

Question	Answer	Mark	Guidance
1	$(X=) 78 \square 5/13 - 50 \times 3/5 = 78 \cos 67.4 - 50 \cos 53.1$ $(Y=) 78 \square 12/13 \square 50 \times 4/5 - 112$ $= 78 \sin 67.4 \square 50 \sin 53.1 - 112$	M1	Attempt to resolve forces either horizontally (2 terms) or vertically (3 terms)
	$[X = 30 - 30 = 0 \quad Y = 72 + 40 - 112 = 0]$	A1	Correct expressions horizontally and vertically
	$X = 0$ and $Y = 0$	A1	From convincing exact calculations
	Alternative method for question 1		
	$\frac{112}{\sin 59.5} \square \frac{50}{\sin 157.4} \square \frac{78}{\sin 143.1}$	M1	Attempt to use Lami, one pair of terms
		A1	All terms correct
	$\frac{112}{56/65} \square \frac{50}{5/13} \square \frac{78}{3/5} \square 130$	A1	Exact values seen and used and shown to be = 130 $\cos [180 - (\theta + \alpha)] = 33/65$ and $\sin [180 - (\theta + \alpha)] = 56/65$
	3		

Question	Answer	Mark	Guidance
2(i)	$[0 = 25 - 10t]$	M1	Use of $v = u \square at$ with $u = 25$, $v = 0$ and $a = -g$ or other complete method for finding t to highest point
	$t = 2.5$	A1	
		3	

Question	Answer	Mark	Guidance
2(ii)	$[20 = 25t - \frac{1}{2}gt^2]$	M1	Applying $s = ut + \frac{1}{2}at^2$ with $s = 20$, $u = 25$
	$[t = 1 \text{ and } t = 4]$	M1	Solve a 3-term quadratic for t , factorising or formula
	Required time = $4 - 1 = 3$ seconds	A1	
	Alternative method for question 2(ii)		
	$[v^2 = 25^2 - 2 \times (-10) \times 20 \rightarrow v = 15]$	M1	Using $v^2 = u^2 + 2as$ with $u = 25$, $s = 20$ and $a = -g$
	$[-15 = 15 - 10T]$ or equivalent	M1	Use v at $s = 20$ to find the time, T , taken to reach the maximum height and to return to $s = 20$
	Required time = $1.5 + 1.5 = 3$ seconds	A1	
		3	
2(iii)	Max height reached at 2.5 s, hence reaches h after 2 s $h - 3 = 25 \times 2 - 5 \times 2^2$	M1	Using their t from 2(i) – 0.5 in $s = ut + \frac{1}{2}at^2$ Allow finding h without taking note of the additional 3 m
	$h = 33$ m	A1	
	Alternative method for question 2(iii)		
	Maximum height = $\frac{1}{2} \times (25 + 0) \times 2.5 [= 31.25]$ o.e. In 0.5 s it falls distance $\frac{1}{2} \times 10 \times 0.5^2 [= 1.25]$	M1	For attempting to find both the maximum height and the distance fallen in 0.5 seconds
	$h = 31.25 - 1.25 = 30$ m	A1	
		2	

Question	Answer	Mark	Guidance
3(i)	$DF = 1500 \square 12\,000 \square g \square 0.08$ [DF = 11100]	M1	Using $DF = \text{Resistance} \square \text{weight component}$ (3 terms)
	Power = DF \square 5	M1	Using $P = Fv$ (their 2 term DF \square 5)
	Power = 11 100 \square 5 = 55.5 kW	A1	AG
		3	
3(ii)	$k \square 5^2 = 1500, k = 60$	B1	AG
		1	
3(iii)	$DF = 60v^2$	B1	Using $DF = \text{resistance} = 60v^2$
	$55500 = DF \square v = 60v^2 \square v = 60v^3$	M1	$P = Fv$ used and attempt to solve a 2-term cubic equation for v
	$v = 9.74 \text{ ms}^{-1}$	A1	
		3	

Question	Answer	Mark	Guidance
4(i)	$R = 13 \cos 67.4 = 13 (5/13)$ [R = 5]	B1	Resolve forces perpendicular to plane. Allow 67.4 used
	$F \square 13 \sin 67.4 = F + 13(12/13) = 20$ [F = 8]	B1	Resolve forces parallel to plane. Allow 67.4 used
		M1	Use $F = \mu R$
	$\mu = 8/5 = 1.6$	A1	AG Must be from exact working here
		4	

Question	Answer	Mark	Guidance
4(ii)	$13 \sin 67.4 - F = 1.3a$ $F = \mu R = 8 \rightarrow [4 = 1.3a]$	M1	For applying Newton's second law along the plane and also using $F = \mu R$ (3 terms)
	$a = 3.08 \text{ ms}^{-2}$	A1	Allow $a = 40/13$
		2	
4(iii)	$s = 0 + 0.5 + (40/13) + 2^2 [= 80/13 = 6.15]$	M1	Use $s = ut + \frac{1}{2}at^2$ with $u = 0$ and their $a \neq \pm g$ to find the distance moved in the first 2 seconds
	WD = 8 + 6.15	M1	WD = $F + d$
	WD = 49.2 J	A1	Allow WD = 640/13 J
	Alternative method for question 4(iii)		
	$s = 0 + 0.5 + (40/13) + 2^2 [= 80/13 = 6.15]$	M1	
	$[v = (40/13) \times 2]$ and $[WD = 1.3g(80/13)(12/13) - \frac{1}{2} + 1.3 + (80/13)^2]$	M1	Finding v after 2 seconds and using WD = PE loss – KE gain
	WD = 49.2 J	A1	Allow WD = 640/13 J
	3		

Question	Answer	Mark	Guidance
5(i)	$a = 2t - 8$	M1	Differentiate to find a
	$a = 0 \rightarrow t = 4$	M1	Set $a = 0$ and solve for t
	Minimum $v = -4 \text{ ms}^{-1}$	A1	Full marks available for correct use of a v - t graph or correct use of " $t = -b/2a$ "
	Alternative method for question 5(i)		
	$v = (t - 4)^2 - 4$	M1	Attempt to complete the square for v
	$[t = 4]$	M1	Choose the t value which gives minimum v
	Minimum $v = -4 \text{ ms}^{-1}$	A1	
		3	
5(ii)	$v = 0$ when $(t - 2)(t - 6) = 0$	M1	Find values of t when $v = 0$, factorise or formula
	$t = 2$ or $t = 6$	A1	
	$[s = \frac{1}{3}t^3 - 4t^2 + 12t (+c)]$	M1	Integrate v to find s
		A1	Correct integration
	$0 \leq t \leq 2 \quad s_1 = 8/3 - 16 + 24 = 32/3$ $2 \leq t \leq 6 \quad s_2 = (216/3 - 144 - 72) - (8/3 - 16 - 24) = -32/3$ $6 \leq t \leq 8$ $s_3 = (512/3 - 4 - 8^2 - 12 - 8) - (216/3 - 144 - 72) = 32/3$	M1	Attempt to find s_1, s_2 and s_3 Look for consideration of the need for 3 intervals Allow use of symmetry when finding s_1 , and s_3
		A1	2 correct values of displacement
	Total distance = 32 m	A1	All correct
		7	

Question	Answer	Mark	Guidance
6(i)	Particle A : $T = 4 \sin \theta$ Particle B : $T = 2$	M1	Resolve forces for A and for B
		M1	Eliminate T and solve for θ
	$\theta = 30$	A1	
		3	
6(ii)(a)	A : $T - 4 \sin 20 = 0.4a$ B : $2 - T = 0.2a$ System: $2 - 4 \sin 20 = (0.4 + 0.2)a$	M1	Apply Newton's second law to A or to B or to the system
		A1	Two correct equations
		M1	Solve for a or T
	$T = 1.79$ and $a = 1.05$	A1	Both correct
		4	
6(ii)(b)	$v^2 = 2 + 1.053 + 0.5 = 1.053$	M1	Attempt to find v using their $a \neq \pm g$
	$v = 1.03 \text{ ms}^{-1}$	A1	
		2	

Question	Answer	Mark	Guidance
6(ii)(c)	Loss in KE = $\frac{1}{2} \times 0.4 \times 1.053 = 0.2106$ Gain in PE = $0.4 \times 10 \times d \sin 20$	M1	Attempt KE loss or PE gain for particle <i>A</i> only after particle <i>B</i> hits the ground.
		A1ft	Both correct, <i>d</i> is distance moved up the plane after <i>B</i> hits ground
	$\frac{1}{2} \times 0.4 \times 1.053 = 0.4 \times 10 \times d \sin 20$	M1	Apply KE loss = PE gain
		A1	FT Correct energy equation
	Total dist <i>A</i> moves up plane = $0.5 \times d = 0.654$ m	A1	
		5	