| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1 | Take logarithms of both sides and apply power law to both sides | M1 | Allow $y=\frac{\log 5}{4 \log 3}$ for M1 A1 |
|  | Rearrange to the form $y=\frac{\ln 5}{4 \ln 3} x$ or equivalent | A1 |  |
|  | Obtain $m=0.366$ | A1 |  |
|  | Total: | 3 |  |
| 2 | State or imply non-modulus inequality $(4-x)^{2} \leqslant(3-2 x)^{2}$ or corresponding equation, pair of linear equations or linear inequalities | M1 |  |
|  | Attempt solution of 3-term quadratic equation, of two linear equations or of two linear inequalities | M1 |  |
|  | Obtain critical values -1 and $\frac{7}{3}$ | A1 | SR Allow B1 for $x \leqslant-1$ only or $x \geqslant \frac{7}{3}$ only if first M1 is not given |
|  | State answer $x \leqslant-1, x \geqslant \frac{7}{3}$ | A1 | Do not accept $\frac{7}{3} \leqslant x \leqslant-1$ or $-1 \geqslant x \geqslant \frac{7}{3}$ for A1 |
|  | Total: | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3 | Integrate to obtain form $k e^{\frac{1}{2} x+3}$ where $k$ is constant not equal to 4 | M1 |  |
|  | Obtain correct $8 e^{\frac{1}{2} x+3}$ | A1 | Allow unsimplified for A1 |
|  | Obtain $8 e^{\frac{1}{2} a+3}-8 e^{3}=835$ or equivalent | A1 |  |
|  | Carry out correct process to find $a$ from equation of form $k e^{\frac{1}{2 a+3}}=c$ | M1 |  |
|  | Obtain 3.65 | A1 | If 3.65 seen with no actual attempt at integration, award B1 if it is thought that trial and improvement with calculator has been used. |
|  | Total: | 5 |  |
| 4(i) | Use iteration correctly at least once | M1 |  |
|  | Obtain final answer 2.08 | A1 |  |
|  | Show sufficient iterations to 4 dp to justify answer or show sign change in interval (2.075, 2.085) | A1 |  |
|  | Total: | 3 |  |
| 4(ii) | State or clearly imply equation $x=\frac{2 x^{2}+x+9}{(x+1)^{2}}$ or same equation using $\alpha$ | B1 |  |
|  | Carry out relevant simplification | M1 |  |
|  | Obtain $\sqrt[3]{9}$ | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(i) | State $R=3$ | B1 | Allow marks for (i) if seen in (ii) |
|  | Use appropriate trigonometric formula to find $\alpha$ | M1 |  |
|  | Obtain 48.19 with no errors seen | A1 |  |
|  | Total: | 3 |  |
| 5(ii) | Carry out evaluation of $\cos ^{-1} \frac{1}{3}(=70.528 \ldots)$ | M1 | M1 for $\cos ^{-1}\left(\frac{1}{R}\right)$ |
|  | Obtain correct answer 118.7 | A1 |  |
|  | Carry out correct method to find second answer | M1 |  |
|  | Obtain 337.7 and no others between 0 and 360 | A1 |  |
|  | Total: | 4 |  |
| 6(i) | State or imply correct $y$-values $0, \tan \frac{1}{6} \pi, \tan \frac{2}{6} \pi$ | B1 | Some candidates have their calculator in degree mode when working out $\tan \frac{\pi}{6}$ etc. this gives 0.00915 and 0.0183. Allow B1. |
|  | Use correct formula, or equivalent, with $h=\frac{1}{12} \pi$ and $y$-values | M1 | Must be convinced they have considered 3 values for $y$ for M1 |
|  | Obtain 0.378 | A1 |  |
|  | Total: | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(ii) | State or imply $\pi \int\left(\sec ^{2} 2 x-1\right) \mathrm{d} x$ | B1 |  |
|  | Integrate to obtain $k_{1} \tan 2 x+k_{2} x$, any non-zero constants including $\pi$ or not | M1 |  |
|  | Obtain $\frac{1}{2} \tan 2 x-x$ or $\pi\left(\frac{1}{2} \tan 2 x-x\right)$ | A1 |  |
|  | Obtain $\pi\left(\frac{1}{2} \sqrt{3}-\frac{1}{6} \pi\right)$ or equivalent | A1 |  |
|  | Total: | 4 |  |
| 7(i) | Differentiate $x$ and $y$ and form $\frac{d y}{d x}$ | M1 |  |
|  | Obtain $\frac{4 t^{3}-6 t^{2}+8 t-12}{3 t^{2}+6}$ | A1 | First 2 marks may be implied by an attempt at division |
|  | Carry out division at least as far as $k t$ or equivalent | M1 | For M1, it must be division by a quadratic factor. Allow attempt at factorisation with same conditions as for division |
|  | Obtain $\frac{4}{3} t$ | A1 |  |
|  | Obtain $\frac{4}{3} t-2$ with complete division shown and no errors seen | A1 |  |
|  | Total: | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(ii) | State or imply gradient of straight line is $\frac{1}{2}$ | B1 | Allow B1 if $y=\frac{1}{2} x+\frac{9}{2}$ is seen |
|  | Attempt value of $t$ from their $\frac{d y}{d x}=$ their negative reciprocal of gradient of line | M1 |  |
|  | Obtain $t=0$ and hence (1,5) | A1 |  |
|  | Total: | 3 |  |
| 8(i) | Apply product rule to find first derivative | *M1 |  |
|  | Obtain $6 x \ln \left(\frac{1}{6} x\right)+3 x$ or equivalent | A1 | Allow unsimplified for A1 |
|  | Identify $x=6$ at $P$ | B1 |  |
|  | Substitute their value of $x$ at $P$ into attempt at first derivative | DM1 | dep *M |
|  | Obtain 18 | A1 |  |
|  | Total: | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $8($ ii) | Equate their first derivative to zero and attempt solution of equation of form <br> $k \ln \left(\frac{1}{6} x\right)+m=0$ | $* \mathbf{M 1}$ |  |
|  | Obtain $x$-coordinate of form $a_{1} e^{a_{2}}$ | DM1 | dep *M |
|  | Obtain $x=6 \mathrm{e}^{-\frac{1}{2}}$ or exact equivalent | A1 |  |
|  | Substitute exact $x-$ value in the form $a_{1} e^{a_{2}}$ and attempt simplification to remove $\ln$ | M1 |  |
|  | Obtain $-54 \mathrm{e}^{-1}$ or exact equivalent | A1 |  |

