup> C <sub>2</sub> only (no additional terms) |
|          | = 300 ways  | A1    | Exact value www   |
|          |   | 4     |   |