| Question | Answer | Marks | Guidance |
| :---: | :--- | :--- | :--- |
| 1 | Attempt to solve quadratic equation in $\mathrm{e}^{x}$ | $\mathbf{M 1}$ | Either directly or using substitution $u=\mathrm{e}^{x}$ |
|  | Obtain $\mathrm{e}^{x}=\frac{1}{3}, \quad \mathrm{e}^{x}=27$ | $\mathbf{A 1}$ | $\mathrm{e}^{x}=\frac{1}{3}, \quad \mathrm{e}^{x}=27$ may be implied if $u=\mathrm{e}^{x}$ is stated |
|  | Use correct process at least once for solving $\mathrm{e}^{x}=c$ where $c>0$ | $\mathbf{M 1}$ |  |
|  | Obtain $-\ln 3$ from a correct solution | $\mathbf{A 1}$ | Condone use of $x=\mathrm{e}^{x}$ |
|  | Obtain $3 \ln 3$ from a correct solution | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2 | Either |  |  |
|  | State or imply equation $\ln y=\ln A+\ln B \ln x$ | B1 |  |
|  | Equate gradient of line to $\ln B$ | M1 |  |
|  | Obtain $\ln B=1.6486 \ldots$ and hence $B=5.2$ | A1 |  |
|  | Substitute appropriate values to find $\ln A$ | M1 |  |
|  | Obtain $\ln A=1.2809 \ldots$ and hence $A=3.6$ | A1 |  |
|  | Or |  |  |
|  | State or imply equation $\ln y=\ln A+\ln B \ln x$ | B1 |  |
|  | Use given coordinates to obtain a correct equation | B1 | Equations are $4.908=\ln A+2.2 \ln B$ and $11.008=\ln A+5.9 \ln B$ |
|  | Use given coordinates to obtain a second correct equation and attempt to solve both equations simultaneously to obtain at least one of the unknowns $\ln A$ or $\ln B$ | M1 |  |
|  | Obtain $\ln B=1.6486 \ldots$ and hence $B=5.2$ | A1 |  |
|  | Obtain $\ln A=1.2809 \ldots$ and hence $A=3.6$ | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2 | Or |  |  |
|  | Use given coordinates to obtain a correct equation | B1 | Equations are $\mathrm{e}^{4.908}=A B^{2.2}$ and $\mathrm{e}^{11.008}=A B^{5.9}$ |
|  | Use given coordinates to obtain a second correct equation | B1 |  |
|  | Solve to obtain B | M1 | M mark dependent on both previous B marks |
|  | $B=5.2$ | A1 |  |
|  | $A=3.6$ | A1 |  |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | :--- | :--- |
| 3 | Rewrite integrand as $4 \mathrm{e}^{2 x}+4 \mathrm{e}^{-x}$ | B1 |  |
|  | Integrate to obtain form $k_{1} \mathrm{e}^{2 x}+k_{2} \mathrm{e}^{-x}$ where $k_{1} \neq 4, k_{2} \neq 4$ | M1 |  |
|  | Obtain correct $2 \mathrm{e}^{2 x}-4 \mathrm{e}^{-x}$ | A1 |  |
|  | Apply limits correctly, retaining exactness | M1 | Dependent on previous M1 |
|  | Obtain $2 \mathrm{e}^{4}-4 \mathrm{e}^{-2}+2$ or exact similarly simplified equivalent | A1 |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | Use quotient rule or equivalent | M1 | Obtaining two terms in numerator and $(2 x+1)^{2}$ in denominator for a quotient |
|  | Obtain correct $\frac{\frac{5}{x}(2 x+1)-10 \ln x}{(2 x+1)^{2}}$ or equivalent, or $\frac{5}{x}(2 x+1)^{-1}-10 \ln x(2 x+1)^{-2}$ or equivalent | A1 | Obtaining one term with $(2 x+1)^{-1}$ oe and a second term with $(2 x+1)^{-2}$ oe for a product <br> Condone poor use of brackets if recovered later |
|  | Substitute $x=1$ to obtain $\frac{15}{9}$ or $\frac{5}{3}$ or equivalent, www | A1 |  |
|  |  | 3 |  |
| 4(ii) | Equate numerator to zero and attempt relevant arrangement | M1 | For M1, need to see at least one line of working after either $10+\frac{5}{x}-10 \ln x=0$ or their numerator (which must have at least 2 terms, one involving $\ln x)=0$ |
|  | Confirm $x=\frac{x+0.5}{\ln x}$ | A1 | AG; necessary detail needed |
|  |  | 2 |  |
| 4(iii) | Use iteration process correctly at least once | M1 |  |
|  | Obtain final answer 3.181 | A1 |  |
|  | Show sufficient iterations to 6 sf to justify answer or show sign change in interval (3.1805, 3.1815) | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | :--- | :--- |
| $5(\mathrm{i})$ | Obtain $\frac{\mathrm{d} x}{\mathrm{~d} \theta}=-4 \sin 2 \theta+3 \cos \theta$ | B1 | B1 may be implied |
|  | Use $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{\mathrm{d} y}{\mathrm{~d} \theta} / \frac{\mathrm{d} x}{\mathrm{~d} \theta}$ in terms of $\theta$ or with 1 already substituted | M1 |  |
|  | Obtain or imply $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{-3 \sin \theta}{-4 \sin 2 \theta+3 \cos \theta}$ | A1 |  |
|  | Substitute 1 to obtain 1.25 | A1 | Or greater accuracy $1.252013 \ldots$ |
|  | Equate denominator of first derivative to zero | $\mathbf{4}$ |  |
|  | Use $\sin 2 \theta=2 \sin \theta \cos \theta$ | M1 |  |
|  | Obtain $\sin \theta=\frac{3}{8}$ | A1 |  |




| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | State $R=\sqrt{29}$ or $5.385 \ldots$ | B1 |  |
|  | Use appropriate trigonometry to find $\alpha$ | M1 | Allow M1 for $\tan \alpha= \pm \frac{2}{5}$ or $\pm \frac{5}{2}$ oe |
|  | Obtain 0.3805 with no errors seen | A1 | Or greater accuracy 0.3805063... |
|  |  | 3 |  |
| 7(ii) | State that equation is $5 \cos \theta-2 \sin \theta=4$ | B1 |  |
|  | Evaluate $\cos ^{-1}(k / R)-\alpha$ to find one value of $\theta$ | M1 | Allow M1 from their $\sqrt{29} \cos (\theta \pm \alpha)$ |
|  | Obtain 0.353 | A1 | Or greater accuracy 0.35307... |
|  | Carry out correct method to find second value | M1 |  |
|  | Obtain 5.17 and no extra solutions in the range | A1 | Or greater accuracy 5.16909... <br> If working consistently in degrees, then no A marks are available, B1, M1, M1 max |
|  |  | 5 |  |
| 7(iii) | State integrand as $\frac{1}{29} \sec ^{2}\left(\frac{1}{2} x+0.3805\right)$ | B1 FT | Following their answer from part (i), must be in the form $R \cos (\theta \pm \alpha)$ |
|  | Integrate to obtain form $k \tan \left(\frac{1}{2} x+\right.$ their $\left.\alpha\right)$ | M1 |  |
|  | Obtain $\frac{2}{29} \tan \left(\frac{1}{2} x+0.3805\right)+c$ | A1 |  |
|  |  | 3 |  |

