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	Cambridge International AS/A Level – May/June 2016	9709	21

- 1 Obtain first derivative of form $k_1 e^{4x} + \frac{k_2}{2x+3}$ **M1**
 Obtain correct $12e^{4x} - \frac{12}{2x+3}$ **A1**
 Obtain 8 **A1** [3]
- 2 Use $\cot \theta = 1 \div \tan \theta$ **B1**
 Form equation involving $\tan \theta$ only and with no denominators involving θ **M1**
 Obtain $\tan^2 \theta = \frac{2}{7}$ **A1**
 Obtain 28.1 **A1**
 Obtain 151.9 **A1** [5]
 Allow other valid methods
- 3 Rearrange to $3e^{2x} - 14e^x + 8 = 0$ or equivalent involving substitution **B1**
 Solve quadratic equation in e^x to find two values of e^x ***M1**
 Obtain $\frac{2}{3}$ and 4 **A1**
 Use natural logarithms to solve equation of form $e^x = k$ where $k > 0$ dep on **DM1**
 Allow M mark if left in exact form **M1**
 Obtain -0.405 **A1**
 Obtain 1.39 **A1** [6]
- 4 (i) Carry out division, or equivalent, at least as far as $8x^2 + kx$ **M1**
 Obtain correct quotient $8x^2 + 14x - 15$ **A1**
 Confirm remainder is 5 **A1** [3]
- (ii) State or imply expression is $(x+2)(\dots\text{their quadratic quotient}\dots)$ **B1^{ft}**
 Attempt factorisation of their quadratic quotient **M1**
 Obtain $(x+2)(2x+5)(4x-3)$ **A1** [3]
- (iii) State $\pm \frac{3}{4}$ and no others, following their 3 linear factors **B1^{ft}** [1]
- 5 (i) Obtain $\frac{dx}{d\theta} = 2 \sec^2 \theta$ and $\frac{dy}{d\theta} = 6 \cos 2\theta$ **B1**
 Use $\cos 2\theta = 2 \cos^2 \theta - 1$ or equivalent **B1**
 Form expression for $\frac{dy}{dx}$ in terms of $\cos \theta$ **M1**
 Confirm $6 \cos^4 \theta - 3 \cos^2 \theta$ with no errors seen **A1** [4]
- (ii) Equate first derivative to zero and obtain at least $\cos \theta = \pm \frac{1}{\sqrt{2}}$ **B1**
 Obtain $\theta = \frac{1}{4}\pi$ or equivalent **B1**
 Obtain (2, 3) **B1** [3]
- (iii) State or imply $\theta = \frac{1}{3}\pi$ or equivalent **B1**
 Obtain $-\frac{3}{8}$ or equivalent only **B1** [2]

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- 6 (i) Use quotient rule or equivalent *M1
 Obtain $\frac{6x(x^2 + 4) - 6x^3}{(x^2 + 4)^2}$ or equivalent A1
 Equate first derivative to $\frac{1}{2}$ and remove algebraic denominators dep on *M1 DM1
 Obtain $48p = p^4 + 8p^2 + 16$ or $48x = x^4 + 8x^2 + 16$ or equivalent A1
 Confirm given result $p = \sqrt{\frac{48p - 16}{p^2 + 8}}$ A1 [5]
- (ii) Consider sign of $p - \sqrt{\frac{48p - 16}{p^2 + 8}}$ at 2 and 3 or equivalent M1
 Complete argument correctly with appropriate calculations A1 [2]
- (iii) Carry out iteration process correctly at least once M1
 Obtain final answer 2.728 A1
 Show sufficient iterations to justify accuracy to 4 sf or show sign change in interval (2.7275, 2.7285) B1 [3]
- 7 (a) Rewrite integrand as $\sec^2 2x + \cos^2 2x$ B1
 Express $\cos^2 2x$ in form $k_1 + k_2 \cos 4x$ M1
 State correct $\frac{1}{2} + \frac{1}{2} \cos 4x$ A1
 Integrate to obtain at least terms involving $\tan 2x$ and $\sin 4x$ M1
 Obtain $\frac{1}{2} \tan 2x + \frac{1}{2}x + \frac{1}{8} \sin 4x$, condoning absence of $+c$ A1 [5]
- (b) Integrate to obtain $2x + 2 \ln(3x - 2)$ B1
 Show correct use of $p \ln k = \ln k^p$ law at least once, must be using $\ln(3x - 2)$ M1
 Show correct use of $\ln m - \ln n = \ln \frac{m}{n}$ law, must be using $\ln(3x - 2)$ M1
 Use or imply $20 = \ln(e^{20})$ B1
 Obtain $\ln(16e^{20})$ A1 [5]