| Question | Answer | Marks |
| :---: | :---: | :---: |
| 1 | Express the LHS in terms of either $\cos \mathrm{x}$ and $\sin \mathrm{x}$ or in terms of $\tan \mathrm{x}$ | B1 |
|  | Use Pythagoras | M1 |
|  | Obtain the given answer | A1 |
|  | Total: | 3 |
| 2 | EITHER: <br> State a correct unsimplified version of the $x$ or $x^{2}$ term in the expansion of $\left(1+\frac{2}{3} x\right)^{-3}$ or $(3+2 x)^{-3}$ <br> [Symbolic binomial coefficients, e.g. $\binom{-3}{2}$, are not sufficient for M1.] | (M1 |
|  | State correct first term $\frac{1}{27}$ | B1 |
|  | Obtain term $-\frac{2}{27} x$ | A1 |
|  | Obtain term $\frac{8}{81} x^{2}$ | A1) |
|  | OR: <br> Differentiate expression and evaluate $\mathrm{f}(0)$ and $\mathrm{f}^{\prime}(0)$, where $\mathrm{f}^{\prime}(x)=k(3+2 x)^{-4}$ | (M1 |
|  | State correct first term $\frac{1}{27}$ | B1 |
|  | Obtain term $-\frac{2}{27} x$ | A1 |
|  | Obtain term $\frac{8}{81} x^{2}$ | A1) |
|  | Total: | 4 |
| 3 | Rearrange as $3 u^{2}+4 u-4=0$, or $3 \mathrm{e}^{2 x}+4 \mathrm{e}^{x}-4=0$, or equivalent | B1 |
|  | Solve a 3-term quadratic for $\mathrm{e}^{x}$ or for $u$ | M1 |
|  | Obtain $\mathrm{e}^{x}=\frac{2}{3}$ or $u=\frac{2}{3}$ | A1 |
|  | Obtain answer $x=-0.405$ and no other | A1 |
|  | Total: | 4 |


| Question | Answer | Marks |
| :---: | :---: | :---: |
| 4 | Integrate by parts and reach $a \theta \cos \frac{1}{2} \theta+b \int \cos \frac{1}{2} \theta \mathrm{~d} \theta$ | *M1 |
|  | Complete integration and obtain indefinite integral $-2 \theta \cos \frac{1}{2} \theta+4 \sin \frac{1}{2} \theta$ | A1 |
|  | Substitute limits correctly, having integrated twice | DM1 |
|  | Obtain final answer $(4-\pi) / \sqrt{2}$, or exact equivalent | A1 |
|  | Total: | 4 |
| 5(i) | Use the chain rule | M1 |
|  | Obtain correct derivative in any form | A1 |
|  | Use correct trigonometry to express derivative in terms of $\tan x$ | M1 |
|  | Obtain $\frac{\mathrm{d} y}{\mathrm{~d} x}=-\frac{4 \tan x}{4+\tan ^{2} x}$, or equivalent | A1 |
|  | Total: | 4 |
| 5(ii) | Equate derivative to -1 and solve a 3-term quadratic for $\tan x$ | M1 |
|  | Obtain answer $x=1.11$ and no other in the given interval | A1 |
|  | Total: | 2 |
| 6(i) | Calculate the value of a relevant expression or expressions at $x=2.5$ and at another relevant value, e.g. $x=3$ | M1 |
|  | Complete the argument correctly with correct calculated values | A1 |
|  | Total: | 2 |
| 6(ii) | State a suitable equation, e.g. $x=\pi+\tan ^{-1}(1 /(1-x))$ without suffices | B1 |
|  | Rearrange this as $\cot x=1-x$, or commence working vice versa | B1 |
|  | Total: | 2 |
| 6(iii) | Use the iterative formula correctly at least once | M1 |
|  | Obtain final answer 2.576 only | A1 |
|  | Show sufficient iterations to 5 d.p. to justify 2.576 to 3 d.p., or show there is a sign change in the interval $(2.5755,2.5765)$ | A1 |
|  | Total: | 3 |


| Question | Answer | Marks |
| :---: | :---: | :---: |
| 7(i) | Use correct quotient rule or product rule | M1 |
|  | Obtain correct derivative in any form | A1 |
|  | Equate derivative to zero and solve for $x$ | M1 |
|  | Obtain $x=2$ | A1 |
|  | Total: | 4 |
| 7(ii) | State or imply ordinates $1.6487 \ldots, 1.3591 \ldots, 1.4938 \ldots$ | B1 |
|  | Use correct formula, or equivalent, with $h=1$ and three ordinates | M1 |
|  | Obtain answer 2.93 only | A1 |
|  | Total: | 3 |
| 7(iii) | Explain why the estimate would be less than $E$ | B1 |
|  | Total: | 1 |
| 8(i) | Justify the given differential equation | B1 |
|  | Total: | 1 |
| 8(ii) | Separate variables correctly and attempt to integrate one side | B1 |
|  | Obtain term $k t$, or equivalent | B1 |
|  | Obtain term $-\ln (50-x)$, or equivalent | B1 |
|  | Evaluate a constant, or use limits $x=0, t=0$ in a solution containing terms $a \ln (50-x)$ and $b t$ | M1* |
|  | Obtain solution $-\ln (50-x)=k t-\ln 50$, or equivalent | A1 |
|  | Use $x=25, t=10$ to determine $k$ | DM1 |
|  | Obtain correct solution in any form, e.g. $\ln 50-\ln (50-x)=\frac{1}{10}(\ln 2) t$ | A1 |
|  | Obtain answer $x=50(1-\exp (-0.0693 t))$, or equivalent | A1 |
|  | Total: | 8 |


| Question | Answer | Marks |
| :---: | :---: | :---: |
| 9(i) | State or imply the form $\frac{A}{x}+\frac{B}{x^{2}}+\frac{C}{3 x+2}$ | B1 |
|  | Use a relevant method to determine a constant | M1 |
|  | Obtain one of the values $A=3, B=-2, C=-6$ | A1 |
|  | Obtain a second value | A1 |
|  | Obtain the third value <br> [Mark the form $\frac{A x+B}{x^{2}}+\frac{C}{3 x+2}$ using same pattern of marks.] | A1 |
|  | Total: | 5 |
| 9(ii) | Integrate and obtain terms $3 \ln x=\frac{2}{x}-2 \ln (3 x+2)$ <br> [The FT is on $A, B$ and $C$ ] <br> Note: Candidates who integrate the partial fraction $\frac{3 x-2}{x^{2}}$ by parts should obtain $3 \ln x+\frac{2}{x}-3$ or equivalent | B3 FT |
|  | Use limits correctly, having integrated all the partial fractions, in a solution containing terms $a \ln x+\frac{b}{x}+c \ln (3 x+2)$ | M1 |
|  | Obtain the given answer following full and exact working | A1 |
|  | Total: | 5 |
| 10(i) | Carry out a correct method for finding a vector equation for $A B$ | M1 |
|  | Obtain $\mathbf{r}=\mathbf{i}-2 \mathbf{j}+2 \mathbf{k}+\lambda(2 \mathbf{i}+3 \mathbf{j}-\mathbf{k})$, or equivalent | A1 |
|  | Equate two pairs of components of general points on $A B$ and $l$ and solve for $\lambda$ or for $\mu$ | M1 |
|  | Obtain correct answer for $\lambda$ or $\mu$, e.g. $\lambda=\frac{5}{7}$ or $\mu=\frac{3}{7}$ | A1 |
|  | Obtain $m=3$ | A1 |
|  | Total: | 5 |


| Question | Answer | Marks |
| :---: | :---: | :---: |
| 10(ii) | EITHER: <br> Use scalar product to obtain an equation in $\mathrm{a}, \mathrm{b}$ and c , e.g. $a-2 b-4 c=0$ | (B1 |
|  | Form a second relevant equation, e.g. $2 a+3 b-c=0$ and solve for one ratio, e.g. $a$ : $b$ | M1 |
|  | Obtain final answer $a: b: c=14:-7: 7$ | A1 |
|  | Use coordinates of a relevant point and values of $a, b$ and $c$ and find $d$ | M1 |
|  | Obtain answer $14 x-7 y+7 z=42$, or equivalent | A1) |
|  | OR 1: <br> Attempt to calculate the vector product of relevant vectors, e.g. $(\mathbf{i}-2 \mathbf{j}-4 \mathbf{k}) \times(2 \mathbf{i}+3 \mathbf{j}-\mathbf{k})$ | (M1 |
|  | Obtain two correct components | A1 |
|  | Obtain correct answer, e.g. 14i-7j $+7 \mathbf{k}$ | A1 |
|  | Substitute coordinates of a relevant point in $14 x-7 y+7 z=d$, or equivalent, and find $d$ | M1 |
|  | Obtain answer $14 x-7 y+7 z=42$, or equivalent | A1) |
|  | OR 2: <br> Using a relevant point and relevant vectors, form a 2 -parameter equation for the plane | (M1 |
|  | State a correct equation, e.g. $\mathbf{r}=\mathbf{i}-2 \mathbf{j}+2 \mathbf{k}+s(\mathbf{i}-2 \mathbf{j}-4 \mathbf{k})+t(2 \mathbf{i}+3 \mathbf{j}-\mathbf{k})$ | A1 |
|  | State 3 correct equations in $x, y, z, s$ and $t$ | A1 |
|  | Eliminate $s$ and $t$ | M1 |
|  | Obtain answer $2 x-y+z=6$, or equivalent | A1) |
|  | OR 3: <br> Using a relevant point and relevant vectors, form a determinant equation for the plane | (M1 |
|  | State a correct equation, e.g. $\left\|\begin{array}{rrr}x-1 & y+2 & z-1 \\ 1 & -2 & -4 \\ 2 & 3 & -1\end{array}\right\|=0$ | A1 |
|  | Attempt to expand the determinant | M1 |
|  | Obtain or imply two correct cofactors | A1 |
|  | Obtain answer $14 x-7 y+7 z=42$, or equivalent | A1) |
|  | Total: | 5 |


| Question | Answer | Marks |
| :---: | :---: | :---: |
| 11(a) | Solve for $z$ or for $w$ | M1 |
|  | Use $\mathrm{i}^{2}=-1$ | M1 |
|  | Obtain $w=\frac{\mathrm{i}}{2-\mathrm{i}}$ or $z=\frac{2+\mathrm{i}}{2-\mathrm{i}}$ | A1 |
|  | Multiply numerator and denominator by the conjugate of the denominator | M1 |
|  | Obtain $w=-\frac{1}{5}+\frac{2}{5} \mathrm{i}$ | A1 |
|  | Obtain $z=\frac{3}{5}+\frac{4}{5} \mathrm{i}$ | A1 |
|  | Total: | 6 |
| 11(b) | EITHER: <br> Find $\pm[2+(2-2 \sqrt{3}) \mathrm{i}]$ | (B1 |
|  | Multiply by 2 i (or -2 i ) | M1* |
|  | Add result to $v$ | DM1 |
|  | Obtain answer $4 \sqrt{3}-1+6 \mathrm{i}$ | A1) |
|  | OR: State $\frac{z-v}{v-u}=k$ i, or equivalent | (M1 |
|  | State $k=2$ | A1 |
|  | Substitute and solve for $z$ even if i omitted | M1 |
|  | Obtain answer $4 \sqrt{3}-1+6 \mathrm{i}$ | A1) |
|  | Total: | 4 |

