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	GCE A LEVEL – May/June 2014	9709	71

Note: “(3 sfs)” means “answer which rounds to ... to 3 sfs”. If correct ans seen to ≥ 3 sfs, ISW for later rounding. Penalise < 3 sfs only once in paper.

1	$N(483.2, 537.92)$ or $N(483.2, 23.2^2)$ $\frac{436-483.2}{\sqrt{537.92}}$ or $\frac{436-483.2}{23.2}$ (= -2.035) $\Phi(-2.035) = 1 - \Phi(2.035)$ $= 0.021$ or 2.1%	B1 M1 M1 A1 [4]	or $\frac{8.2}{\sqrt{8}}$ or $\frac{8.2^2}{8}$ seen or implied or $\frac{436-60.4}{8.2/\sqrt{8}}$ standardising (no mixed methods) Correct area consistent with their working
		[Total: 4]	
2	$\frac{70}{69} \times 2.70 = 2.73913$ $3.61 \pm z \sqrt{\frac{2.73913}{70}}$ $z = 1.96$ 3.22 to 4.00 (3 sf)	M1A1 M1 B1 A1 [5]	or $3.61 \pm z \sqrt{\frac{2.70}{69}}$ M2A1(implied) without $\frac{70}{69}$: $3.61 \pm z \sqrt{\frac{2.70}{70}}$ M0A0M1 $z = 1.96$ B1 3.23 to 3.99(4.00) (3 sf) A1 Answer must be an interval
		[Total: 5]	
3	$H_0: \mu = 250$ $H_1: \mu > 250$ $\frac{250.06-250}{0.2/\sqrt{40}}$ $= 1.90$ comp with $z = 1.645$ Claim is justified or There is evidence that claim is true	B1 M1 A1 M1 A1 [5]	Both hypotheses M1 for standardising, must have $\sqrt{40}$. Accept cv method For valid comparison “1.90” with 1.645 or area comparison or CVs Correct conclusion. No contradictions NB 2-tail test scores B0 M1 A1 M1 (use 1.96) A0
		[Total: 5]	
4 (i)	$B(3500, 0.001)$ Poisson with mean = 3.5 $n > 50$ and $np < 5$	B1 B1 B1 [3]	or $Po(3.5)$ Both. Or $n > 50$ and $\lambda < 5$ or $3.5 < 5$
(ii)	$e^{-3.5}(1 + 3.5 + \frac{3.5^2}{2} + \frac{3.5^3}{3!})$ $= 0.537$ (3 dp)	M1 A1 [2]	Allow any λ
		[Total: 5]	

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5	(i)	$0.25(1 + 4 + 9) - 1.5^2$ (=1.25 AG)	B1 [1]	
	(ii)	$\frac{1.4-1.5}{\sqrt{\frac{5}{4} \div 300}}$ (= -1.549) $\Phi(\text{"-1.549"}) = 1 - \Phi(\text{"1.549"})$ = 0.0607 (3 sf)	M1 M1 A1 [3]	$\frac{1.4-\frac{1}{600}-1.5}{\sqrt{\frac{5}{4} \div 300}}$ (= -1.523) $\Phi(\text{"-1.523"}) = 1 - \Phi(\text{"1.523"})$ = 0.0639 (3 sf)
	(iii)	Large sample or large n (\bar{X} (approx) normally distr) or Central Limit Theorem	B1 [1]	
			[Total: 5]	
6	(i)	H_0 : Rate = 0.9 H_1 : Rate < 0.9 $1 - P(17, 18, 19, 20)$ $1 - ({}^{20}C_{17} \times 0.1^3 \times 0.9^{17} + {}^{20}C_{18} \times 0.1^2 \times 0.9^{18} + 20 \times 0.1 \times 0.9^{19} + 0.9^{20})$ = 0.133 (3 sf)	B1 M1 M1 A1 [4]	$p = 0.9$ $p < 0.9$ Use of B(20,0.1) Allow $1 - P(18, 19, 20)$ or $1 - P(16, 17, 18, 19, 20)$
	(ii)	Type II H_0 will not be rejected	B1 B1 [2]	or Stephan will conclude standard not fallen No contradictions
			[Total: 6]	

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7	(i)	$\int_1^a \frac{k}{x} dx = 1$ $k[\ln x]_1^a = 1$ $k \ln a = 1 \quad k = 1/\ln a$	M1 A1 A1 [3]	Int $f(x)$ & equate to 1. Ignore limits Correct integration and limits and = 1 AG
	(ii)	$\frac{1}{\ln a} \int_1^a 1 dx$ or $k \int_1^a 1 dx$ $= \frac{1}{\ln a} [x]_1^a$ or $k[x]_1^a$ $= \frac{1}{\ln a} (a - 1)$	M1 A1 A1 [3]	Int $xf(x)$. Ignore limits Correct integration and limits (condone missing k)
	(iii)	$\frac{1}{\ln a} \int_1^m \frac{1}{x} dx = 0.5$ $\frac{1}{\ln a} [\ln x]_1^m = 0.5$ $\frac{1}{\ln a} \ln m = 0.5$ $\ln m = 0.5 \ln a$ $m = \sqrt{a}$	M1 A1 A1 A1 [4]	Int $f(x)$ and equate to 0.5. Ignore limits Correct integration and limits (1 to m or m to a) (condone missing k) or $\ln m = \ln a^{0.5}$
			[Total: 10]	
8	(i)	V : cannot have neg value W : cannot have non-integer value	B1 B1 [2]	
	(ii)	(a) $e^{-\lambda} = p$ and $\lambda e^{-\lambda} = 2.5p$ (Hence $\lambda = 2.5$ AG)	B1 [1]	or equiv explanation
	(ii)	(b) $1 - e^{-2.5} (1 + 2.5 + \frac{2.5^2}{2})$ $= 0.456$ (3 sf)	M1 A1 [2]	Allow one end error
(iii)	$\Phi^{-1}(0.5793) = -0.2$ $N(\mu, \mu)$ seen or implied $\frac{40.5 - \mu}{\sqrt{\mu}} = "-0.2"$ $\mu + "-0.2" \sqrt{\mu} - 40.5 = 0$ $\sqrt{\mu} = \frac{"0.2" \pm \sqrt{"0.2" ^2 + 4 \times 40.5}}{2}$ $(= 6.4647..)$ $\mu = 41.8$ (3 sf)	B1 M1 M1 M1 A1 [5]	Allow no cc or incorrect cc For solving quadratic in $\sqrt{\mu}$ (or μ) Ignore other answer for $\sqrt{\mu}$, but not for μ	
			[Total: 10]	

[Total for paper 50]