| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 1 | $\lambda=4.4$ | $\mathbf{B 1}$ |  |
|  | $\mathrm{P}(X<4)=\mathrm{e}^{-4.4}\left(1+4.4+\frac{4.4^{2}}{2}+\frac{4.4^{3}}{3!}\right)$ | $\mathbf{M 1}$ | Allow any $\lambda$ allow one end error |
|  | $=0.359$ | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2 | A: $\mathrm{N}(6,4.8)$ | B1 B1 | B1 for $\mathrm{N}(6, .$.$) for either \mathrm{A}$ or B. B1 for 4.8 (or $2.19^{2}$ ) (or $\mathrm{SD}=2.19$ ) |
|  | B: $\mathrm{N}(6,2.4)$ | B1 | B1 For 2.4 (or $1.55^{2}$ ) (or $\mathrm{SD}=1.55$ ) (SR $3 / 3$ but error seen withhold B1 so $2 / 3$ scored) |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 3 (i) | $52 \pm z \times \frac{6.5}{\sqrt{15}}$ | M1 | Expression of the correct form. Any $z$ |
|  | $z=1.96$ | B1 | Seen or used |
|  | 48.7 to $55.3(3 \mathrm{sf})$ | A1 | Must be an interval |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 3 (ii) | Narrower <br> because more information or <br> because $\frac{\sigma}{\sqrt{n}}$ smaller | $\mathbf{B 1}$ | oe <br> Accept 'sample size is larger' 'more employees' 'width inversely proportional to sq root of n <br> 'if n increases width decreases' '95\% CI is 49.7 to 54.3' <br> or similar. No contradictions |
|  |  | $\mathbf{1}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | $\operatorname{Est}(\mu)=495.9$ | B1 | Accept 496 |
|  | $\operatorname{Est}\left(\sigma^{2}\right)=\frac{10}{9}\left(\frac{2459283}{10}-" 495.9{ }^{2}\right)$ | M1 | Attempt $\Sigma x^{2}$ and subst in correct formula (1/9("2459283" - " 4959 " $\left.2 / 10\right)$ ). May be implied by correct answer |
|  | $=12.8(3 \mathrm{sf})$ or $383 / 30$ | A1 | (Note: Biased var " 11.49 " scores M0 A0) |
|  |  | 3 |  |
| 4(ii) | $\begin{aligned} & \mathrm{H}_{0}: \mu=505 \\ & \mathrm{H}_{1}: \mu<505 \\ & \frac{75660-505}{} \\ & \frac{150}{3.6 \div \sqrt{150}} \end{aligned}$ | B1 | Allow 'Pop mean' but not just 'mean' |
|  | $=-2.04$ | M1 | Correct stand'n; must have $\sqrt{ } 150$. No sd/var mixes. Condone sample SD (3.58/3.39) Accept standardisation of totals ((75660-75750)/44.091) Accept CV method |
|  |  | A1 | Accept +2.04 (Note: if valid area comparison done $0.0207 / 0.0206$ or 0.979 needed for A1) |
|  | comp $z=-2.054$ | M1 | Valid comparison of z's or area (0.0207/6>0.02; $0.979(3)<0.98)$ |
|  | No evidence (at 2\%) that machine pkts mean mass $<505$ | A1ft | oe No contradictions. <br> SC Two tail test can score B0 M1 A1 M1 for comparison with 2.326 A0 (max 3/5) |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 4 (iii) | Large sample, so sample mean approx <br> normally distr'd | B1 | Allow just 'Sample is large' or ' $n$ is large' $n>30$ |
|  |  | $\mathbf{1}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(i) | $\frac{1}{2} \times a \times b=1$ | M1 | Attempt $\Delta$ area $=1$ or $\int(b-b x / a) \mathrm{d} x=1$ with correct limits |
|  | $b=\frac{2}{a}$ | A1 |  |
|  |  | 2 |  |
| 5(ii) | $\operatorname{grad}=-\frac{2}{a^{2}}$ or $-\frac{b}{a}$ | B1 | allow without '-' sign (could be implied or seen in (i)) |
|  | $y-\left(\frac{2}{a}\right)=\operatorname{grad} \times x$ or $y=\operatorname{grad} \times(x-a)$ | M1 | correct use of $y=m x+c$ or $y-y_{1}=m\left(x-x_{1}\right)$ with $(0, \mathrm{~b})$ or $(\mathrm{a}, 0)$ including attempt at substitution of their $b$ |
|  | $\begin{aligned} & y-\left(\frac{2}{a}\right)=-\frac{2}{a^{2}} x \text { or } y=-\frac{2}{a^{2}}(x-a) \\ & \text { and } y=\frac{2}{a}-\frac{2}{a^{2}} x \quad \text { AG } \end{aligned}$ | A1 | No errors seen |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(iii) | $\int_{0}^{a}\left(\frac{2}{a} x-\frac{2}{a^{2}} x^{2}\right) \mathrm{d} x$ | M1 | Attempt int $x \mathrm{f}(x)$ ignore limits |
|  | $=\left[\frac{1}{a} x^{2}-\frac{2}{3 a^{2}} x^{3}\right]_{0}^{a}$ | A1 | Correct integration ignore limits |
|  | $a-\frac{2}{3} a=0.5$ | M1 | Sub correct limits into their integral and $=0.5$ |
|  | $a=1.5$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| $6(\mathrm{i})$ | Accidents occur independently or <br> randomly | $\mathbf{B 1}$ | In context. Allow 'singly'. |
|  |  | $\mathbf{1}$ |  |
|  | $\mathrm{e}^{-2.5} \times \frac{2.54}{4!}$ | $\mathbf{M 1}$ | Poisson P(4), allow any $\lambda$ |
|  | $=0.134(3 \mathrm{sfs})$ | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{2}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(iii) | $\lambda=\frac{25}{12}$ or 2.08(333) | B1 |  |
|  | $1-\mathrm{e}^{-\frac{25}{12}}\left(1+\frac{25}{12}+\frac{25^{2}}{2!}+\frac{25^{3}}{3!}\right)$ | M1 | 1 - Poisson $\mathrm{P}(0,1,2,3)$, allow any $\lambda$ allow one end error |
|  | $=0.158(3 \mathrm{sfs})$ | A1 | As final answer |
|  |  | 3 |  |
| 6(iv) | $\mathrm{N}\left(\frac{1825}{84}, \frac{1825}{84}\right)$ or $\mathrm{N}(21.7(26), 21.7(26))$ | B1 | Stated or implied |
|  | $\frac{29.5-\frac{1825}{84}}{\sqrt{\frac{1825}{84}}}$ | M1 | Allow with wrong or no cc with their mean/sd |
|  | $\Phi(" 1.668$ ") | M1 | Correct area consistent with their working |
|  | $=0.952(3 \mathrm{sfs})$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | $\begin{aligned} & \mathrm{H}_{0}: \mathrm{P}(10)=0.1 \\ & \mathrm{H}_{1}: \mathrm{P}(10)>0.1 \end{aligned}$ | B1 | Both. Allow ' $p$ ' for $\mathrm{P}(10)$ |
|  | $\begin{aligned} & \mathrm{B}(9,0.1) \\ & \mathrm{P}(X \geqslant 3)= \\ & 1-\left(0.9^{9}+9 \times 0.9^{8} \times 0.1+{ }^{9} \mathrm{C}_{2} \times 0.9^{7} \times\right. \\ & \left.0.1^{2}\right) \end{aligned}$ | M1 | Allow one extra term in bracket |
|  | $=0.05297 \ldots$ or 0.053(0) | A1 |  |
|  | comp 0.01 | M1 | Valid comparison. (comparison with 0.99 can recover previous M1 A1 for 0.9470) |
|  | No evidence (at $1 \%$ level) to reject $\mathrm{H}_{0}$ Claim not justified | A1ft | No contradictions |
|  |  | 5 |  |
| 7(ii) | $\mathrm{H}_{0}$ not rejected oe | B1 |  |
|  |  | 1 |  |
| 7(iii) | $\begin{aligned} & \mathrm{P}(X \geqslant 4) \\ & =" 0.05297 "-{ }^{9} \mathrm{C}_{3} \times 0.9^{6} \times 0.1^{3} \end{aligned}$ | M1 | or $1-\left(0.9^{9}+9 \times 0.9^{8} \times 0.1+{ }^{9} \mathrm{C}_{2} \times 0.9^{7} \times 0.1^{2}+{ }^{9} \mathrm{C}_{3} \times 0.9^{6} \times 0.1^{3}\right)$ |
|  | $=0.00833$ | A1 | Note: 0.05297 and 0.00833 both needed in (i) or (iii) to justify CV |
|  | Hence crit value is 4 | B1 | Allow without working. Or in (i) May be implied by attempt at $\mathrm{P}(X<4)$ below |
|  | $\begin{aligned} & \mathrm{B}(9,0.5) \\ & \mathrm{P}(X<4) \end{aligned}$ | M1 | stated or implied |
|  | $\begin{aligned} & =0.5^{9}+9 \times 0.5^{8} \times 0.5+{ }^{9} \mathrm{C}_{2} \times 0.5^{7} \times \\ & 0.5^{2}+{ }^{9} \mathrm{C}_{3} \times 0.5^{6} \times 0.5^{3} \end{aligned}$ | M1 | Attempt $\mathrm{P}(X<4)$ with $p=0.5$ |
|  | $\mathrm{P}($ Type II) $=0.254(3 \mathrm{sf})$ | A1 |  |
|  |  | 6 |  |

