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| 1 | | θ is obtuse, $\sin \theta = k$ | | | | |
| (i) | | $\cos\theta = -\sqrt{(1-k^2)}$ | B1 [1] | cao | | |
| (ii) | | $\tan \theta = \frac{\sin \theta}{\cos \theta} \text{ used}$ | M1 | Used, atter | npt at cosine | seen in (i) |
| | | $\rightarrow \tan \theta = -\frac{k}{\sqrt{(1-k^2)}}$ aef | A1√ [^] [2] | Ft for their only, from | cosine as a fu part (i) | nction of <i>k</i> |
| (iii) | | $\sin\left(\theta+\pi\right)=-k$ | B1 [1] | cao | | |
| 2 | | $y = 2x^2$, $X(-2, 0)$ and $P(p, 0)$ | | | | |
| (i) | | $A = \frac{1}{2} \times (2 + p) \times 2p^{2} (= 2p^{2} + p^{3})$ | M1 A1 [2] | Attempt at of <i>p</i> and use | base and heig e of $\frac{bh}{2}$ | ht in terms |
| (ii) | | $\frac{\mathrm{d}A}{\mathrm{d}p} = 4p + 3p^2$ | B1 | cao | | |
| | | $\frac{\mathrm{d}A}{\mathrm{d}t} = \frac{\mathrm{d}A}{\mathrm{d}p} \times \frac{\mathrm{d}p}{\mathrm{d}t} = 0.02 \times 20 = 0.4$ | M1 A1 | any correct | method, cao | |
| | | or $\frac{dA}{dt} = 4p \frac{dp}{dt} + 3p^2 \frac{dp}{dt}$ | [3] | | | |
| 3 | | $(1-x)^2(1+2x)^6$. | | | | |
| (i) (a | (a) | $(1-x)^6 = 1 - 6x + 15x^2$ | B2,1 [2] | -1 each erro | or | |
| (1 | b) | $(1+2x)^6 = 1 + 12x + 60x^2$ | B2,1 [2] | -1 each erro SC B1 only correct desc SC only on of the '1' in | or y, in each part cending powe e penalty for a each expans | , for all 3 ers omission ion |
| (ii) | | Product of (a) and (b) with >1 term $\rightarrow 60 - 72 + 15 = 3$ | M1 DM1A1 [3] | Must be 2 c M1 exactly condone 3 <i>x</i> | or more products. $\frac{3}{2}$ | icts cao, |

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| 4 | $\overrightarrow{OA} = \begin{pmatrix} 3\\0\\-4 \end{pmatrix}, \overrightarrow{OB} = \begin{pmatrix} 6\\-3\\2 \end{pmatrix}, \overrightarrow{OC} = \begin{pmatrix} k\\-2k\\2k-3 \end{pmatrix}$ | | | | |
| (i) | $OA \cdot OB = 18 - 8 = 10$ Modulus of $OA = 5$, of $OB = 7$ | M1 | Use of $x_1x_2 + y_1y_2 + z_1z_2$ | | |
| | Angle $AOB = \cos^{-1}\left(\frac{10}{35}\right)$ aef | M1 | All linked with modulus cao, (if angle given, no penalty), | | |
| | $\rightarrow \frac{10}{35} \text{ or } \frac{2}{7}$ | A1 [3] | correct angle implies correct cosine | | |
| (ii) | $\overrightarrow{AB} = \mathbf{b} - \mathbf{a} = \begin{pmatrix} 3 \\ -3 \\ 6 \end{pmatrix}$ | B1 | allow for $\mathbf{a} - \mathbf{b}$ | | |
| | $k^2 + 4k^2 + (2k - 3)^2 = 9 + 9 + 36$ | M1 | Correct use of moduli using their AB obtains 3 term quadratic. cao | | |
| | $\rightarrow 9k^2 - 12k - 45(=0)$ $\rightarrow k=3 \text{ or } k = -\frac{5}{3}$ | DM1 A1 [4] | | | |
| 5 (i) | $24 = r + r + r\theta$ $\rightarrow \theta = \frac{24 - 2r}{r}$ $4 = \frac{1}{r} + 2\theta + 24r + 2\theta + 12\theta + 2\theta + 12\theta$ | M1 | (May not use θ) Attempt at $s = r\theta$ linked with 24 and r | | |
| | $A = \frac{1}{2}r^{2}\theta = \frac{1}{2}r^{2} = 12r - r^{2}$. aet, ag | [3] | Uses A formula with θ as $f(r)$. cao | | |
| (ii) | $(A=)36-(r-6)^2$ | B1 B1 [2] | cao | | |
| (iii) | Greatest value of $A = 36$ | B1√ | Ft on (ii). | | |
| | $(r=6) \rightarrow \theta = 2$ | B1 [2] | cao, may use calculus or the discriminant on $12r - r^2$ | | |

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| 6 (i) | y-2t = -2(x-3t)(y+2x=8t) | M1 | Unsimplified or equivalent forms |
| | Set x to $0 \rightarrow B(0, 8t)$ Set y to $0 \rightarrow A(4t, 0)$ \rightarrow Area = $16t^2$ | M1 A1 [3] | Attempt at both <i>A</i> and <i>B</i> , then using cao |
| (ii) | $m = \frac{1}{2}$ $\rightarrow y - 2t = \frac{1}{2}(x - 3t)(2y = x + t)$ Set y to 0 $\rightarrow C(-t, 0)$ Midpoint of CP is (t, t) | B1 M1 A1 | cao Unsimplified or equivalent forms co correctly shown. |
| | This lies on the line $y = x$. | A1 [4] | |
| 7 (a) | $ar^2 = \frac{1}{3}$, $ar^3 = \frac{2}{9}$ | | |
| | $\rightarrow r = \frac{2}{3}$ aef | M1 | Any valid method, seen or implied. Could be answers only. |
| | Substituting $\rightarrow a = \frac{3}{4}$ | A1 | Both a and r |
| | $\rightarrow S_{\infty} = \frac{\frac{3}{4}}{\frac{1}{3}} = 2\frac{1}{4}$ aef | M1 A1 [4] | Correct formula with $ r < 1$, cao |
| (b) | $4a = a + 4d \rightarrow 3a = 4d$ | B1 | May be implied in 360 = 5/2(a+4a) |
| | $360 = S_5 = \frac{5}{2}(2a+4d)$ or $12.5a$ | M1 | Correct S_n formula or sum of 5 terms |
| | $\rightarrow a = 28.8^{\circ}$ aef Largest = $a + 4d$ or $4a = 115.2^{\circ}$ aef | A1 B1 [4] | cao, may be implied (may use degrees or radians) |

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| 8 | f: $x \mapsto 5 + 3\cos\left(\frac{1}{2}x\right)$ for $0 \le x \le 2\pi$. | | |
| (i) | $5 + 3\cos\left(\frac{1}{2}x\right) = 7$ | | (1) 2 |
| | $\cos\left(\frac{1}{2}x\right) = \frac{2}{3}$ | B1 | Makes $\cos\left(\frac{-x}{2}\right) = \frac{-3}{3}$ |
| | $\frac{1}{2}x = 0.84 x = 1.68 \text{ only, aef}$ | M1A1 [3] | Looks up \cos^{-1} first, then $\times 2$ |
| | (in given range) | | |
| (ii) | 8 | B1 B1 [2] | <i>y</i> always +ve, <i>m</i> always –ve. from $(0, 8)$ to $(2\pi, 2)$ (may be implied) |
| | 2 × 2π | | |
| (iii) | No turning point on graph or 1:1 | B1 [1] | cao, independent of graph in (ii) |
| (iv) | $y = 5 + 3\cos\left(\frac{1}{2}x\right)$ | M1 | Tries to make x subject. |
| | Order; $-5, \div 3, \cos^{-1}, \times 2$ | M1 | Correct order of operations |
| | $x = 2\cos^{-1}\left(\frac{x-5}{3}\right)$ | A1 [3] | cao |

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| 9 | $y = x^3 + px^2$ | | | | |
| (i) | $\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 + 2px$ | B1 | cao | | |
| | Sets to $0 \rightarrow x = 0$ or $-\frac{2p}{3}$ | M1 | Sets differen | ntial to 0 | |
| | $\rightarrow (0,0) \text{ or } \left(-\frac{2p}{3},\frac{4p^3}{27}\right)$ | A1 A1 [4] | cao cao, first A1 for any correct turning point or any correct pair of x values. 2nd A1 for 2 complete TPc | | correct ect pair of omplete |
| (ii) | $\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} = 6x + 2p$ | M1 | Other methods include; clear demonstration of sign change of gradient, clear reference to the shape of the curve | | |
| | At $(0, 0) \rightarrow 2p$ +ve Minimum | A1 | WWW | | |
| | At $\left(-\frac{2p}{3}, \frac{4p^3}{27}\right) \rightarrow -2p$ -ve Maximum | A1 [3] | | | |
| (iii) | $y = x^{3} + px^{2} + px \rightarrow 3x^{2} + 2px + p (= 0)$ | B1 | | | |
| | Uses $b^2 - 4ac$ $\rightarrow 4n^2 - 12n \le 0$ | M1 | Any correct | use of discri | minant |
| | $\rightarrow 0 aef$ | A1 [3] | cao (condo | ne ≤) | |

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| 10 | $y = \frac{8}{\sqrt{3x+4}}$ | | | |
| (i) | $\frac{dy}{dx} = \frac{-4}{(3x+4)^{\frac{3}{2}}} \times 3 \text{aef}$ | B1 B1 | Without the "×3" For "×3" even if 1st B mark lost. | |
| | $\rightarrow m_{(x=0)} = -\frac{3}{2}$ Perpendicular $m_{(x=0)} = \frac{2}{3}$ | M1 | Use of $m_1m_2 = -1$ after attempting to find $\frac{dy}{dx}_{(x=0)}$ | |
| | Eqn of normal $y-4 = \frac{2}{3}(x-0)$ | M1 | Unsimplified line equation | |
| | Meets $x = 4$ at $B\left(4, \frac{20}{3}\right)$ | A1 [5] | cao | |
| (ii) | $\int \frac{8}{\sqrt{(3x+4)}} \mathrm{d}x = \frac{8\sqrt{(3x+4)}}{\frac{1}{2}} \div 3$ | B1 B1 | Without "÷3". For "÷3" | |
| | Limits from 0 to 4 \rightarrow Area $P = \frac{32}{3}$ Area $Q = \text{Trapezium} - P$ | M1 A1 | Correct use of correct limits. cao | |
| | Area of Trapezium = $\frac{1}{2}\left(4 + \frac{20}{3}\right) \times 4 = \frac{64}{3}$ | M1 | Correct method for area of trapezium | |
| | \rightarrow Areas of <i>P</i> and <i>Q</i> are both $\frac{32}{3}$ | A1 [6] | All correct. | |