| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1 | State or imply non-modulus equation $(x+a)^{2}=(2 x-5 a)^{2}$ or pair of linear equations | B1 | SR B1 for $x=6 a$ |
|  | Attempt solution of quadratic equation or of pair of linear equations | M1 | Allow M1 if $\frac{4}{3}$ and 6 seen |
|  | Obtain, as final answers, $6 a$ and $\frac{4}{3} a$ | A1 |  |
|  | Total: | 3 |  |
| 2 | Apply logarithms to both sides and apply power law | *M1 |  |
|  | Obtain $(x+4) \log 3=2 x \log 5$ or equivalent | A1 |  |
|  | Solve linear equation for $x$ | DM1 | dep *M |
|  | Obtain 2.07 | A1 | Allow greater accuracy |
|  | Total: | 4 |  |
| 3(i) | Draw sketch of $y=x^{3}$ | *B1 | May be implied by part graph in first quadrant |
|  | Draw straight line with negative gradient crossing positive $y$-axis and indicate one intersection | DB1 | dep *B |
|  | Total: | 2 |  |
| 3(ii) | Use iterative formula correctly at least once | M1 |  |
|  | Obtain final answer 1.926 | A1 |  |
|  | Show sufficient iterations to justify 4 sf or show sign change in interval (1.9255,1.9265) | A1 |  |
|  | Total: | 3 |  |


| Question | Answer | Marks | Guidance |
| :--- | :--- | ---: | ---: |
| 4 | Use quotient rule (or product rule) to find first derivative | M1 |  |
|  | Obtain $\frac{8 x \mathrm{e}^{4 x}+10 \mathrm{e}^{4 x}}{(2 x+3)^{2}}$ or equivalent | A1 |  |
|  | Substitute $x=0$ to obtain gradient $\frac{10}{9}$ | A1 |  |
|  | Form equation of tangent through $\left(0, \frac{1}{3}\right)$ with numerical gradient | M1 |  |
|  | Obtain $10 x-9 y+3=0$ | A1 |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5 | State or imply $\ln y=\ln K-2 x \ln a$ | B1 |  |
|  | EITHER: |  |  |
|  | Obtain -0.525 as gradient of line | (M1 |  |
|  | Equate their $-2 \ln a$ to their gradient and solve for $a$ | M1 | Allow $2 \ln a=$ their gradient for M1 |
|  | Obtain $a=1.3$ | A1 |  |
|  | Substitute to find value of $K$ | M1 |  |
|  | Obtain $K=8.4$ | A1) |  |
|  | OR: |  |  |
|  | Obtain two equations using coordinates correctly | (M1 |  |
|  | Solve these equations to obtain $2 \ln a$ or equivalent | M1 |  |
|  | Obtain $a=1.3$ | A1 |  |
|  | Substitute to find value of $K$ | M1 |  |
|  | Obtain $K=8.4$ | A1) |  |
|  |  | 6 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(i) | Evaluate expression when $x=-2$ | M1 |  |
|  | Obtain 0 with all necessary detail present | A1 | Use of $\mathrm{f}(x)=(x+2)\left(a x^{2}+b x+c\right)$ to find $a, b$ and $c$, allow M1 A0 Use of $\mathrm{f}(x)=(x+2)\left(a x^{2}+b x+c\right)+d$ to find $a, b$ and $c$, and show $d=0$, allow M1 A1 |
|  | Carry out division, or equivalent, at least as far as $x^{2}$ and $x$ terms in quotient | M1 |  |
|  | Obtain $6 x^{2}+x-35$ | A1 |  |
|  | Obtain factorised expression $(x+2)(2 x+5)(3 x-7)$ | A1 |  |
|  | Total: | 5 |  |
| 6(ii) | State or imply substitution $x=\frac{1}{y}$ or equivalent | M1 |  |
|  | Obtain $-\frac{1}{2},-\frac{2}{5}, \frac{3}{7}$ | A1 |  |
|  | Total: | 2 |  |
| 7(a) | Obtain $\int\left(2 \cos ^{2} \theta-\cos \theta-3\right) \mathrm{d} \theta$ | B1 |  |
|  | Attempt use of identity to obtain integrand involving $\cos 2 \theta$ and $\cos \theta$ | M1 |  |
|  | Integrate to obtain form $k_{1} \sin 2 \theta+k_{2} \sin \theta+k_{3} \theta$ for non-zero constants | M1 |  |
|  | Obtain $\frac{1}{2} \sin 2 \theta-\sin \theta-2 \theta+c$ | A1 |  |
|  | Total: | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(b)(i) | Integrate to obtain form $k_{1} \ln (2 x+1)+k_{2} \ln (x)$ or $k_{1} \ln (2 x+1)+k_{2} \ln (2 x)$ | M1 |  |
|  | Obtain $2 \ln (2 x+1)+\frac{1}{2} \ln x$ or $2 \ln (2 x+1)+\frac{1}{2} \ln (2 x)$ | A1 |  |
|  | Total: | 2 |  |
| 7(b)(ii) | Use relevant logarithm power law for expression obtained from application of limits | M1 |  |
|  | Use relevant logarithm addition / subtraction laws | M1 |  |
|  | Obtain $\ln 18$ | A1 |  |
|  | Total: | 3 |  |
| 8(i) | Obtain $\frac{\mathrm{d} x}{\mathrm{~d} t}=2 \sin 2 t$ | B1 |  |
|  | Obtain $\frac{\mathrm{d} y}{\mathrm{~d} t}=6 \sin ^{2} t \cos t-9 \cos ^{2} t \sin t$ | B1 |  |
|  | Use $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{\mathrm{d} y}{\mathrm{~d} t} / \frac{\mathrm{d} x}{\mathrm{~d} t}$ for their first derivatives | M1 |  |
|  | Use identity $\sin 2 t=2 \sin t \cos t$ | B1 |  |
|  | Simplify to obtain $\frac{3}{2} \sin t-\frac{9}{4} \cos t$ with necessary detail present | A1 |  |
|  | Total: | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 8(ii) | Equate $\frac{\mathrm{d} y}{\mathrm{~d} x}$ to zero and obtain $\tan t=k$ | M1 |  |
|  | Obtain $\tan t=\frac{3}{2}$ or equivalent | A1 |  |
|  | Substitute value of $t$ to obtain coordinates (2.38, 2.66) | A1 |  |
|  | Total: | 3 |  |
| 8(iii) | Identify $t=\frac{1}{4} \pi$ | B1 |  |
|  | Substitute to obtain exact value for gradient of the normal | M1 |  |
|  | Obtain gradient $\frac{4}{3} \sqrt{2}, \frac{8}{3 \sqrt{2}}$ or similarly simplified exact equivalent | A1 |  |
|  | Total: | 3 |  |

