

| Question | Answer | Marks | Guidance |
|----------|--|-----------|---|
| 1 | Substitute -1 into $p(x)$ and equate to zero | M1 | Allow algebraic long division or the use of an identity with the remainder, in terms of m and k , equated to zero |
| | Obtain $-4 + (k + 1) + m + 3k = 0$ or equivalent | A1 | |
| | Obtain $m = 3 - 4k$ | A1 | |
| | | 3 | |

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|----------|---|-----------|---|
| 2(i) | State or imply non-modular equation $(4 + 2x)^2 = (3 - 5x)^2$ or pair of linear equations | B1 | |
| | Attempt solution of 3-term quadratic eqn or pair of linear equations | M1 | |
| | Obtain $-\frac{1}{7}, \frac{7}{3}$ | A1 | SC B1 for $x = -\frac{1}{7}$ from one linear equation |
| | | 3 | |
| 2(ii) | Attempt correct process to solve $e^{3y} = k$ where $k > 0$ from (i) | M1 | |
| | Obtain 0.282 and no others | A1 | |
| | | 2 | |

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| 3 | Use quotient rule to find first derivative or equivalent | *M1 | |
| | Obtain $\frac{dy}{dx} = \frac{3 \ln x - 3x \times \frac{1}{x}}{(\ln x)^2}$ or equivalent | A1 | Condone lack of brackets in denominator unless specifically simplified to $2 \ln x$ |
| | Equate first derivative to zero and attempt value of x from $\ln x = k$ oe | DM1 | Must get as far as $x =$ |
| | Obtain $x = e$ | A1 | Allow e^1 |
| | Obtain $y = 3e$ | A1 | Allow $3e^1$ SC1: If $3 \ln x - 3x \times \frac{1}{x} = 0$ seen with no reference to $\frac{dy}{dx}$, then allow M1 A1 then following marks SC2: If denominator incorrect and numerator correct/reversed/added then max marks M0A0M1A1A1 SC3: If numerator reversed then max marks M1A0M1A1A1 |
| | | 5 | |

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| 4(a) | Use identity $2 \cos^2 x = 1 + \cos 2x$ | B1 | |
| | Integrate to obtain form $x + \frac{1}{2} \sin 2x$ | B1 | |
| | Integrate to obtain $-2 \cos 2x$ | B1 | |
| | Apply limits correctly, retaining exactness | M1 | Dependent on at least one B mark |
| | Obtain $4 + \frac{1}{2}\pi$ or similarly simplified equivalent | A1 | |
| | | 5 | |
| 4(b) | Use y values $\sqrt{\ln 3}$, $\sqrt{\ln 6}$, $\sqrt{\ln 9}$ or decimal equivalents | B1 | Allow awrt 1.05, 1.34, 1.48, the correct level of accuracy may be implied by a correct answer |
| | Use correct formula, or equivalent, with $h = 3$, and three y values | M1 | |
| | Obtain $\frac{1}{2} \times 3(\sqrt{\ln 3} + 2\sqrt{\ln 6} + \sqrt{\ln 9})$ and hence 7.81 | A1 | Allow greater accuracy |
| | | 3 | |

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| 5(i) | Carry out division to obtain quotient of form $x^2 + k$ | M1 | |
| | Obtain quotient $x^2 - 4$ | A1 | Allow use of an identity |
| | Obtain remainder 4 | A1 | |
| | | 3 | SC: If only the remainder theorem is used to obtain 4 then B1 |

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| 5(ii) | Integrate to obtain at least k_1x^3 and $k_2 \ln(2x+1)$ terms using the result from (i) | *M1 | |
| | Obtain correct $\frac{1}{3}x^3 - 4x + 2\ln(2x+1)$ | A1 | |
| | Apply limits and note or imply that constant k_3 can be written $\ln e^{k_3}$ | DM1 | |
| | Apply appropriate logarithm properties correctly | M1 | |
| | Obtain $\ln(49e^{-3})$ | A1 | |
| | | 5 | |

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| 6(i) | Equate $4t^2e^{-t}$ to 1, rearrange to $t^2 = \dots$ and hence $t = \dots$ | M1 | Allow M1 for $t = \sqrt{\frac{1}{4}e^{-t}}$ |
| | Confirm $t = \frac{1}{2}e^{\frac{1}{2}t}$ with necessary detail needed as answer is given | A1 | |
| | | 2 | |
| 6(ii) | Use iterative process correctly at least once | M1 | |
| | Obtain final answer $t = 0.715$ | A1 | |
| | Show sufficient iterations to 5 sf to justify answer or show a sign change in the interval [0.7145, 0.7155] | A1 | SC: M1A1 from iterations to 4sf resulting in 0.71 |
| | | 3 | |

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| 6(iii) | Obtain $\frac{dx}{dt} = 3 + 12e^{-2t}$ | B1 | |
| | Use product rule to find $\frac{dy}{dt}$ | M1 | |
| | Obtain $8te^{-t} - 4t^2e^{-t}$ | A1 | |
| | Divide correctly to obtain $\frac{dy}{dx}$ | M1 | |
| | Substitute value from part (ii) to obtain 0.31 | A1 | Allow greater accuracy |
| | | 5 | |

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| 7(a)(i) | State $R = \sqrt{32}$ or equivalent or 5.657... | B1 | |
| | Use appropriate trigonometry to find α | M1 | |
| | Obtain $\alpha = 45$ | A1 | |
| | | 3 | |
| 7(a)(ii) | Carry out correct process to find one value of θ | M1 | |
| | Obtain 17.1 | A1 | Ignore other positive values greater than 17.1 |
| | | 2 | |

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| 7(b) | Use or imply $\cot 2x = \frac{1}{\tan 2x}$ | B1 | |
| | Use identity of form $\tan 2x = \frac{\pm 2 \tan x}{1 \pm \tan^2 x}$ to obtain equation in $\tan x$ | M1 | |
| | Obtain $6 \tan^2 x + 10 \tan x - 4 = 0$ or equivalent | A1 | |
| | Attempt solution of 3-term quadratic equation for $\tan x$ | M1 | |
| | Obtain $\tan x = \frac{1}{3}$ and hence 0.32 | A1 | Allow greater accuracy |
| | Obtain $\tan x = -2$ and hence 2.03 and no others between 0 and π | A1 | Allow greater accuracy |
| | | 6 | |