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Note: '(3 sfs)' means 'answer which rounds to ... to 3 sfs'. If correct ans seen to > 3sfs, ISW for later rounding. Penalise < 3 sfs only once in paper.

1		B(200, $\frac{1}{6}$) \rightarrow N($\frac{100}{3}$, $\frac{250}{9}$)	B1		seen or implied		
		$\frac{25.5-\frac{100}{3}}{\sqrt{\frac{250}{3}}}$	M1		allow with wrong or no cc		
		=-1.486	A1		(Accept alternative correct methods)		
		comp '1.486' with 1.282	M1		or comp ('1.486') with 0.1		
		Evidence to reject H_0 There is some evidence that $p < \frac{1}{6}$					
		or, e.g. It is likely that $p < \frac{1}{6}$ oe	A1 ft	[5]	No contradictions		
2	(i)	Each employee has an equal chance of being chosen	B1	[1]	oe		
	(ii)	Est $(\mu) = 4$	B1				
		Est $(\sigma^2) = \frac{10}{9} (\frac{199.22}{10} - 4'^2)$	M1		sub in correct formula attempted		
		= 4.36 (3 sf)	A1	[3]	working may not be seen		
	(iii)	Distances travelled by all employees at the firm	B1	[1]	oe		
3	(i)	$((0.5672 + 0.6528) \div 2) = 0.61$	B1	[1]			
	(ii)	$0.61' + z \sqrt{\frac{0.61' \times (1 - 0.61')}{350}} = 0.6528$	M1		oe		
		$z = 0.0428 \times \sqrt{\frac{700}{'0.61' \times (1-'0.61')}}$ oe	M1		correct rearrangement of correct equn, ft '0.61'		
		= 2.321 98% confidence	A1 A1 ft	[4]	ft their z (dep on both Ms)		

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4	(i)	H ₀ : $\mu = 12.5$ H ₁ : $\mu \neq 12.5$ $\frac{13.5-12.5}{4.2 \div \sqrt{50}}$	B1 M1		allow 4.2 ÷ 50		
		= 1.68(4) '1.684' < 1.96	M1		comp 1.96 allow comp 1.645 if H1: μ > 12.5 or comp 1 – ('1.684') with 0.025		
		No evidence that mean time has changed	A1 ft	[5]	No contradictions ft their 1.684, but not comp 1.645		
	(ii)	0.05	B 1	[1]			
5	(i)	$T \sim N(6 \times 2.4, 6 \times 0.3^{2})$ (= N(14.4, 0.54) $\frac{16^{-14.4'}}{\sqrt{0.54'}}$ (= 2.177)	M1 M1		seen or implied ft their E and Var; allow without $\sqrt{(Accept alternative method N(2.4,(0.3^2)/6))}$		
		1 – (*2.177')	M1		correct area consistent with their working		
		= 0.0147 (3 sf)	A1	[4]			
	(ii)	$D = X_1 - 1.1X_2$ E(D) = -0.24 Var(D) = 0.3 ² + 1.1 ² × 0.3 ² (= 0.1989) $\frac{0 - (-0.24)}{\sqrt{0.1989'}} (= 0.538)$	B1 M1 M1		ft their E and Var; allow without $$		
		('0.538')	M1		correct area consistent with their working		
		= 0.705 (3 sf)	A1	[5]			
6	(i)	2 m	B1	[1]	allow without un	nits	
	(ii)	$k \int_0^2 x^2 (2-x) dx = 1$	M1		attempt integ $f(x)$ and '= 1'. Ignore limits correct integration and limits		
		$k\left[\frac{2x^3}{3} - \frac{x^4}{4}\right]_0^2$	A1				
		$k \times \left[\frac{16}{3} - 4\right] = 1 \text{ or } k \times \frac{4}{3} = 1 \text{ oe}$					
		$k = \frac{3}{4} \operatorname{AG}$	A1	[3]	No errors seen		
	(iii)	$\frac{3}{4}\int_0^2 x^3(2-x)dx$	M1		attempt integ xf((x), condone	missing k
		$= \frac{3}{4} \times \left[\frac{2x^4}{4} - \frac{x^5}{5} \right]_0^2$	A1		correct integration and limits, condone missing k		
		1.2 m oe	A1	[3]	allow without un	nits	

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(iv)	$\frac{\frac{3}{4}}{\left(=\frac{3}{4} \times \left(\frac{2}{3} - \frac{1}{4}\right)\right)}$	M1		attempt integ $f(x)$, 0 to 1, condone missing k					
	$=\frac{5}{16}$ or 0.3125 oe	A1							
	$400 \times \frac{5}{16} = 125$	A1 ft	[3]	ft their $\frac{5}{16}$					
7 (a) (i)	$0.01 \times 80 \text{ and } 0.015 \times 60 (1 - e^{-0.8}) \times (1 - e^{-0.9}) = 0.327 (3 \text{ sf})$	M1 M1 A1	[3]	$(1 - e^{-\lambda}) \times (1 - e^{-\lambda})$ allow one end end	(λ, μ) any λ, μ (λ	$\lambda \neq \mu$)			
(ii)	$\lambda = 0.02 \times 40 + 0.015 \times 60$	M1		or their $0.8 + 0.9$)				
	$e^{-1.7} \times (1 + 1.7 + \frac{1.7^2}{2})$ = 0.757 (3 sf)	M1 A1	[3]						
(b)	$e^{-\lambda} \times \lambda = p$ and $e^{-\lambda} \times \frac{\lambda^2}{2} = 1.5p$	M1		or $e^{-\lambda} \times \frac{\lambda^2}{2} = 1.5$ implied	$5 \times e^{-\lambda} \times \lambda$ see	en or			
	$\lambda = 3$	A1							
	$p = e^{-3} \times 3$ = 0.149 (3 sf)	M1 A1	[4]	their λ					

[Total for paper 50]