| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1(i) | 38 | B1 |  |
|  |  | 1 |  |
| 1(ii) | Median $=38.5$ | B1 | CAO |
|  | $\mathrm{IQR}=40-38$ | M1 | $39<\mathrm{UQ}<45-36<\mathrm{LQ} \leqslant 38$ |
|  | $=2$ | A1 | If M0 awarded <br> SCB1 for both $\mathrm{UQ}=40$ or 40.5 and $\mathrm{LQ}=38$ or 37.75 seen |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2(i) | Method 1 $\mathrm{P}(M \cap H)=\frac{3}{4} \times \frac{3}{5}=\frac{9}{20}(0.45)$ | B1 | Seen, accept unsimplified |
|  | $\mathrm{P}(F$ or $M \cap H)=\frac{1}{4}+\frac{9}{20}=\frac{14}{20}$ | M1 | Numerical attempt at $\mathrm{P}(F)+\mathrm{P}(M \cap H)$ |
|  | 420 | A1 | Correct unsimplified expression |
|  | $=\frac{7}{10}(0.7) \mathrm{OE}$ | A1 | Correct final answer |
|  | Method 2 $\begin{equation*} \mathrm{P}\left(M \cap H^{\prime}\right)=\frac{3}{4} \times \frac{2}{5}=\frac{6}{20} \tag{0.3} \end{equation*}$ | B1 | Seen, accept unsimplified |
|  | $\mathrm{P}(F$ or $M \cap H)=1-\mathrm{P}\left(M \cap H^{\prime}\right)$ | M1 | Numerical attempt at $1-\mathrm{P}\left(M \cap H^{\prime}\right)$ |
|  | $=1-\frac{3}{4} \times \frac{2}{5}$ | A1 | Correct unsimplified expression |
|  | $=\frac{7}{10}(0.7) \mathrm{OE}$ | A1 | Correct final answer |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2(i) | Method 3 $\mathrm{P}\left(F \cap H^{\prime} \text { or } H\right)=\frac{1}{4} \times \frac{1}{5}+\frac{1}{4} \times \frac{4}{5}+\frac{3}{4} \times \frac{3}{5}$ | B1 | $\frac{3}{4} \times \frac{3}{5}\left(\frac{9}{20}\right)$ or $\frac{1}{4} \times \frac{4}{5}\left(\frac{4}{20}\right)$ or $\frac{3}{4} \times \frac{3}{5}+\frac{1}{4} \times \frac{4}{5}\left(\frac{13}{20}\right)$ seen |
|  | $=\frac{1}{20}+\frac{4}{20}+\frac{9}{20}$ | M1 | Numerical attempt at $\mathrm{P}\left(F \cap H^{\prime}\right)+\mathrm{P}(F \cap H)+\mathrm{P}(M \cap H)$ |
|  |  | A1 | Correct unsimplified expression |
|  | $=\frac{7}{10}(0.7) \mathrm{oe}$ | A1 | Correct final answer |
|  | Method 4 - Venn diagram style approach $\mathrm{P}(F \mathrm{U} H)=\mathrm{P}(F)+\mathrm{P}(H)-\mathrm{P}(F \cap H)$ | B1 | $\frac{3}{4} \times \frac{3}{5}\left(\frac{9}{20}\right)$ or $\frac{1}{4} \times \frac{4}{5}\left(\frac{4}{20}\right)$ or $\frac{3}{4} \times \frac{3}{5}+\frac{1}{4} \times \frac{4}{5}\left(\frac{13}{20}\right)$ seen |
|  | $=\frac{1}{4}+\frac{1}{4} \times \frac{4}{5}+\frac{3}{4} \times \frac{3}{5}-\frac{1}{4} \times \frac{4}{5}$ | M1 | Numerical attempt at $\mathrm{P}(F)+\mathrm{P}(H)-\mathrm{P}(F \cap H)$ |
|  | $=\frac{1}{4}+\frac{4}{20}+\frac{9}{20}-\frac{4}{20}$ | A1 | Correct unsimplified expression |
|  | $=\frac{7}{10}(0.7) \mathrm{oe}$ | A1 | Correct final answer |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2(ii) | Method 1 $\begin{aligned} & (\mathrm{P}(M) \times \mathrm{P}(H)=) \frac{3}{4} \times \text { their } \frac{13}{20}=\frac{39}{80} \\ & (\mathrm{P}(M \cap H)=) \frac{3}{4} \times \frac{3}{5}=0.45 \end{aligned}$ | M1 | Unsimplified, or better, legitimate numerical attempt at $\mathrm{P}(M) \times \mathrm{P}(H)$ and $\mathrm{P}(M \cap H)$ <br> Descriptors $\mathrm{P}(M \cap H)$ and $\mathrm{P}(M) \times \mathrm{P}(H)$ seen, correct numerical evaluation and comparison, conclusion stated |
|  | $\frac{39}{80}(0.4875) \neq 0.45$, not independent | A1 |  |
|  | Method 2 $\begin{aligned} \mathrm{P}(M \mid H) & =\frac{\mathrm{P}(M \cap H)}{\mathrm{P}(H)}=\frac{\frac{9}{20}}{\text { their } \frac{13}{20}}=\frac{9}{13} \\ \mathrm{P}(M) & =\frac{3}{4} \end{aligned}$ | M1 | Unsimplified, or better, numerical attempt at $\mathrm{P}(H)$ and $\mathrm{P}(M \cap H), \mathrm{P}(M)$ |
|  | $\frac{9}{13} \neq \frac{3}{4}$, not independent | A1 | Descriptors $\mathrm{P}(M \cap H), \mathrm{P}(H)$ and $\mathrm{P}(M)$ OR $\mathrm{P}(M \mid H)$ and $\mathrm{P}(M)$ seen, numerical evaluation and comparison, conclusion stated <br> Any appropriate relationship can be used, the M is awarded for an unsimplified, or better, numerical attempt at the terms required, the A mark requires the correct descriptors, numerical evaluation and comparison and the conclusion |
|  |  | 2 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3(i) | $z=-1.282$ | B1 | $\pm 1.282$ seen |
|  | $-1.282=\frac{440-\mu}{9}$ | M1 | $\pm$ Standardisation equation with 440,9 and $\mu$, equated to a $z$-value, (not $1-z$-value or probability e.g. $0.1841,0.5398,0.6202,0.8159$ ) |
|  | $\mu=452$ | A1 | Correct answer rounding to 452, not dependent on B1 |
|  |  | 3 |  |
| 3(ii) | $\mathrm{P}(z>1.8)=1-0.9641=0.0359$ | B1 |  |
|  | $\begin{aligned} \text { Number } & =0.0359 \times 150 \\ & =5.385 \end{aligned}$ | M1 | $p \times 150,0<p<1$ |
|  | $($ Number of cartons $=) 5$ | A1FT | Accept either 5 or 6 , not indicated as an approximation, e.g. $\sim$, about FT their $p \times 150$, answer as an integer |
|  |  | 3 |  |


| Question | Answer |  |  |  | Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4(i) | X | 0 | 1 | 2 | B1 | Prob distribution table drawn, top row correct with at least one probability $0<p<1$ entered, condone additional values with $p=0$ stated |
|  | Prob | $\frac{2}{7}$ | $\frac{4}{7}$ | $\frac{1}{7}$ |  |  |
|  | $\mathrm{P}(0)=\frac{5}{7} \times \frac{4}{6} \times \frac{3}{5}=\frac{2}{7}(0.2857)$ |  |  |  | B1 | One probability correct (need not be in table) |
|  | $\mathrm{P}(1)=\frac{2}{7} \times \frac{5}{6} \times \frac{4}{5} \times{ }^{3} C_{1}=\frac{4}{7}(0.5713)$ |  |  |  | B1 | Another probability correct (need not be in table). |
|  | $\mathrm{P}(2)=\frac{2}{7} \times \frac{1}{6} \times \frac{5}{5} \times{ }^{3} C_{2}=\frac{1}{7}(0.1429)$ |  |  |  | B1 | Values in table, all probs correct (to 3 SF ) or 3 probabilities summing to 1 |
|  |  |  |  |  | 4 |  |
| 4(ii) | $\begin{aligned} \operatorname{Var}(X) & =1 \times \frac{4}{7}+4 \times \frac{1}{7}-\left(\frac{6}{7}\right)^{2} \\ & =\frac{8}{7}-\left(\frac{6}{7}\right)^{2} \end{aligned}$ |  |  |  | M1 | Unsimplified correct numerical expression for variance or their probabilities from (i) $0<p<1$ in unsimplified variance expression |
|  | $=\frac{20}{49} \text { or } 0.408$ |  |  |  | A1 | Correct answer (0.40816...) nfww <br> Final answer does not imply the method mark |
|  |  |  |  |  | 2 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(i) | $a=40$ | B1 |  |
|  |  | 1 |  |
| 5(ii) | $\begin{aligned} & \text { Mean }=\frac{0.5 \times 14+1.5 \times 46+3.5 \times 102+7.5 \times \text { their } 40+20 \times 40}{242} \\ & =\frac{1533}{242} \end{aligned}$ | M1 | Numerator: 5 products with at least 3 acceptable mid-points $\times$ appropriate frequency FT (i). Denominator: 242 CAO <br> $\frac{1533}{242}$ implies M1, but if FT an unsimplified expression required |
|  | $=6 \frac{81}{242} \text { or } 6.33$ | A1 | CAO (6.3347 $\ldots$ r rounded to 3 or more SF) |
|  |  | 2 |  |
| 5(iii) | $\mathrm{fd}=14,46,34,\left(\frac{\text { their }(i)}{5}=\right) 8,2$ | M1 | Attempt at fd [f/(attempt at cw$)]$ or scaled freq |
|  |  | A1FT | Correct heights seen on diagram with linear vertical scale from $(x, 0)$ FT their $\frac{a}{5}$ only |
|  |  | B1 | Correct bar widths (1:1:3:5:20) at axis, visually no gaps, with linear horizontal scale from $(0, y)$, first bar starting at $(0,0)$ |
|  |  | B1 | Labels (time, mins, and $\mathrm{fd}(\mathrm{OE})$ seen, some may be as a title) and a linear scale with at least 3 values marked on each axis. <br> (Interval notation not acceptable) |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(a)(i) | $(\mathrm{AAAIU}) * * * *$ <br> Arrangements of vowels/repeats $\times$ arrangements of $($ consonants $\&$ vowel group $)=$ | M1 | $k \times 5!(k$ is an integer, $k \geqslant 1)$ |
|  | $\frac{5!\times 5!}{3!}$ | M1 | $\frac{m}{3}!(m \text { is an integer, } m \geqslant 1)$ <br> Both Ms can only be awarded if expression is fully correct |
|  | $=2400$ | A1 | Correct answer |
|  |  | 3 |  |
| 6(a)(ii) | E.g. $\mathrm{R} * * * \mathrm{~T} * * * \mathrm{~L}$. <br> Arrangements of consonants RL, RS, $\mathrm{SL}={ }^{3} \mathrm{P}_{2}=6$ <br> Arrangements of remaining letters $=\frac{6!}{3!}=120$ | M1 | $k \times \frac{6!}{3!}$ or $k \times{ }^{3} \mathrm{P}_{2}$ or $k \times{ }^{3} \mathrm{C}_{2}$ or $k \times 3$ ! or $k \times 3 \times 2(k$ is an integer, $k \geqslant 1)$, no irrelevant addition |
|  | Total $120 \times 6$ | M1 | Correct unsimplified expression or $\frac{6!}{3!} \times{ }^{3} \mathrm{C}_{2}$ |
|  | $=720$ ways | A1 | Correct answer |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(b) | $\begin{array}{lll} \text { Method 1 } \\ \mathrm{N}(2) & \mathrm{R}(8) & \mathrm{Br}(4) \\ 1 & 2 & 1 \end{array}=2 \times{ }^{8} \mathrm{C}_{2} \times 4=224 .$ | M1 | Multiply 3 combinations, ${ }^{2} \mathrm{C}_{x} \times{ }^{8} \mathrm{C}_{y} \times{ }^{4} \mathrm{C}_{z}$. Accept ${ }^{2} \mathrm{C}_{1}=2$ etc. |
|  | $\begin{array}{llll} 2 & 1 & 1 & =1 \times{ }^{8} \mathrm{C}_{1} \times 4=32 \\ 1 & 1 & 2 & =2 \times 8 \times{ }^{4} \mathrm{C}_{2}=96 \end{array}$ | A1 | 3 or more options correct unsimplified |
|  | $\begin{array}{llll} 2 & 0 & 2 & =1 \times 1 \times{ }^{4} \mathrm{C}_{2}=6 \\ 1 & 0 & 3 & =2 \times 1 \times 4=8 \end{array}$ | M1 | Summing their values of 4 or 5 legitimate scenarios (no extra scenarios) |
|  | Total $=366$ ways | A1 | Correct answer |
|  | Method 2 <br> ${ }^{14} \mathrm{C}_{4}-(2 \mathrm{~N} 2 \mathrm{R}$ or 1 N 3 R or 4 R or 3 R 1 B or 2 R 2 B or 1 R 3 B or 4 B$)$ | M1 | ${ }^{14} \mathrm{C}_{4}-k$ ' seen, $k$ an integer from an expression containing ${ }^{8} \mathrm{C}_{x}$ |
|  | $1001-\left(1 \times{ }^{8} \mathrm{C}_{2}+2 \times{ }^{8} \mathrm{C}_{3}+{ }^{8} \mathrm{C}_{4}+{ }^{8} \mathrm{C}_{3} \times 4+{ }^{8} \mathrm{C}_{2} \times{ }^{4} \mathrm{C}_{2}+8 \times 4+1\right)$ | A1 | 4 or more 'subtraction' options correct unsimplified, may be in a list |
|  | $1001-(28+112+70+224+168+32+1)$ | M1 | Their ${ }^{14} \mathrm{C}_{4}-[$ their values of 6 or more legitimate scenarios] (no extra scenarios, condone omission of final bracket) |
|  | $=366$ | A1 | Correct answer |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | Method 1 $\mathrm{P}(<11)=1-\mathrm{P}(11,12,13)$ | M1 | Binomial expression of form ${ }^{13} \mathrm{C}_{\mathrm{x}}(p)^{x}(1-p)^{13-x}, 0<x<13,0<p<1$ |
|  | $=1-{ }^{13} \mathrm{C}_{11}(0.6){ }^{11}(0.4)^{2}-{ }^{13} \mathrm{C}_{12}(0.6){ }^{12}(0.4)-(0.6){ }^{13}$ | M1 | Correct unsimplified answer |
|  | $=0.942$ | A1 | CAO |
|  | Method 2 $\mathrm{P}(<11)=\mathrm{P}(0,1,2,3,4,5,6,7,8,9,10)$ | M1 | Binomial expression of form ${ }^{13} \mathrm{C}_{\mathrm{x}}(p)^{x}(1-p)^{13-x} 0<x<13,0<p<1$ |
|  | $=(0.4){ }^{13}+{ }^{13} \mathrm{C}_{1}(0.4)^{12}(0.6)+\ldots+{ }^{13} \mathrm{C}_{10}(0.4)^{3}(0.6)^{10}$ | M1 | Correct unsimplified answer |
|  | $=0.942$ | A1 | CAO |
|  |  | 3 |  |
| 7(ii) | $\mu=130 \times 0.35=45.5$ var $=130 \times 0.35 \times 0.65=29.575$ | B1 | Correct unsimplified mean and var (condone $\left.\sigma^{2}=29.6, \sigma=5.438\right)$ |
|  | $\mathrm{P}(\geqslant 50)=\mathrm{P}\left(z>\frac{49.5-45.5}{\sqrt{29.575}}\right)=\mathrm{P}(z>0.7355)$ | M1 | Standardising, using $\pm\left(\frac{x-\text { their mean }}{\text { their } \sigma}\right), x=$ value to standardise 49.5 or 50.5 seen in $\pm$ standardisation equation |
|  | $=1-\Phi(0.7355)$ | M1 | Correct final area |
|  | $=1-0.7691$ | M1 |  |
|  | $=0.231$ | A1 | Correct final answer |
|  |  | 5 |  |


| Question | Answer | Marks |  |
| :---: | :--- | ---: | :--- |
| 7 (iii) | $1-(0.65)^{n}>0.98$ or $0.02>(0.65)^{\mathrm{n}}$ | $\mathbf{M 1}$ | Eqn or inequality involving, $0.65^{n}$ and 0.02 or $0.35^{n}$ and 0.98 |
|  | $n>9.08$ | $\mathbf{M 1}$ | Attempt to solve their eqn or inequality by logs or trial and error |
|  | $n=10$ | $\mathbf{A 1}$ | CAO |
|  |  | $\mathbf{3}$ |  |

