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1	$5C2 \left(\frac{1}{x}\right)^3 (3x^2)^2$ $10(\times 1) \times 3^2$ $90(x)$	B1 B1 B1 [3]	Can be seen in expansion Identified as leading to answer
2	$(\pi) \int (x^3 + 1) dx$ $(\pi) \left[\frac{x^4}{4} + x \right]$ $6\pi \text{ or } 18.8$	M1 A1 DM1A1 [4]	Attempt to resolve y^2 and attempt to integrate Applying limits 0 and 2. (Limits reversed: Allow M mark and allow A mark if final answer is 6π)
3 (i)	$6 + k = 2 \rightarrow k = -4$	B1 [1]	
3 (ii)	$(y) = \frac{6x^3}{3} - \frac{4}{-2}x^{-2} (+c)$ $9 = 2 + 2 + c \quad c \text{ must be present}$ $(y) = 2x^3 + 2x^{-2} + 5$	B1B1 ^h M1 A1 [4]	fit on <i>their</i> k . Accept $+\frac{k}{-2}x^{-2}$ Sub (1,9) with numerical k . Dep on attempt \int Equation needs to be seen Sub (2, 3) $\rightarrow c = -13\frac{1}{2}$ scores M1A0
4	$r = \frac{3+2d}{3} \text{ or } \frac{3+12d}{3+2d} \text{ or } r^2 = \frac{3+12d}{3}$ $(3+2d)^2 = 3(3+12d) \text{ oe}$ OR sub $2d = 3r - 3$ $(4)d(d-6) = 0$ OR $3r^2 = 18r - 15 \rightarrow (r-1)(r-5)$ $d = 6$ $r = 5$	B1 M1 DM1 A1 A1 [5]	1 correct equation in r and d only is sufficient Eliminate r or d using valid method Attempt to simplify and solve quadratic Ignore $d = 0$ or $r = 1$ Do not allow -5 or ± 5

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5	$\frac{dy}{dx} = [8] + [-2] [(2x-1)^{-2}]$ $= 0 \rightarrow 4(2x-1)^2 = 1 \text{ oe eg } 16x^2 - 16x + 3 = 0$ $x = \frac{1}{4} \text{ and } \frac{3}{4}$ $\frac{d^2y}{dx^2} = 8(2x-1)^{-3}$ <p>When $x = \frac{1}{4}$, $\frac{d^2y}{dx^2} (= -64)$ and/or < 0 MAX</p> <p>When $x = \frac{3}{4}$, $\frac{d^2y}{dx^2} (= 64)$ and/or > 0 MIN</p>	B2,1,0 M1 A1 B1 ^{✓*} DB1 DB1 [7]	Set to zero, simplify and attempt to solve soi Needs both x values. Ignore y values fit to $k(2x-1)^{-3}$ where $k > 0$ Alt. methods for last 3 marks (values either side of $1/4$ & $3/4$) must indicate <u>which</u> x -values and cannot use $x = 1/2$. (M1A1A1)
6	$BAC = \sin^{-1}(3/5)$ or $\cos^{-1}(4/5)$ or $\tan^{-1}(3/4)$ $ABC = \sin^{-1}(4/5)$ or $\cos^{-1}(3/5)$ or $\tan^{-1}(4/3)$ $ACB = \pi/2$ (Allow 90°) Shaded area = ΔABC – sectors ($AEF + BEG + CFG$) $\Delta ABC = \frac{1}{2} \times 4 \times 3$ oe Sum sectors = $\frac{1}{2} [3^2 0.6435] + 2^2 0.9273 + 1^2 1.5708$ OR $\frac{\pi}{360} [3^2 36.8(7) + 2^2 53.1(3) + 1^2 90]$ $6 - 5.536 = 0.464$	B1 B1 B1 M1 B1 M1 A1 [7]	Accept $36.8(7)^\circ$ Accept $53.1(3)^\circ$
7	$\frac{dy}{dx} = 2x - 5x^{1/2} + 5$ $\frac{dy}{dx} = 2$ $2x - 5x^{1/2} + 5 = 2$ $2x - 5x^{1/2} + 3 (= 0) \text{ or equivalent 3-term quadratic}$ <p>Attempt to solve for $x^{1/2}$ e.g.</p> $(2x^{1/2} - 3)(x^{1/2} - 1) = 0$ $x^{1/2} = 3/2 \text{ and } 1$ $x = 9/4 \text{ and } 1$	B1 B1 M1 A1 DM1 A1 A1 [7]	Equate their dy/dx to <i>their</i> 2 or $1/2$. Dep. on 3-term quadratic ALT $5x^{1/2} = 2x + 3 \rightarrow 25x = (2x + 3)^2$ $4x^2 - 13x + 9 (= 0)$ $x = 9/4$ and 1

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8	<p>(i) $3\sin^2 x - \cos^2 x + \cos x = 0$ Use $s^2 = 1 - c^2$ and simplify to 3-term quad $\cos x = -3/4$ and 1 $x = 2.42$ (allow 0.77π) or 0 (extra in range max 1)</p> <p>(ii) $2x = 2\pi - \text{their } 2.42$ or $360 - 138.6$ $x = 1.21$ (0.385π), 1.93 ($0.614/5\pi$), 0, π (3.14) (extra max 1)</p>	<p>M1 M1 A1 A1A1 [5]</p> <p>B1^h B1B1 [3]</p>	<p>Multiply by $\cos x$ Expect $4c^2 - c - 3 = 0$ SC1 for 0.723 (or 0.23π), π following $4c^2 + c - 3 = 0$ Expect $2x = 3.86$ Any 2 correct B1. Remaining 2 correct B1. SCB1 for all 69.3, 110.7, 0, 180 (degrees) SCB1 for .361, $\pi/2$, 2.78 after $4c^2 + c - 3 = 0$</p>
9	<p>(i) $\mathbf{AB} = \mathbf{OB} - \mathbf{OA} = \begin{pmatrix} -1 \\ 2 \\ p+4 \end{pmatrix}$ $\mathbf{CB} = \mathbf{OB} - \mathbf{OC} = \begin{pmatrix} -4 \\ 5 \\ p-2 \end{pmatrix}$ $1+4+(p+4)^2 = 16+25+(p-2)^2$ $p=2$</p> <p>(ii) $\mathbf{AB} \cdot \mathbf{CB} = 4+10-5 = 9$ $\mathbf{AB} = \sqrt{1+4+25} = \sqrt{30}$, $\mathbf{CB} = \sqrt{16+25+1} = \sqrt{42}$ $\cos ABC = \frac{9}{\sqrt{30}\sqrt{42}}$ or $\frac{9}{6\sqrt{35}}$ $ABC = 75.3^\circ$ or 1.31rads (ignore reflex angle 285°)</p>	<p>B1 B1 M1 A1 [4]</p> <p>M1 M1 M1 A1 [4]</p>	<p>Ignore labels. Allow BA or BC Use of $x_1x_2 + y_1y_2 + z_1z_2$ Product of moduli Allow one of AB, CB reversed - but award A0</p>
10	<p>(i) $2(ax^2 + b) + 3 = 6x^2 - 21$ $a = 3$, $b = -12$</p> <p>(ii) $3x^2 - 12 \geq 0$ or $6x^2 - 21 \geq 3$ $x \leq -2$ i.e. (max) $q = -2$</p> <p>(iii) $y \geq 6(-3)^2 - 21 \Rightarrow$ range is $(y) \geq 33$</p>	<p>M1 A1A1 [3]</p> <p>M1 A1 [2]</p> <p>B1 [1]</p>	<p>Allow = or \leq or $>$ or $<$. Ft from <i>their</i> a, b Must be in terms of q (eg $q \leq -2$) Do not allow $y > 33$. Accept all other notations e.g. $[33, \infty)$ or $[33, \infty]$</p>

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(iv)	$y = 6x^2 - 21 \Rightarrow x = (\pm)\sqrt{\frac{y+21}{6}}$ $(\text{fg})^{-1}(x) = -\sqrt{\frac{x+21}{6}}$ Domain is $x \geq 33$	M1 A1 B1 ^h [3]	Allow $y = \dots$. Must be a function of x ft from <i>their</i> part (iii) but x essential
11 (i)	$AB^2 = 6^2 + 7^2 = 85, BC^2 = 2^2 + 9^2 = 85$ (\rightarrow isosceles) $AC^2 = 8^2 + 2^2 = 68$ $M = (2, -2) \text{ or } BM^2 = (\sqrt{85})^2 - (\frac{1}{2}\sqrt{68})^2$ $BM = \sqrt{2^2 + 8^2} = \sqrt{68} \text{ or } \sqrt{85 - 17} = \sqrt{68}$ $\text{Area } \Delta ABC = \frac{1}{2}\sqrt{68}\sqrt{68} = 34$	B1B1 B1 B1 B1 B1 [6]	Or $AB = BC = \sqrt{85}$ etc Where M is mid-point of AC
(ii)	Gradient of $AB = 7/6$ Equation of AB is $y + 1 = \frac{7}{6}(x + 2)$ Gradient of $CD = -6/7$ Equation of CD is $y + 3 = \frac{-6}{7}(x - 6)$ Sim Eqns $2 = \frac{-6}{7}x + \frac{36}{7} - \frac{7}{6}x - \frac{14}{6}$ $x = \frac{34}{85} = \frac{2}{5} \text{ oe}$	B1 M1 M1 M1 M1 A1 [6]	Or $y - 6 = \frac{7}{6}(x - 4)$