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1	$\text{Var} = 16 \times 9 + 25 \times 36$ (= 1044) $\text{sd} = 32.3$ or $6\sqrt{29}$ or $\sqrt{1044}$	B1 M1 A1	M1 for 16 (or 4^2) & 25 (or 5^2) used M1 for add any multiples of 9 and 36 only
	Total	3	
2 (i)	$H_0: \lambda = 0.5$ $H_1: \lambda > 0.5$	B1 1	or Pop mean = 0.5, not just Mean = 0.5 or Pop mean (per m^2) = 0.1 Accept μ instead of λ
(ii)	$1 - e^{-0.5}(1 + 0.5)$ $= 0.0902$ (3 sf) comp 0.1 Claim justified or there is evidence to support claim	M1 A1 M1 A1 [✓] 4	$1 - P(X = 0, 1)$ attempted, any λ . Allow 1 end error Allow 0.09 Valid comparison NB $0.9098 > 0.9$ recovers M1A1 M1 oe Accept 'Reject H_0 ' if correctly defined No contradictions.
	Total	5	
3	$\lambda = 5 \times 0.15$ (= 0.75) $E(\text{amount}) = 200 \times 0.75 = 150$ $\text{Var}(\text{weekly no of hole-in-ones}) = 0.75$ $\text{Var}(\text{amount}) = 200^2 \times 0.75$ $= 30,000$	M1 A1 B1 [✓] M1 A1 5	Allow $200^2 \times$ their variance (with nothing added/subtracted at any stage) (SR probability table can score M1A0 srB1 if var rounds to 30,000 (2sf))
	Total	5	
4 (i)	Conclude flight times affected when in fact they have not been.	B1 B1 2	Or accept pop mean changed from 6.2 although pop mean has not changed from 6.2
(ii)	$H_0: \text{Pop mean (or } \mu) = 6.2$ $H_0: \text{Pop mean (or } \mu) \neq 6.2$ $\frac{5.98 - 6.2}{\frac{0.8}{\sqrt{40}}}$ $= -1.739$ (\pm) Accept (\pm)1.74 comp $z = 1.96$ No evidence that flight times affected	B1 M1 A1 B1 [✓] 4	Allow with 40 instead of $\sqrt{40}$ Allow SD/Var mix (CV method 5.952 or 6.2279 M1 A1) For valid comparison or $P(z < -1.739) = 0.041 > 0.025$ or $5.98 > 5.952$ or $6.2 < 6.228$ and correct conclusion
(iii)	H_0 was not rejected oe Type II	B1* B1*dep 2	If in (ii) H_0 was rejected, then: H_0 rejected B1; Type I B1dep
	Total	8	

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5	(i)	$\frac{14800}{50} \text{ or } 296$ $\frac{50}{49} \left(\frac{4390000}{50} - 296^2 \right) (= 187.755)$ $= 188 \text{ (3 sf)}$	B1 M1 A1	3	Oe
	(ii)	$2 \times z \times \sqrt{\frac{187.755}{50}} = 5.45 \quad \text{oe}$ $z = 1.406 \text{ or } 1.405$ $\Phi(1.406) (= 0.92 \text{ or } 0.9199)$ $\alpha = 84 \text{ (2 sf)} \quad \text{allow } 83.98$	M1 A1 M1 A1	4	If '2 ×' omitted: $z \times \sqrt{\frac{187.755}{50}} = 5.45$ M1 $z = 2.812 \text{ or } 2.810$ A0 $\Phi(2.812) (= 0.9975)$ $\alpha = 99.5 \text{ or } 99 \text{ or } 100$ M1 A0 For complete method to find α SR use of biased var(184) scores M1A1(1.4205) A=84.5 M1A1
	(iii)	0.96^4 $= 0.849 \text{ (3 sf)}$	M1 A1	2	
		Total		9	
6	(i)	$k \int_0^{15} (225 - t^2) dt = 1$ $k \left[225t - \frac{t^3}{3} \right]_0^{15} = 1$ $k \times [3375 - 1125] = 1 \text{ or } k \times 2250 = 1$ $\left(k = \frac{1}{2250} \text{ AG} \right)$	M1 A1 A1	3	Attempt integ $f(x)$ and = 1. Ignore limits Correct integration and limits No errors seen
	(ii)	$\frac{1}{2250} \int_0^{15} (225 - t^2) dt$ $\left(= \frac{1}{2250} \left[225t - \frac{t^3}{3} \right]_0^{15} \right)$ $= \frac{1}{2250} \left[2250 - \left(2250 - \frac{1000}{3} \right) \right]$ $= \frac{4}{27} \text{ or } 0.148 \text{ (3 sf)}$	M1 A1 A1	3	Attempt integ, ignore limits Or $1 - \int_0^{10}$ Correct integration and limits. Condone missing k
	(iii)	$\frac{1}{2250} \int_0^{15} (225t - t^3) dt$ $= \frac{1}{2250} \left[\frac{225t^2}{2} - \frac{t^4}{4} \right]_0^{15}$ $= \frac{1}{2250} \left[\frac{50625}{2} - \frac{50625}{4} \right]$ $= \frac{45}{8} \text{ or } 5.625 \text{ or } 5.63 \text{ (3 sf)}$	M1* A1 M1*dep A1	4	Attempt integ $xf(x)$, ignore limits Correct integration and limits. Condone missing k Sub correct limits into their integral Accept 5 mins 37 or 38 secs
		Total		10	

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7	(i)	Poisson (Actually binomial with) $n > 50$ and np (or λ) (= 2.1) which is < 5	B1 B1 B1	3	Allow without “binomial” Accept n large Accept p small ($p < 0.1$)
	(ii)	$\lambda = 2.1$ $e^{-2.1} \left(1 + 2.1 + \frac{2.1^2}{2} + \frac{2.1^3}{3!} \right)$ = 0.839 (3 sf)	B1 M1 A1	3	Attempt $P(0,1,2,3)$ any λ allow 1 end error SR ₁ Ft Normal $N(2.1,2.1)$ B1 standardising M1 0.833 A1 SR ₂ Ft Binomial $B(10500,0.0002)$ B1 calculating binomial prob $P(0,1,2,3)$ M1 = 0.8386 A1
	(iii)	$P(X \geq 1) = 1 - e^{-2.1}$ (= 0.87754) $P(X = 1,2,3) = e^{-2.1} \left(2.1 + \frac{2.1^2}{2} + \frac{2.1^3}{3!} \right)$ (= 0.71619) $\frac{P(X = 1,2,3)}{P(X > 1)}$ $\left(= \frac{0.71619}{0.87754} \right)$ = 0.816 (3 sf)	M1 M1 M1 A1	4	Any λ Or ‘0.839’ – $e^{-2.1}$ Any λ Allow any attempted $\frac{P(X = 1,2,3)}{P(X > 1)}$ Any λ SR ₁ Ft Normal $P(>0.5) = 0.86523$ M1 $P(1,2,3) = 0.698$ M1 $0.698/0.86523 = 0.807$ M1A1 SR ₂ FT Binomial M1 M1 M1 A1
	Total		10		
	Total for paper		50		