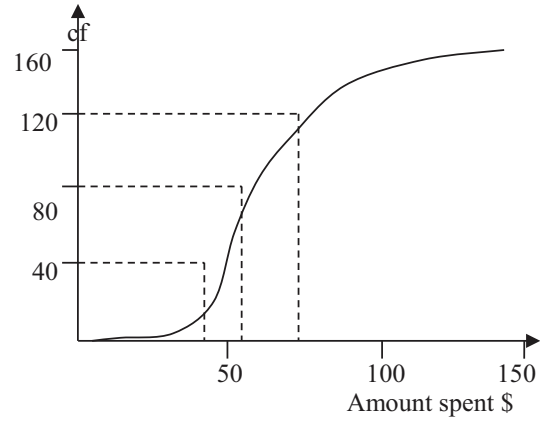


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Question	Answer	Marks	Guidance
<b>1</b>	$z = 1.037$ $1.037 = \frac{1.8 - 1.62}{\sigma}$  $\sigma = 0.18/1.037 = 0.174$	<b>B1</b>  <b>M1</b>  <b>A1</b> [3]	Rounding to 1.04  Standardising attempt allow cc no sq rt must have a z-value i.e. not 0.8023 or 0.5596.
<b>2</b>	$P(\text{throwing a 4}) = (1 - 0.4) / 4 = 0.15$  $P(\text{at most 1}) = P(0, 1) \text{ or } 1 - P(2, 3)$ $= (0.85)^3 + {}^3C_1 (0.15) (0.85)^2$  $= 0.939$	<b>M1</b> <b>A1</b>  <b>M1</b> <b>M1</b>  <b>A1</b> [5]	Sensible attempt to find P(1) Correct answer  A binomial term with ${}^3C_n$ or any $p$ Binomial expression with ${}^3C_n P(0, 1)$ or $1 - P(2, 3)$ $p = 0.15$ or $0.85$
<b>3 (i)</b>	$P(\text{cup of coffee}) = 0.6 \times 0.9 + 0.4 \times 0.3 = 0.66$	<b>M1</b> <b>A1</b> [2]	Summing two 2-factor probabilities Correct answer accept 0.660
<b>(ii)</b>	$P(\text{Not on time} \mid \text{no cup of coffee})$  $= \frac{P(\text{not on time} \cap \text{no cup})}{P(\text{no cup})} = \frac{0.4 \times 0.7}{1 - 0.66}$  $= \frac{0.28}{0.34} = 0.824$	<b>M1</b>  <b>M1</b>  <b>A1</b> [3]	$0.4 \times 0.7$ seen as num or denom of a fraction  Attempt at P(no cup) as $0.1 \times p_1 + 0.7 \times p_2$ or as $1 - (i)$ seen anywhere
<b>4</b>	$[P(X = 0)] = P(B, B) = 5/7 \times 4/6 = 10/21$  $[P(X = 1)] = P(G, B) + P(B, G) = 2/7 \times 5/6 \times 2 = 10/21$ $[P(X = 2)] = P(G, G) = 2/7 \times 1/6 = 1/21$  $E(X) = 0 + 10/21 + 2/21 = 4/7 (0.571)$  $\text{Var}(X) = 0 + 10/21 + 4/21 - (4/7)^2 = 50/147 (0.340)$	<b>M1</b>  <b>A1</b>  <b>A1</b>  <b>B1</b>  <b>M1</b> <b>A1</b> [6]	Attempt to find P(0) or P(1) or P(2) can be seen as P(BB) etc. or table unsimplified P(1) or P(BG)+P(GB) correct  P(0) or P(2) correct must see X value  Correct answer fit their probs P(1) and P(2)  Attempt at $\sum x^2 p - [E(X)]^2$
<b>5 (i)</b>	$P(x < 3.0) = P\left(z < \frac{3.0 - 2.6}{0.25}\right) + P(z < 1.6) = 0.945$	<b>M1</b> <b>M1</b> <b>A1</b> [3]	Standardising no sq rt no cc Correct area i.e. prob > 0.5 legit
<b>(ii)</b>	$X \sim B(500, 0.9452) \sim N(472.6, 25.898)$ $P\left(z > \frac{479.5 - 472.6}{\sqrt{25.89848}}\right) = P(z > 1.3558)$ $= 1 - 0.9125 = 0.0875$	<b>M1</b> <b>M1</b> <b>M1</b> <b>M1</b> <b>A1</b> [5]	$500 \times '0.9452'$ and $500 \times '0.9452' \times ('1 - 0.9452')$ seen or Standardising must have sq rt. All M marks indep cc either 479.5 or 480.5 seen correct area i.e. < 0.5

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Question	Answer	Marks	Guidance
(iii)	$500 \times 0.9452$ and $500 \times (1 - 0.9452)$ are both $> 5$	<b>B1</b> <sup>ft</sup> [1]	must see at least $500 \times 0.0548 > 5$ or ft their (i) accept $np > 5$ , $nq > 5$ if both not $npq > 5$
6 (a) (i)	$9 \times 9 \times 8$  $= 648$  OR $900 - 28 \times 9 = 648$	<b>M1 M1</b>  <b>A1</b> [3]	Logical listing attempt
	(ii)	<b>M1</b>	
(b)	8 ... in $1 \times 8 \times 5 = 40$ 9... in $1 \times 8 \times 4 = 32$  Total 104 ways	<b>M1</b> <b>M1</b>  <b>A1</b> [4]	Mult 3 combs, ${}^6C_x \times {}^5C_y \times {}^4C_z$ Summing 2 or 3 three-factor outcomes can be perms, + instead of $\times$ 2 options correct unsimplified
	(b)	<b>M1</b> <b>M1</b>  <b>A1</b> <b>A1</b> [4]	
7 (i)	cf 16, 56, 104, 130, 160	<b>M1</b>	Attempt at cf table (up to 160) no graph needed accept %cf but give final
		<b>B1</b>  <b>M1</b>  <b>A1</b> [4]	linear scale minimum 0 to 160 and 0 to 120  Attempt to plot points at (30, 16), (50, 56), (70, 104), (90, 130), (140, 160) up to 2 errors can have a polygon  All points correct from their scale and joined up, with (0,0) as well
(ii)	median \$59  IQR = $82 - 43 = \$39$	<b>B1</b> <sup>ft</sup>  <b>M1</b> <b>A1</b> <sup>ft</sup> [3]	accept 57–60 or ft their graph if used lb, midpts instead of ub or assume linear interpolation.  Subt a (sensible) LQ from a sensible UQ (generous) Ans ft need a cf graph and UQ 80–84, LQ

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<b>Question</b>	<b>Answer</b>	<b>Marks</b>	<b>Guidance</b>
<b>(iii)</b>	160 – 149 = 11 OR 115 is mid pt of last interval so # of shoppers is $30/2 = 15$ (can be implied)	<b>M1</b> <b>A1</b> [2]	41–46 Subtracting from 160 can be implied Correct answer accept 9–16
<b>(iv)</b>	mean = $(15 \times 16 + 40 \times 40 + 60 \times 48 + 80 \times 26 + 115 \times 30) / 160$ = $10250 / 160 = \$64.1 = \$64.1$	<b>M1</b> <b>A1</b> [2]	Using $\Sigma xf / 160$ with mid-points