| Question | Answer | Marks |  |
| :---: | :--- | ---: | :--- |
| 1 | KE gain $=\frac{1}{2} \times 80 \times\left(5.5^{2}-4^{2}\right)[=570]$ | B1 | Either initial or final KE correct |
|  | WD against Res $=60 P$ | B1 |  |
|  | $\left[\frac{1}{2} \times 80 \times\left(5.5^{2}-4^{2}\right)+60 P=1200\right]$ | M1 | Four term work-energy equation |
|  | $P=10.5$ | A1 |  |
|  |  | $\mathbf{4}$ |  |


| Question | Answer | Marks |  |
| :---: | :--- | :--- | :--- |
| 2 | Driving force $\mathrm{DF}=\frac{P}{15}$ | B1 | Correct use of $P=F v$ |
|  | $[\mathrm{DF}-240000 g \sin 4-18000=240000 \times(-0.2)]$ | M1 | A four-term Newton 2nd law equation |
|  |  | A1 | Correct equation |
|  | Power is $2060000(\mathrm{~W})$ | A1 | Allow 2060 kW or 2.06 MW |
|  |  | $\mathbf{4}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3 | [ $3 \cos 60=2 \cos \theta$ ] | M1 | Attempt to resolve forces horizontally (2 terms) |
|  | $\theta=41.4$ | A1 |  |
|  | $[P=3 \sin 60+2 \sin \theta]$ | M1 | Attempt to resolve forces vertically (3 terms) |
|  | $P=3.92$ | A1 |  |
|  |  | 4 |  |
|  | First alternative method for Q3 |  |  |
|  | $\frac{P}{\sin (120-\theta)}=\frac{2}{\sin 150}=\frac{3}{\sin (90+\theta)}$ | M1 | Attempt two terms of Lami's equation which can be used to find $\theta$ |
|  | $\theta=41.4$ | A1 |  |
|  |  | M1 | Attempt an equation which can be used to find $P$ |
|  | $P=3.92$ | A1 |  |
|  | Second alternative method for Q3 |  |  |
|  | [Triangle with sides $2,3, P$ and angles opposite of $30,90-\theta, 60+\theta$ ] $\frac{P}{\sin (60+\theta)}=\frac{2}{\sin 30}=\frac{3}{\sin (90-\theta)}$ | M1 | Attempt two terms from the triangle of forces which can be used to find $\theta$ |
|  | $\theta=41.4$ | A1 |  |
|  |  | M1 | Attempt an equation which can be used to find $P$ |
|  | $P=3.92$ | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | For example $100=4 u+8 a$ or $100=\frac{1}{2}(u+v) \times 4$ or $148=4 v+8 a$ <br> or any equation in two of the variables $u, v, w, a$ | M1 | Any relevant use of constant acceleration equations in any two of the variables below <br> $a$ is acceleration <br> $u$ is speed at $A$ <br> $v$ is speed at $B$ <br> $w$ is speed at $C$ |
|  |  | A1 | One correct equation |
|  | For example $248=8 u+32 a$ or two further correct equations in 3 unknowns such as $148=4 v+8 a$ and $v=u+4 a$ or $148=\frac{1}{2}(v+w) \times 4 \text { and } 248=\frac{1}{2}(u+w) \times 8$ | A1 | A second correct equation in the same two variables or two further correct equations leading to three equations in three of the unknowns $u, v, w, a$ |
|  |  | M1 | Attempt to solve for $a$ or $u$ This must reach $a=\ldots$ or $u=\ldots$ |
|  | $a=3$ | A1 | AG |
|  | $u=19$ | B1 |  |
|  |  | 6 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(ii) | $61^{2}=19^{2}+2 \times 3 \times s$ | M1 | Attempt equation for $s=A D$ |
|  | $[s=560 \rightarrow C D=560-248]$ | M1 | Attempt to find $C D$ |
|  | Distance CD is 312 | A1 |  |
|  |  | 3 |  |
|  | Alternative method for 4(ii) |  |  |
|  | Speed at $C$ is $19+8 \times 3[=43]$ | M1 | Attempt to find speed at $C$ |
|  | $\left[61^{2}=43^{2}+2 \times 3 \times C D\right]$ | M1 | Attempt to find $C D$ |
|  | Distance CD is 312 | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5 | $R=20 g \cos 60[=100]$ | B1 |  |
|  | $F=\mu \times 20 g \cos 60[=100 \mu]$ | M1 | Use $F=\mu R$ |
|  |  | M1 | Resolve along plane in either case |
|  | $\left(P_{\text {max }}=\right) 20 g \sin 60+F$ | A1 | One correct equation |
|  | $\left(P_{\text {min }}=\right) 20 g \sin 60-F$ | A1 | Second correct equation |
|  | $20 g \sin 60+F=2(20 g \sin 60-F)$ | M1 | Use of $P_{\text {max }}=2 P_{\text {min }}$ to give four term equation in $F$ or $\mu$ or $P$ |
|  | $\mu=\frac{\sqrt{3}}{3}=0.577$ | A1 |  |
|  |  | 7 |  |
|  | Iternative solution for final 3 marks if $\boldsymbol{P}_{\text {min }}$ is taken as acting down the plane |  |  |
|  | $P_{\text {min }}=F-20 g \sin 60$ | A1 |  |
|  | $20 g \sin 60+F=2(F-20 g \sin 60)$ | M1 |  |
|  | $\mu=3 \sqrt{3}=5.196$ | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(i) |  | M1 | Attempt to integrate $a$ |
|  | $v=6 t-0.12 t^{2}(+c)$ | A1 |  |
|  | $0=6 \times 20-0.12 \times 20^{2}+c$ | DM1 | Substitute $v=0, t=20$ in an equation with arbitrary constant |
|  | $0.12 t^{2}-6 t+72=0$ | DM1 | Substitute $v=0$ and attempt to solve a 3-term quadratic |
|  | $t=30$ | A1 |  |
|  |  | 5 |  |
| 6(ii) | $s=3 t^{2}-0.04 t^{3}-72 t(+k)$ | M1 | Attempt to integrate $v$ |
|  | $s(30)-s(20)=-540-(-560)$ | DM1 | Use of limits 20 and their 30 |
|  | Distance travelled $=20$ | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | $[T=1.6 a, 2.4 g \sin 30-T=2.4 a]$ <br> System is $2.4 g \sin 30=4 a$ | M1 | Attempt Newton's 2nd law for $A$ or $B$ or for the system |
|  |  | A1 | Two correct equations |
|  |  | M1 | Solve for $a$ or $T$ |
|  | $a=3$ | A1 |  |
|  | $T=4.8$ | A1 |  |
|  |  | 5 |  |
| 7(ii) | Friction force on $A$ is $F=0.2 \times 1.6 \mathrm{~g}[=3.2]$ | B1 | From $F=\mu R$ |
|  | $\begin{aligned} & T-F=1.6 a \\ & 2.4 g \sin 30-T=2.4 a \\ & \text { System is } 2.4 g \sin 30-F=4 a \end{aligned}$ | M1 | Attempt Newton's $2^{\text {nd }}$ law for both particles or for the system |
|  |  | A1 | Correct equations for $A$ and $B$ or correct system equation |
|  |  | M1 | Attempt to solve for $a$ |
|  | $a=2.2$ | A1 |  |
|  | $v^{2}=2 \times 2.2 \times 1$ | M1 | Attempt to find $v$ or $v^{2}$ when $B$ reaches the barrier |
|  | Subsequent acceleration of $A$ is -2 | B1 |  |
|  | $4.4=2 \times 2 \times s$ | M1 | Attempt to find distance $A$ travels while decelerating to $v=0$ |
|  | Total distance travelled is 2.1 m | A1 |  |
|  |  | 9 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(ii) | Alternative method for Q7 [Work-Energy applied to $\boldsymbol{A}$ and $\boldsymbol{B}$ ] |  |  |
|  | $F=0.2 \times 1.6 \mathrm{~g}[=3.2]$ | B1 | From $F=\mu R=0.2 \times 1.6 \mathrm{~g}=3.2$ |
|  |  | M1 | Attempt PE loss as $B$ reaches the barrier |
|  | PE loss $=2.4 g \sin 30[=12]$ | A1 |  |
|  |  | M1 | Attempt KE gain for both $A$ and $B$ |
|  | $\text { KE gain }=\frac{1}{2}(1.6+2.4) v^{2}\left[=2 v^{2}\right]$ | A1 |  |
|  | $\begin{aligned} & {\left[2.4 g \sin 30=\frac{1}{2} \times 4 \times v^{2}+3.2 \times 1\right]} \\ & {\left[v^{2}=4.4\right]} \end{aligned}$ | M1 | Apply work-energy equation for the motion until $B$ reaches the barrier (Three relevant terms) |
|  | KE loss $=\frac{1}{2} \times 1.6 \times 4.4$ | B1 | Find KE loss as $A$ comes to rest after $B$ has stopped |
|  | $\left[\frac{1}{2} \times 1.6 \times 4.4=3.2 d\right]$ $[d=1.1]$ | M1 | Apply work-energy equation where $d$ is the extra distance travelled by $A$ leading to a positive value for $d$ |
|  | Total distance $=2.1 \mathrm{~m}$ | A1 | Distance $=d+1$ |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(ii) | Alternative scheme for first 6 marks of 7(ii) [Work-energy applied to $A$ ] |  |  |
|  | Friction $=0.2 \times 1.6 \mathrm{~g}[=3.2]$ | B1 |  |
|  | $\begin{aligned} & {[2.4 g \sin 30-T=2.4 a} \\ & T-F=1.6 a] \end{aligned}$ | M1 | Apply Newton's 2nd law to $A$ and $B$ and solve for $T$ |
|  | $T=6.72$ | A1 |  |
|  | $\left[\frac{1}{2} \times 1.6 \times v^{2}\right]$ | M1 | Attempt KE for $A$ only |
|  |  | A1 | Correct KE for $A$ |
|  | $\left[6.72 \times 1=\frac{1}{2} \times 1.6 \times v^{2}+3.2 \times 1\right]$ | M1 | Use work/energy equation for $A$ |
|  | Alternative scheme for first 6 marks of 7(ii) [Work-energy applied to B] |  |  |
|  | Friction $=0.2 \times 1.6 \mathrm{~g}$ [=3.2] | B1 |  |
|  | $\begin{aligned} & {[2.4 g \sin 30-T=2.4 a} \\ & T-F=1.6 a] \end{aligned}$ | M1 | Apply Newton's 2nd law to $A$ and $B$ and solve for $T$ |
|  | $T=6.72$ | A1 |  |
|  |  | M1 | Find energy loss/gain for $B$ Allow either term |
|  | $\pm\left(\frac{1}{2} \times 2.4 \times v^{2}-2.4 g \sin 30\right)$ | A1 |  |
|  | $2.4 g \sin 30=\frac{1}{2} \times 2.4 \times v^{2}+6.72 \times 1$ | M1 | Use work/energy equation for $B$ |

