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- 1 (i) State or imply equation  $(3x+4)^2 = (3x-11)^2$  or  $3x+4 = -(3x-11)$  B1  
 Attempt solution of 'quadratic' equation or linear equation M1  
 Obtain  $x = \frac{7}{6}$  or equivalent (and no other solutions) A1 [3]
- (ii) Use logarithms to solve equation of form  $2^y =$  their answer to (i) ( must be + ve) M1  
 Obtain 0.222 (and no other solutions) A1 [2]
- 2 State or imply that  $\ln y = \ln A + p(x-1)$  B1  
 Equate gradient to  $p$  or obtain two equations for  $\ln A$  and  $p$  M1  
 Obtain  $p = 0.44$  A1  
 Substitute values correctly, to find value of  $\ln A$  DM1  
 Obtain  $A = 3.2$  A1 [5]
- Alternative:  
 Obtain an equation either  $e^{1.6} = Ae^p$  or  $e^{2.92} = Ae^{4p}$  M1  
 Obtain both equations correctly A1  
 Solve to obtain  $p = 0.44$  A1  
 Substitute value correctly to find  $A$  DM1  
 Obtain  $A = 3.2$  A1 [5]
- 3 Differentiate to obtain form  $p \cos x + q \sin 2x$  or equivalent M1  
 Obtain correct  $6 \cos x + 4 \sin 2x$  or equivalent A1  
 Substitute  $\frac{1}{6}\pi$  to obtain derivative equal to  $5\sqrt{3}$  or 8.66 A1  
 Form equation of tangent (not normal) using numerical value of gradient obtained by differentiation M1  
 Obtain  $y = 8.66x - 2.53$  cao A1 [5]
- 4 (i) Substitute  $x = -2$  in  $f(x)$  and equate to zero to obtain  $-8 + 4a + b = 0$  or equiv B1  
 Substitute  $x = -1$  in  $g(x)$  and equate to  $-18$  M1  
 Obtain  $-1 + b - a = -18$  or equivalent A1  
 Solve a pair of linear equations for  $a$  or  $b$  DM1  
 Obtain  $a = 5, b = -12$  A1 [5]
- (ii) Simplify  $g(x) - f(x)$  to obtain form  $kx^2 + c$  where  $k < 0$  M1  
 Obtain  $-17x^2 + 7$  and state 7, following their value of  $c$  A1√ [2]

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- 5 (i) Obtain integral of form  $ke^{\frac{1}{2}x} + mx$  M1  
 Obtain correct  $6e^{\frac{1}{2}x} + x$  A1  
 Apply limits and obtain correct  $6e^{\frac{1}{2}a} + a - 6$  A1  
 Equate to 10 and introduce natural logarithm correctly DM1  
 Obtain given answer  $a = 2\ln\left(\frac{16-a}{6}\right)$  correctly A1 [5]
- (ii) Use the iterative formula correctly at least once M1  
 Obtain final answer 1.732 A1  
 Show sufficient iterations to justify accuracy to 3 d.p. or show sign change in interval (1.7315, 1.7325) A1 [3]
- 6 (i) State or imply  $\operatorname{cosec} 2\theta = \frac{1}{\sin 2\theta}$  B1  
 Express left-hand side in terms of  $\sin \theta$  and  $\cos \theta$  M1  
 Obtain given answer  $\sec^2 \theta$  correctly A1 [3]
- (ii) (a) State or imply  $\cos \theta = \frac{1}{\sqrt{5}}$  or  $\tan \theta = 2$  at least B1  
 Obtain 1.11 or awrt 1.11, allow  $0.353\pi$  B1  
 Obtain 2.03 or awrt 2.03, allow  $0.648\pi$  and no other values between 0 and  $\pi$  B1 [3]
- (b) State integrand as  $\sec^2 2x$  B1  
 Integrate to obtain expression of form  $k \tan mx$  M1  
 Obtain correct  $\frac{1}{2} \tan 2x$  A1  
 Obtain  $\frac{1}{2}\sqrt{3}$  or exact equivalent A1 [4]
- 7 (i) Obtain  $3y^2 \frac{dy}{dx}$  as derivative of  $y^3$  B1  
 Obtain  $4y + 4x \frac{dy}{dx}$  as derivative of  $4xy$  B1  
 Equate derivative of left-hand side to zero and solve for  $\frac{dy}{dx}$ , must be from implicit differentiation M1  
 Confirm given answer  $\frac{dy}{dx} = -\frac{4y}{3y^2 + 4x}$  correctly A1 [4]
- (ii) State or imply  $y = 0$  B1  
 Substitute in equation of curve and show contradiction B1 [2]
- (iii) State or imply  $3y^2 + 4x = 0$  B1  
 Eliminate one variable from equation of curve using  $3y^2 + 4x = 0$  M1  
 Obtain  $y = -2$  A1  
 Obtain  $x = -3$  A1 [4]