| Question | Answer |  | Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 573, 43 (or 043), 289 |  | B1B1B1 | Ignore incorrect numbers. But allow other correct use of table (i.e. $573,650,431$ ) |
|  |  | Total: | 3 |  |
| 2(i) | $z=1.751$ |  | B1 |  |
|  | $\frac{103}{200} \pm z \sqrt{\frac{\frac{103}{200} \times\left(1-\frac{103}{200}\right)}{200}} \mathrm{oe}$ |  | M1 | all correct except for recognisable value of $z$, allow for one side only |
|  | $=0.453$ to $0.577(3 \mathrm{sf})$ as final answer |  | A1 | must be an interval |
|  | Total: |  | 3 |  |
| 2(ii) | 0.08 oe 8\%, 8/100 |  | B1 |  |
| 3 | $10 \times 0.46^{2}(=2.116) \text { or } \frac{0.46}{\sqrt{10}}$ |  | B1 | SOI |
|  | Total mass of ore $\sim \mathrm{N}(70,2.116)$ or$\sim \mathrm{N}\left(7,\left(\frac{0.46}{\sqrt{10}}\right)^{2}\right)$ |  | B1 |  |
|  | $\pm \frac{71-" 70 "}{\sqrt{" 2.116^{"}}} \text { or } \pm \frac{7.1-" 7.0 "}{0.46 / \sqrt{10}}(=0.687)$ |  | M1 | correct, using their sd or $\sqrt{ }$ (their var) e.g. allow $\frac{71-" 70 "}{4.6}$ for M1 |
|  | 1 - $\phi$ ("0.687") |  | M1 | for correct area consistent with their working |
|  | $=0.246(3 \mathrm{sf})$ |  | A1 |  |
|  | Total: |  | 5 |  |


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| 4(i) | $\bar{x}=6.7 / 200(=67 / 2000=0.0335)$ | B1 |  |
|  | $\mathrm{s}^{2}=\frac{200}{199} \times\left(\frac{0.2312}{200}-" 0.0335{ }^{\prime \prime}\right)$ | M1 | $\begin{equation*} \mathrm{s}^{2}=\frac{0.2312}{200}-0.0335^{2} \tag{M0} \end{equation*}$ |
|  | $=0.0000339(2)=27 / 796000$ | A1 | $=0.00003375$ A0 |
|  | Total: | 3 |  |
| 4(ii) | $\mathrm{H}_{0}$ : Pop mean level $=0.034$ <br> $\mathrm{H}_{1}$ : Pop mean level $\neq 0.034$ | B1 | not just "mean", but allow just " $\mu$ " |
|  | $\frac{\text { "030335"-0.034 }}{\frac{\sqrt{" 0.00003392 "}}{\sqrt{200}}}$ | M1 | must have $\sqrt{200}$ <br> $\frac{0.0335-0.034}{\frac{\sqrt{00.00033755^{\prime}}}{\sqrt{200}}}$ <br> M1 |
|  | $=-1.21(4)(3 \mathrm{sfs})(-1.22 \leftrightarrow-1.21)$ | A1 | $=-1.217$ (3 sfs) A1 |
|  | Comp with $z=-1.645$ (or $0.1124>0.05$ ) | M1 | $0.112>0.05$ <br> valid comparison $z$ or areas |
|  | No evidence that (mean) pollutant level has changed, accept $\mathrm{H}_{0}$ (if correctly defined) | A1FT | correct conclusion no contradictions <br> SR: One tail test: B0, M1A1 as normal, M1 (comparison with 1.282 consistent signs) A0 |
|  | Total: | 5 |  |


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| 5(i)(a) | $X \sim \mathrm{~N}(42,42)$ |  | B1 | stated or implied |
|  | $\frac{39.5-" 42 "}{\sqrt{" 42 "}}(=-0.386)$ |  | M1 | allow with wrong or no cc |
|  | $1-\phi$ ("-0.386") = $\phi$ ("0.386") |  | M1 | correct area consistent with their working |
|  | $=0.65(0)(3 \mathrm{sf})$ |  | A1 |  |
|  |  | Total: | 4 |  |
| 5(i)(b) | $42>$ (e.g. 15) or mean is large |  | B1 | $\lambda>15$ or higher, $\lambda=$ large ignore subsequent work if not undermining what already written |
|  |  | Total: | 1 |  |
| 5(ii)(a) | $Y \sim \operatorname{Po}(1.2)$ |  | B1 | stated or implied |
|  | $1-\mathrm{e}^{-1.2}\left(1+1.2+\frac{1.2^{2}}{2}\right)$ |  | M1 | allow any $\lambda$ allow one end error |
|  | $=0.121(3 \mathrm{sf})$ |  | A1 | Using binomial: 0.119 SR B1 |
|  |  | Total: | 3 |  |
| 5(ii)(b) | $60 \times 0.02=1.2<5$ or mean is small |  | B1FT | or large $n$ small $p$ <br> FT Poisson only |
|  |  | Total: | 1 |  |


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| 6 (i) | $k \int_{0}^{1}\left(x-x^{2}\right) \mathrm{d} x=1$ |  | M1 | Attempt integ $\mathrm{f}(x)$ and " $=1$ ", ignore limits |
|  | $=k\left[\frac{x^{2}}{2}-\frac{x^{3}}{3}\right]_{0}^{1}=1$ |  | A1 | correct integration, limits 0 and 1 |
|  | $=k\left[\begin{array}{ll}\frac{1}{2} & -\frac{1}{3}\end{array}\right]=1$ or $\frac{k}{6}=1$ |  | A1 | correctly obtained, no errors seen |
|  |  | Total: | 3 |  |
| 6(ii) | $\mathrm{E}(X)=0.5$ |  | B1 |  |
|  | $6 \int_{0}^{1}\left(x^{3}-x^{4}\right) d x$ |  | M1 | Attempt integ $x^{2} \mathrm{f}(x)$, limits 0 to 1 |
|  | $\begin{aligned} & \left(=6\left[\frac{1}{4}-\frac{1}{5}\right]=0.3\right) \\ & " 0.3 "-" 0.5 "^{2} \end{aligned}$ |  | M1 | their int $x^{2} \mathrm{f}(x)$ - their $(\mathrm{E}(X))^{2}$ dep + ve result |
|  | $=0.05(=1 / 20)$ |  | A1 |  |
|  |  | Total: | 4 |  |
| 6(iii) | $6 \int_{0.4}^{1}\left(x-x^{2}\right) \mathrm{d} x$ |  | M1 | ignore limits, eg M1 for $6 \int_{0.4}^{2}\left(x-x^{2}\right) \mathrm{d} x$ |
|  | $=6\left\{\frac{1}{2}-\frac{1}{3}-\left(\frac{0.4^{2}}{2}-\frac{0.4}{3}\right)\right\}$ |  | A1FT | subst correct limits into correct integration |
|  | $=0.648(=81 / 125)$ |  | A1 | condone incorrect " k " for A1 |
|  |  | Total: | 3 |  |


| Question | Answer | Marks | Guidance |
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| 7(i) | $\mathrm{H}_{0}$ : Pop mean no. accidents $=5.64$ <br> $\mathrm{H}_{1}$ : Pop mean no. accidents $<5.64$ | B1 | or " $=0.47$ (per month)" not just "mean", but allow just " $\lambda$ " or " $\mu$ " |
|  | Use of $\lambda=5.64$ | B1 | used in a Poisson calculation |
|  | $=\mathrm{e}^{-5.64}\left(1+5.64+\frac{5.64{ }^{2}}{2}\right)$ | M1 | Allow incorrect $\lambda$ in otherwise correct |
|  | $=0.08(0)$ | A1 |  |
|  | Comp with 0.05 | M1 | Valid comparison (Poisson only), no contradictions. |
|  | No evidence to believe mean no. of accidents has decreased; accept $\mathrm{H}_{0}$ (if correctly defined) | A1FT | Normal distribution: M0M0 |
|  | Total: | 6 |  |
| 7(ii) | Mean $<0.47$ but conclude that this is not so | B1 | (Mean) no. of accidents reduced, but conclude not reduced. Must be in context. |
|  | Total: | 1 |  |
| 7(iii) | (Need greatest $x$ such that $\mathrm{P}(X \leqslant x)<0.05$ ) $\begin{aligned} & \mathrm{P}(X \leqslant 1)=\mathrm{e}^{-5.64}(1+5.64)=0.024 \\ & \mathrm{P}(X \leqslant 2)=0.08 \end{aligned}$ | B1 | Both, could be seen in (i) |
|  | Hence rejection region is $X \leqslant 1$ | B1 | Can be implied |
|  | $\begin{aligned} & \text { With } \lambda=12 \times 0.05=0.6 \\ & 1-\mathrm{P}(X \leqslant 1)=1-\mathrm{e}^{-0.6}(1+0.6) \end{aligned}$ | M1 | $\lambda=0.6$ and $1-\mathrm{P}(X \leqslant 1)$ |
|  | $=0.122(3 \mathrm{sf})$ | A1 | Normal scores 0 |
|  | Total: | 4 |  |

