

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge International AS/A Level – May/June 2015	9709	61

1	$P(x < 3.273) = 0.5 - 0.475 = 0.025$ $z = -1.96$ $\frac{3.2 - \mu}{0.714} = -1.96$ $\mu = 4.60s$	M1 A1 M1 A1 [4]	Attempt to find z-value using tables in reverse ± 1.96 seen Solving their standardised equation z-value not nec Correct ans accept 4.6
2 (i)	UQ 5.5 – 7.0 cm	B1 [1]	
(ii)	fd 5.33, 25, 28, 20.7, 6, fd <p style="text-align: center;">length in cm</p>	M1 A1 B1 B1 [4]	Attempt at fd or scaled freq [fr/cw] Correct heights seen on graph Correct bar widths no gaps Labels (fd and length/cm) and correct bar ends
3 (i)	$P(A) = \frac{1}{3} \times \frac{2}{3} + \frac{2}{3} \times \frac{1}{3} = \frac{4}{9}$ $P(B) = \frac{27}{36} = \frac{3}{4}$ $P(A \cap B) = \frac{12}{36} = \frac{1}{3}$ $P(A) \times P(B) = \frac{4}{9} \times \frac{3}{4} = \frac{1}{3}$ Independent as $P(A \cap B) = P(A) \times P(B)$	M1 M1 B1 M1 A1 [5]	Sensible attempt at $P(A)$ Sensible attempt at $P(B)$ correct $P(A \cap B)$ Cf $P(A \cap B)$ with $P(A) \times P(B)$ need at least 1 correct Correct conclusion following all correct working
(ii)	Not mutually exclusive because $P(A \cap B) \neq 0$ Or give counter example e.g. 1 and 6	B1^{ft} [1]	ft their $P(A \cap B)$
4 (i)	$(1 - x)0.9 + x \times 0.24 = 0.801$ $x = 0.15$	M1 A1 A1 [3]	Eqn with sum of two 2-factor probs = 0.801 Correct equation Correct answer

Page 5	Mark Scheme	Syllabus	Paper
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(ii)	$P(\geq 100 \text{ times given } \leq 3 \text{ views})$ $\frac{P(\geq 100 \text{ times} \cap \geq 3 \text{ views})}{P(\geq 3 \text{ views})} =$ $\frac{0.85 \times 0.1}{0.85 \times 0.1 + 0.15 \times 0.76 \text{ or } 1 - 0.801}$ $= 0.427$	B1 M1 A1 A1 [4]	0.85×0.1 seen on its own as num or denom of a fraction Attempt at $P(\geq 3 \text{ views})$ either $(0.85 \times p_1 + 0.15 \times p_2)$ or $1 - 0.801$ seen anywhere Correct unsimplified $P(\geq 3 \text{ views})$ as num or denom of a fraction Correct answer
5 (i)	$\text{new mean} = \frac{9 \times 7.1 + 18 \times 5.2}{27}$ $= 5.83$	M1 A1 [2]	Mult by 9 and 18 and dividing by 27 correct answer
(ii)	$1.45^2 = \text{so } \frac{\sum x_t^2}{9} = 472.6125 \text{ mm}$ $0.96^2 = \frac{\sum x_g^2}{18} - 5.2^2 \text{ so}$ $\sum x_g^2 = 503.3088$ $\frac{\text{New sd}^2}{27} = \frac{472.6125 + 503.3088}{27} - 5.83^2 = 2.117$ $\text{New sd} = 1.46$	M1 A1 A1 M1 A1 [5]	subst in a correct variance formula sq rt or not correct $\sum x_t^2$ (rounding to 470) correct $\sum x_g^2$ (rounding to 500) using $\sum x_t^2 + \sum x_g^2$, dividing by 27 and subtr comb mean ² correct answer
6 (i)	$P(5, 6, 7) = {}^8C_5(0.68)^5(0.32)^3 + {}^8C_6(0.68)^6(0.32)^2 + {}^8C_7(0.68)^7(0.32)$ $= 0.722$	M1 M1 A1 A1 [4]	Binomial term ${}^8C_x p^x(1-p)^{8-x}$ seen $0 < p < 1$ Summing 3 binomial terms Correct unsimplified answer Correct answer
(ii)	$np = 340, npq = 108.8$ $P(x > 337) = P\left(z > \frac{337.5 - 340}{\sqrt{108.8}}\right)$ $= P(z > -0.2396)$ $= 0.595$	B1 M1 M1 M1 A1 [5]	Correct (unsimplified) mean and var standardising with sq rt must have used 500 cc either 337.5 or 336.5 correct area (> 0.5) must have used 500 correct answer
(iii)	$np(340) > 5 \text{ and } nq(160) > 5$	B1 [1]	must have both or at least the smaller, need numerical justification
7 (a) (i)	$\frac{9!}{2!2!3!}$ $= 15120 \text{ ways}$	B1 B1 [2]	Dividing by 2!2!3! Correct answer

Page 6	Mark Scheme	Syllabus	Paper
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(ii)	*****3 in $\frac{8!}{2!2!3!} = 1680$ ways	B1	Correct ways end in 3
	*****7 in $\frac{8!}{2!3!} = 3360$ ways	B1	Correct ways end in 7
	Total even = 15120 – 1680 – 3360	M1	Finding odd and subt from 15120 or their (i)
	= 10080 ways	A1 [4]	Correct answer
	OR		
	*****2 in $8!/2!3! = 3360$ ways	B1	One correct way end in even
*****6 in $8!/2!2!3! = 1680$ ways	B1	correct way end in another even	
*****8 in $8!/2!2!2! = 5040$ ways	M1	Summing 2 or 3 ways	
Total = 10080 ways	A1	Correct answer	
OR			
“15120” $\times 6/9 = 10080$	M2	Mult their (i) by 2/3 oe	
	A2	Correct answer	
(b)	T(3) S(6) G(14)		
	1 1 3 in $3 \times 6 \times {}^{14}C_3 = 6552$	M1	Mult 3 (combinations) together assume $6 = {}^6C_1$ etc
	1 3 1 in $3 \times {}^6C_3 \times 14 = 840$	M1	Listing at least 4 different options
	3 1 1 in $1 \times 6 \times 14 = 84$	M1	Summing at least 4 different options
	2 2 1 in ${}^3C_2 \times 6 \times {}^{14}C_2 = 630$	M1	options
	2 1 2 in ${}^3C_2 \times 6 \times {}^{14}C_2 = 1638$	B1	At least 3 correct numerical options
	1 2 2 in $3 \times {}^6C_2 \times {}^{14}C_2 = 4095$		
Total ways = 13839 (13800)	A1 [5]	Correct answer	