| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 1 | For $\left(\frac{2}{\boldsymbol{x}}-3 x\right)^{5}$ term in $x$ is 10 or $5 \mathrm{C}_{3}$ or $5 \mathrm{C} 2 \times\left(\frac{2}{x}\right)^{2} \times(-3 x)^{3}$ or | B2,1 | 3 elements required. -1 for each error with or <br> without $x$ 's. Can be seen in an expansion. |
|  | $\left(\frac{2}{x}\right)^{5} \frac{5.4 .3}{3!}\left(-\frac{3}{2} x^{2}\right)^{3}$ or $(-3 x)^{5} \frac{5.4}{2!}\left(\frac{2}{3 x^{2}}\right)^{2}$ | B1 | Allow $-1080 x$ <br> Allow if expansion stops at this term. <br> Allow from expanding brackets. |
|  | -1080 identified | $\mathbf{3}$ |  |


| Question | Answer | Marks |  |
| :---: | :--- | ---: | :--- |
| 2 | Midpoint of $A B$ is $(5,1)$ | B1 | Can be seen in working, accept $\left(\frac{10}{2}, \frac{2}{2}\right)$. |
|  | $m_{A B}=-1 / 2$ oe | B1 |  |
|  | C to $(5,1)$ has gradient 2 | $* \mathbf{M 1}$ | Use of $m_{1} \times m_{2}=-1$. |
|  | Forming equation of line $(y=2 x-9)$ | DM1 | Using their perpendicular gradient and their <br> midpoint to form the equation. |
|  | $C(0,-9)$ or $y=-9$ | A1 |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| $3(\mathrm{i})$ | $\frac{\mathrm{d} y}{\mathrm{~d} t}=\frac{\mathrm{d} y}{\mathrm{~d} x} \times \frac{\mathrm{d} x}{\mathrm{~d} t}=7 \times-0.05$ | M1 | Multiply numerical gradient at $x=2$ by $\pm 0.05$. |
|  | $-0.35(\mathrm{units} / \mathrm{s})$ or Decreasing at a rate of $(+) 0.35$ | $\mathbf{A 1}$ | Ignore notation and omission of units |
|  | 3(ii) | $(y)=\frac{x^{4}}{4}+\frac{4}{x}(+c)$ oe | $\mathbf{2}$ |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | $a^{2}+2 a b+b^{2}, a^{2}-2 a b+b^{2}$ | B1 | Correct expansions. |
|  | $\sin ^{2} x+\cos ^{2} x=1$ used $\rightarrow(a+b)^{2}+(a-b)^{2}=1$ | M1 | Appropriate use of $\sin ^{2} x+\cos ^{2} x=1$ with $(a+b)^{2}$ and $(a-b)^{2}$ |
|  | $a^{2}+b^{2}=1 / 2$ | A1 | No evidence of $\pm 2 a b$, scores $2 / 3$ |
|  | Alternative method for question 4(i) |  |  |
|  | $2 a=(\mathrm{s}+\mathrm{c}) \& 2 b=(\mathrm{s}-\mathrm{c})$ or $a=1 / 2(\mathrm{~s}+\mathrm{c}) \& b=1 / 2(\mathrm{~s}-\mathrm{c})$ | B1 |  |
|  | $a^{2}+b^{2}=\frac{1}{4}(s+c)^{2}+\frac{1}{4}(s-c)^{2}=1 / 2\left(\mathrm{~s}^{2}+\mathrm{c}^{2}\right)$ | M1 | Appropriate use of $\sin ^{2} x+\cos ^{2} x=1$ |
|  | $a^{2}+b^{2}=1 / 2$ | A1 | Method using only $(\sin x-b)^{2}$ and $(a-\cos x)^{2}$ scores $0 / 3$. |
|  |  | 3 | SC B1 for assuming $\theta$ is acute giving $a=\frac{1}{\sqrt{5}}+b$ or $2 \sqrt{5}-b$ |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(ii) | $\tan x=\frac{\sin x}{\cos x} \rightarrow \frac{a+b}{a-b}=2$ | M1 | Use of $\tan x=\frac{\sin x}{\cos x}$ to form an equation in a and $b$ only |
|  | $a=3 b$ | A1 |  |
|  |  | 2 |  |


| Question | Answer | Marks |  |
| :---: | :--- | ---: | :--- |
| 5 | Perimeter of $A O C=2 r+r \theta$ | $\mathbf{B 1}$ |  |
|  | Angle $C O B=\pi-\theta$ | $\mathbf{B 1}$ | Could be on the diagram. Condone $180-\theta$. |
|  | Perimeter of $B O C=2 r+r(\pi-\theta)$ | $\mathbf{B 1}$ | FT on angle $C O B$ if of form $(k \pi-\theta), k>0$. |
|  | $(2 r+) \pi r-r \theta=2((2 r)+r \theta)$ <br> $\left(2+\pi-\theta=4+2 \theta \rightarrow \theta=\frac{\pi-2}{3}\right)$ | M1 | Sets up equation using $r(k \pi-\theta)$ and $\times 2$ on correct <br> side. Condone any omissions of OA, OB and/or <br> OC. |
|  | $\theta=0.38$ | $\mathbf{A 1}$ | Equivalent answer in degrees scores A0. |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(i) | 3, -3 | B1 | Accept $\pm 3$ |
|  | $-1 / 2$ | B1 |  |
|  | $21 / 2$ | B1 |  |
|  |  | 3 | Condone misuse of inequality signs. |
| 6(ii) |  |  | Only mark the curve from $0 \rightarrow 2 \pi$. If the $x$ axis is not labelled assume that $0 \rightarrow 2 \pi$ is the range shown. Labels on axes are not required. |
|  | 2 complete oscillations of a cosine curve starting with a maximum at ( $0, a), \mathrm{a}>0$ | B1 |  |
|  | Fully correct curve which must appear to level off at 0 and/or $2 \pi$. | B1 |  |
|  | Line starting on positive $y$ axis and finishing below the $x$ axis at $2 \pi$. Must be straight. | B1 |  |
|  |  | 3 |  |
| 6(iii) | 4 | B1 |  |
|  |  | 1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | $\left(\mathrm{f}^{-1}(x)\right)=\frac{x+2}{3} \text { oe }$ | B1 |  |
|  | $y=\frac{2 x+3}{x-1} \rightarrow(x-1) y=2 x+3 \rightarrow x(y-2)=y+3$ | M1 | Correct method to obtain $x=$, (or $y=$, if interchanged) but condone $+/$ - sign errors |
|  | $\left(\mathrm{g}^{-1}(x)\right.$ or $\left.y\right)=\frac{x+3}{x-2}$ oe $\left(\operatorname{eg} \frac{5}{x-2}+1\right)$ | A1 | Must be in terms of $x$ |
|  | $x \neq 2$ only | B1 | FT for value of $x$ from their denominator $=0$ |
|  |  | 4 |  |
| 7(ii) | $(f g(x)=) \frac{3(2 x+3)}{x-1}-2\left(=\frac{7}{3}\right)$ | B1 |  |
|  | $\begin{aligned} & 18 x+27=13 x-13 \text { or } 3(4 x+11)=7(x-1) \\ & (5 x=-40) \end{aligned}$ | M1 | Correct method from their $f g=\frac{7}{3}$ leading to a linear equation and collect like terms. Condone omission of $2(x-1)$. |
|  | Alternative method for question 7(ii) |  |  |
|  | $\left(\mathrm{f}^{-1}\left(\frac{7}{3}\right)\right)=\frac{13}{9}$ | B1 |  |
|  | $\frac{2 x+3}{x-1}=\frac{13}{9} \rightarrow 9(2 x+3)=13(x-1)(\rightarrow 5 x=-40)$ | M1 | Correct method from $g(x)=$ their $\frac{13}{9}$ leading to a linear equation and collect like terms. |
|  | $x=-8$ | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 8(i) | $\begin{aligned} & 6 \times 3+-2 \times \mathrm{k}+-6 \times-3=0 \\ & (18-2 k+18=0) \end{aligned}$ | M1 | Use of scalar product $=0$. <br> Could be $\overrightarrow{A O} \cdot \overrightarrow{O B}, \overrightarrow{A O} \cdot \overrightarrow{B O}$ or $\overrightarrow{O A} \cdot \overrightarrow{B O}$ |
|  | $k=18$ | A1 |  |
|  | Alternative method for question 8(i) |  |  |
|  | $76+18+k^{2}=18+(k+2)^{2}$ | M1 | Use of Pythagoras with appropriate lengths. |
|  | $k=18$ | A1 |  |
|  |  | 2 |  |
| 8(ii) | $36+4+36=9+k^{2}+9$ | M1 | Use of modulus leading to an equation and solve to $k=$ or $k^{2}=$ |
|  | $k= \pm \sqrt{ } 58$ or $\pm 7.62$ | A1 | Accept exact or decimal answers. <br> Allow decimals to greater accuracy. |
|  |  | 2 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 8(iii) | $\overrightarrow{A B}=\left(\begin{array}{c}-3 \\ 6 \\ 3\end{array}\right) \rightarrow \overrightarrow{A C}=\left(\begin{array}{c}-2 \\ 4 \\ 2\end{array}\right)$ then $\overrightarrow{O A}+\overrightarrow{A C}$ | M1 | Complete method using $\overrightarrow{A C}= \pm 2 / 3 \overrightarrow{A B}$ And then $\overrightarrow{O A}+$ their $\overrightarrow{A C}$ |
|  | $\overrightarrow{O C}=\left(\begin{array}{c}4 \\ 2 \\ -4\end{array}\right)$ | A1 |  |
|  | $\div \sqrt{(\text { their } 4)^{2}+(\text { their } 2)^{2}+(\text { their }-4)^{2}}$ | M1 | Divides by modulus of their $\overrightarrow{O C}$ |
|  | $=\frac{1}{6}\left(\begin{array}{c}4 \\ 2 \\ -4\end{array}\right)$ or $\frac{1}{6}(4 i+2 j-4 k)$ | A1 |  |
|  | Alternative method for question 8(iii) |  |  |
|  | Let $\overrightarrow{O C}=\left(\begin{array}{l}p \\ q \\ r\end{array}\right) \rightarrow \overrightarrow{A C}=\left(\begin{array}{c}p-6 \\ q+2 \\ r+6\end{array}\right) \& \overrightarrow{C B}=\left(\begin{array}{c}3-p \\ 4-q \\ -3-r\end{array}\right)$ | M1 | Correct method. Equates coefficients leading to values for $p, q, r$ |
|  | $\begin{aligned} & p-6=2(3-p) ; q+2=2(4-q) ; r+6=2(-3-r) \\ & \rightarrow p=4, q=2 \& r=-4 \end{aligned}$ | A1 |  |
|  | $\div \sqrt{(\text { their } 4)^{2}+(\text { their } 2)^{2}+(\text { their }-4)^{2}}$ | M1 | Divides by modulus of their $\overrightarrow{O C}$ |
|  | $=\frac{1}{6}\left(\begin{array}{c}4 \\ 2 \\ -4\end{array}\right)$ or $\frac{1}{6}(4 i+2 j-4 k)$ | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 8(iii) | Alternative method for question 8(iii) |  |  |
|  | $\begin{aligned} \overrightarrow{C B}= & \overrightarrow{O B}-\overrightarrow{O C} \therefore 2(\overrightarrow{O B}-\overrightarrow{O C})=\overrightarrow{O C}-\overrightarrow{O A} \\ & \rightarrow 2 \overrightarrow{O B}+\overrightarrow{O A}=3 \overrightarrow{O C} \therefore 3 \overrightarrow{O C}=\left(\begin{array}{c} 12 \\ 6 \\ -12 \end{array}\right) \end{aligned}$ | M1 | Correct method. Gets to a numerical expression for $\mathrm{k} \overrightarrow{O C}$ from $\overrightarrow{O A} \& \overrightarrow{O B}$. |
|  | $\overrightarrow{O C}=\left(\begin{array}{c}4 \\ 2 \\ -4\end{array}\right)$ | A1 |  |
|  | $\div \sqrt{(\text { their } 4)^{2}+(\text { their } 2)^{2}+(\text { their }-4)^{2}}$ | M1 | Divides by modulus of their $\overrightarrow{O C}$ |
|  | $=\frac{1}{6}\left(\begin{array}{c}4 \\ 2 \\ -4\end{array}\right)$ or $\frac{1}{6}(4 i+2 j-4 k)$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 9 | For $\mathrm{C}_{1}: \frac{\mathrm{d} y}{\mathrm{~d} x}=2 x-4 \rightarrow m=2$ | B1 |  |
|  | $y-$ 'their 4 ' $=$ 'their $\mathrm{m} '(x-3)$ or using $y=m x+c$ | M1 | Use of : $\frac{\mathrm{d} y}{\mathrm{~d} x}$ and (3, their 4) to find the tangent equation. |
|  | $y-4=2(x-3)$ or $y=2 x-2$ | A1 | If using $=m x+c$, getting $c=-2$ is enough. |
|  | $2 x-2=\sqrt{4 x+k}\left(\rightarrow 4 x^{2}-12 x+4-k=0\right)$ | *M1 | Forms an equation in one variable using tangent \& $\mathrm{C}_{2}$ |
|  | Use of $b^{2}-4 a c=0$ on a 3 term quadratic set to 0. | *DM1 | Uses 'discriminant $=0$ ' |
|  | $144=16(4-k) \rightarrow k=-5$ | A1 |  |
|  | $4 x^{2}-12 x+4-k=0 \rightarrow 4 x^{2}-12 x+9=0$ | DM1 | Uses $k$ to form a 3 term quadratic in $x$ |
|  | $x=\frac{3}{2}\left(\right.$ or $\left.\frac{1}{2}\right), y=1($ or -1$)$. | A1 | Condone 'correct' extra solution. |
|  | Alternative method for question 9 |  |  |
|  | For $\mathrm{C}_{1}: \frac{\mathrm{d} y}{\mathrm{~d} x}=2 x-4 \rightarrow m=2$ | B1 |  |
|  | $y-$ 'their 4 ' $=$ 'their m ' $(x-3)$ or using $y=m x+c$ | M1 | Use of : $\frac{\mathrm{d} y}{\mathrm{~d} x}$ and (3, their 4) to find the tangent equation. |
|  | $y-4=2(x-3)$ or $y=2 x-2$ | A1 | If using $=m x+c$, getting $c=-2$ is enough. |
|  | For $\mathrm{C}_{2}: \frac{d y}{d x}=A(4 x+k)^{-\frac{1}{2}}$ | *M1 | Finds $\frac{d y}{d x}$ for $C_{2}$ in the form $A(4 x+k)^{-\frac{1}{2}}$ |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 9 | At P: 'their 2 ' $=A(4 x+k)^{-\frac{1}{2}} \prime \rightarrow\left(x=\frac{1-k}{4}\right.$ or $\left.4 x+k=1\right)$ | *DM1 | Equating 'their 2' to 'their $\frac{d y}{d x}$, and simplify to form a linear equation linking $4 x+k$ and a constant. |
|  | $(2 x-2)^{2}=4 x+k \rightarrow(2 x-2)^{2}=1 \rightarrow\left(4 x^{2}-8 x+3=0\right)$ | DM1 | Using their $y=2 x-2, y^{2}=4 x+k$ and their $4 x+k=1$ (but not $=0$ ) to form a 3 term quadratic in $x$. |
|  | $x=\frac{3}{2}\left(\right.$ or $\left.\frac{1}{2}\right)$ and from $k=-5(o r-1)$ | A1 | Needs correct values for $x$ and $k$. |
|  | from $y^{2}=4 x+k, y=1($ or -1$)$. | A1 | Condone 'correct' extra solution. |
|  | Alternative method for question 9 |  |  |
|  | For $\mathrm{C}_{1}: \frac{\mathrm{d} y}{\mathrm{~d} x}=2 x-4 \rightarrow m=2$ | B1 |  |
|  | $y-$ 'their $4^{\prime}=$ 'their $\mathrm{m}^{\prime}(x-3)$ or using $y=m x+c$ | M1 | Use of : $\frac{\mathrm{d} y}{\mathrm{~d} x}$ and (3, their 4) to find the tangent equation. |
|  | $y-4=2(x-3)$ or $y=2 x-2$ | A1 | If using $=m x+c$, getting $c=-2$ is enough. |
|  | For $\mathrm{C}_{2}: \frac{d y}{d x}=A(4 x+k)^{-\frac{1}{2}}$ | *M1 | Finds $\frac{d y}{d x}$ for $C_{2}$ in the form $A(4 x+k)^{-\frac{1}{2}}$ |
|  | At P: 'their 2 ' $=A(4 x+k)^{-\frac{1}{2}} " \rightarrow\left(x=\frac{1-k}{4}\right.$ or $\left.4 x+k=1\right)$ | *DM1 | Equating 'their 2' to 'their $\frac{d y}{d x}$, and simplify to form a linear equation linking $4 x+k$ and a constant. |
|  | From $4 x+k=1$ and $y^{2}=4 x+k \rightarrow y^{2}=1$ | DM1 | Using their $4 x+k=1$ (but not $=0$ ) and $C_{2}$ to form $y^{2}=$ a constant |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 9 | $y=1($ or -1$)$ and $x=\frac{3}{2}\left(\right.$ or $\left.\frac{1}{2}\right)$ | $\mathbf{A 1}$ | Needs correct values for $y$ and $x$. |
|  | From $4 x+k=1, k=-5($ or -1$)$ | $\mathbf{A 1}$ | Condone 'correct' extra solution |
|  |  | $\mathbf{8}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 10(a)(i) | $S_{10}=S_{15}-S_{10}$ or $\mathrm{S}_{10}=\mathrm{S}_{(11 \text { to } 15)}$ | M1 | Either statement seen or implied. |
|  | $5(2 a+9 d)$ oe | B1 |  |
|  | $7.5(2 a+14 d)-5(2 a+9 d) \text { or } \frac{5}{2}[(a+10 d)+(a+14 d)] \text { oe }$ | A1 |  |
|  | $d=\frac{a}{3} \mathbf{A G}$ | A1 | Correct answer from convincing working |
|  |  | 4 | Condone starting with $d=\frac{a}{3}$ and evaluating both summations as 25 a . |
| 10(a)(ii) | $(a+9 d)=36+(a+3 d)$ | M1 | Correct use of $a+(n-1) d$ twice and addition of $\pm 36$ |
|  | $a=18$ | A1 |  |
|  |  | 2 | Correct answer www scores 2/2 |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 10(b) | $S_{\infty}=9 \times S_{4} ; \frac{a}{1-r}=9 \frac{a\left(1-r^{4}\right)}{1-r} \text { or } 9\left(a+a r+a r^{2}+a r^{3}\right)$ | B1 | May have 12 in place of $a$. |
|  | $9\left(1-r^{\mathrm{n}}\right)=1$ where $n=3,4$ or 5 | M1 | Correctly deals with $a$ and correctly eliminates ' $1-r$ ' |
|  | $r^{4}=\frac{8}{9} \text { oe }$ | A1 |  |
|  | $\left(5^{\text {th }}\right.$ term $\left.=\right) 10^{2} / 3$ or 10.7 | A1 |  |
|  |  | 4 | Final answer of 10.6 suggests premature approximation - award $3 / 4$ www. |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 11(i) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=\left[\frac{1}{2}(4 x+1)^{-\frac{1}{2}}\right][\times 4]\left[-\frac{9}{2}(4 x+1)^{-\frac{3}{2}}\right][\times 4]$ | B1B1B1 | B1 B1 for each, without $\times 4$. B1 for $\times 4$ twice. |
|  | $\left(\frac{2}{\sqrt{4 x+1}}-\frac{18}{(\sqrt{4 x+1})^{3}}\right.$ or $\left.\frac{8 x-16}{(4 x+1)^{\frac{3}{2}}}\right)$ |  | SC If no other marks awarded award B1 for both powers of $(4 x+1)$ correct. |
|  | $\int y \mathrm{~d} x=\left[\frac{(4 x+1)^{\frac{3}{2}}}{\frac{3}{2}}\right][\div 4]+\left[\frac{9(4 x+1)^{\frac{1}{2}}}{\frac{1}{2}}\right][\div 4](+\mathrm{C})$ | B1B1B1 | B1 B1 for each, without $\div 4$. B1 for $\div 4$ twice. +C not required. |
|  | $\left(\frac{(\sqrt{4 x+1})^{3}}{6}+\frac{9}{2}(\sqrt{4 x+1})(+C)\right)$ |  | SC If no other marks awarded, B1 for both powers of $(4 x+1)$ correct. |
|  |  | 6 |  |
| 11(ii) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=0 \rightarrow \frac{2}{\sqrt{4 x+1}}-\frac{18}{(4 x+1)^{\frac{3}{2}}}=0$ | M1 | Sets their $\frac{\mathrm{d} y}{\mathrm{~d} x}$ to 0 (and attempts to solve |
|  | $4 x+1=9$ or $(4 x+1)^{2}=81$ | A1 | Must be from correct differential. |
|  | $x=2, y=6$ or M is $(2,6)$ only . | A1 | Both values required. <br> Must be from correct differential. |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 11(iii) | Realises area is $\int y \mathrm{~d} x$ and attempt to use their 2 and sight of 0 . | *M1 | Needs to use their integral and to see 'their 2' substituted. |
|  | Uses limits 0 to 2 correctly $\rightarrow[4.5+13.5]-\left[\frac{1}{6}+4.5\right](=131 / 3)$ | DM1 | Uses both 0 and 'their 2' and subtracts. Condone wrong way round. |
|  | $\left(\right.$ Area $=1^{11 / 3}$ or 1.33 | A1 | Must be from a correct differential and integral. |
|  |  | 3 | $131 / 3$ or $11 / 3$ with little or no working scores M1DM0A0. |

