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- 1 Use power law for logarithms correctly at least once
Obtain $3x \log 5 = 4y \log 7$ or $3x \ln 5 = 4y \ln 7$ or equivalent
Obtain 1.612
- M1
A1
A1 [3]
- 2 (i) Carry out division, or equivalent, at least as far as quotient $2x + k$
Obtain quotient $2x - 3$
Obtain remainder $-25x + 18$
- M1
A1
A1 [3]
- (ii) Subtract remainder of form $ax + b$ ($ab \neq 0$) from $2x^3 - 7x^2 - 9x + 3$ or multiply their quotient by $x^2 - 2x + 5$
Obtain $p = 16$ and $q = -15$
- M1
A1 [2]
- 3 (i) State or imply non-modular equation $(3u + 1)^2 = (2u - 5)^2$ or corresponding pair of linear equations
Attempt solution of 3-term quadratic equation or of 2 linear equations
Obtain -6 and $\frac{4}{5}$
- B1
M1
A1 [3]
- (ii) Evaluate $\tan^{-1} \frac{1}{k}$ for at least one of their solutions k from part (i)
Obtain 0.896
- M1
A1 [2]
- 4 (i) State $\sin \theta \cos 60 + \cos \theta \sin 60 + \sin \theta \cos 120 + \cos \theta \sin 120$
Use $\sin 60 = \sin 120 = \frac{1}{2}\sqrt{3}$ and $\cos 60 = \frac{1}{2}$, $\cos 120 = -\frac{1}{2}$
Confirm result $\sqrt{3} \cos \theta$, dependent on *B *B
- *B1
*B1
DB1 [3]
- (ii) (a) $\cos 45$ seen
State $\sqrt{\frac{3}{2}}$ or $\frac{1}{2}\sqrt{6}$ or exact equivalent, dependent *B
- *B1
DB1 [2]
- (b) Carry out correct process to find at least one value of θ from $\cos^2 \theta = k$
Obtain 40.6
Obtain 139.4
- M1
A1
A1 [3]
- 5 (i) Use product rule to obtain form $k_1 e^{\frac{1}{3}x} + k_2 x e^{\frac{1}{3}x}$
Obtain correct $6e^{\frac{1}{3}x} + 2xe^{\frac{1}{3}x}$
Equate first derivative to 40 and obtain equation without e present, dep *M
Confirm $p = 3 \ln \frac{20}{p+3}$ or $x = 3 \ln \frac{20}{x+3}$
- *M1
A1
DM1
A1 [4]
- (ii) Consider sign of $p - 3 \ln \frac{20}{p+3}$ at 3.3 and 3.5 or equivalent
Complete argument correctly with appropriate calculations
- M1
A1 [2]
- (iii) Carry out iterative process correctly at least once
Obtain final answer 3.412
Show sufficient iterations to justify accuracy to 3 dp or show sign change in interval (3.4115, 3.4125)
- M1
A1
B1 [3]

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- 6 (a) Obtain integrand $2e^{-2x} + \frac{1}{2}e^{-x}$ B1
 Obtain integral of form $k_1e^{-2x} + k_2e^{-x}$ M1
 Obtain answer $-e^{-2x} - \frac{1}{2}e^{-x}$, condoning absence of $+c$ A1 [3]
- (b) Integrate to obtain $\frac{1}{2}\ln(2x+5)$ B1
 Show correct use of $p \ln k = \ln k^p$ law at least once M1
 Show correct use of $\ln m - \ln n = \ln \frac{m}{n}$ law M1
 Obtain $\ln \frac{5}{3}$ A1 [4]
- (c) State or imply correct ordinates $\log 2, \log 5, \log 8$ or decimal equivalents B1
 Use correct formula, or equivalent, correctly with $h=3$ and 3 ordinates M1
 Obtain answer 3.9 with no errors seen A1 [3]
- 7 (i) State $\frac{dx}{dt} = \sin t$ and $\frac{dy}{dt} = -6 \sin 2t$ B1
 Use $\sin 2t = 2 \sin t \cos t$ B1
 Form expression for $\frac{dy}{dx}$ in terms of t M1
 Confirm $-12 \cos t$ A1 [4]
- (ii) Identify $\frac{1}{2}\pi$ as value of t B1
 Obtain $(2, -2)$ B1 [2]
- (iii) Identify $\cos 2t = -\frac{1}{3}$ B1
 Attempt to find value of t (or of $\cos t$) for at least one of the two points M1
 Obtain 0.955 (or $\frac{1}{\sqrt{3}}$) or 2.186 (or $-\frac{1}{\sqrt{3}}$) A1
 Obtain $-\frac{12}{\sqrt{3}}$ or $-4\sqrt{3}$ or -6.93 and $\frac{12}{\sqrt{3}}$ or $4\sqrt{3}$ or 6.93 A1 [4]