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|--|---|--|----------|-----------|---|------|-------------|-------|-------|---------|--|---|--|---|-----|--|---|-----------|--|---|-----|-------------------------------|--|
| <p>1 (i)</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="border-right: 1px solid black; padding: 5px;">Adults</td> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="padding: 5px;">Children</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;">8 6 5 4 3</td> <td style="border-right: 1px solid black; padding: 5px;">4</td> <td style="padding: 5px;">3</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;">7 4 3 3 2 1</td> <td style="border-right: 1px solid black; padding: 5px;">5</td> <td style="padding: 5px;">4</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;">8 4 3 1</td> <td style="border-right: 1px solid black; padding: 5px;">6</td> <td style="padding: 5px;">1 2 7 8</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="border-right: 1px solid black; padding: 5px;">7</td> <td style="padding: 5px;">2 7</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="border-right: 1px solid black; padding: 5px;">8</td> <td style="padding: 5px;">1 3 4 6 9</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="border-right: 1px solid black; padding: 5px;">9</td> <td style="padding: 5px;">2 5</td> </tr> </table> <p>key 3 5 4 represents 53 seconds for adults and 54 seconds for children</p> | Adults | | Children | 8 6 5 4 3 | 4 | 3 | 7 4 3 3 2 1 | 5 | 4 | 8 4 3 1 | 6 | 1 2 7 8 | | 7 | 2 7 | | 8 | 1 3 4 6 9 | | 9 | 2 5 | <p>B1</p> <p>B1</p> <p>B1</p> | <p>Single stem and key correct – including adults, children and seconds</p> <p>Right hand leaves correct shape</p> <p>Left hand leaves correct shape</p> |
| Adults | | Children | | | | | | | | | | | | | | | | | | | | | |
| 8 6 5 4 3 | 4 | 3 | | | | | | | | | | | | | | | | | | | | | |
| 7 4 3 3 2 1 | 5 | 4 | | | | | | | | | | | | | | | | | | | | | |
| 8 4 3 1 | 6 | 1 2 7 8 | | | | | | | | | | | | | | | | | | | | | |
| | 7 | 2 7 | | | | | | | | | | | | | | | | | | | | | |
| | 8 | 1 3 4 6 9 | | | | | | | | | | | | | | | | | | | | | |
| | 9 | 2 5 | | | | | | | | | | | | | | | | | | | | | |
| <p>(ii) Two from: Children's estimates more spread out Adults estimates lower Adults are symmetrical whereas children are skewed</p> | <p>B1</p> <p>B1</p> | <p>oe</p> <p>oe</p> <p>oe</p> <p style="text-align: center;">2</p> | | | | | | | | | | | | | | | | | | | | | |
| <p>2 (i) $np = 252 \times 1/7 = 36$, $npq = 252 \times 1/7 \times 6/7 = 30.857$</p> $P\left(z < \left(\frac{29.5 - 36}{\sqrt{30.857}}\right)\right) + P\left(z > \left(\frac{44.5 - 36}{\sqrt{30.857}}\right)\right)$ $= P(z < -1.170) + P(z > 1.530)$ $= 1 - 0.8790 + 1 - 0.9370$ $= 0.184$ | <p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> | <p>Unsimplified 36 and 30.857 seen, oe</p> <p>any standardising, sq rt needed any continuity correction either 29.5, 30.5, 43.5, 44.5</p> <p>correct area $2 - (\Phi_1 + \Phi_2)$</p> <p>correct answer</p> <p style="text-align: center;">5</p> | | | | | | | | | | | | | | | | | | | | | |
| <p>(ii) np and nq are both > 5</p> | <p>B1</p> | <p>1 must have both</p> | | | | | | | | | | | | | | | | | | | | | |
| <p>3 (i) $P(2) = {}^6C_3 \times {}^3C_2 / {}^9C_5$ OR</p> $\frac{{}^6C_3 \times {}^3C_2}{{}^6C_5 + {}^6C_4 \times {}^3C_1 + {}^6C_3 \times {}^3C_2 + {}^6C_2 \times {}^3C_3}$ <p>OR</p> $3/9 \times 2/8 \times 6/7 \times 5/6 \times 4/5 \times {}^5C_2 = 10/21$ $= 60/126$ <p style="text-align: center;">AG</p> | <p>M1</p> <p>OR</p> <p>M1</p> <p>OR</p> <p>M1</p> <p>A1</p> | <p>Using combinations ${}^aC_b \times {}^cC_d / {}^eC_f$</p> <p>Mult 5 probs with a pC_q If 5C_2 replace by 10, oe must be justified Legit method, as answer given</p> <p style="text-align: center;">2</p> | | | | | | | | | | | | | | | | | | | | | |
| <p>(ii)</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 5px;">x</td> <td style="padding: 5px;">0</td> <td style="padding: 5px;">1</td> <td style="padding: 5px;">2</td> <td style="padding: 5px;">3</td> </tr> <tr> <td style="padding: 5px;">Prob</td> <td style="padding: 5px;">2/42</td> <td style="padding: 5px;">15/42</td> <td style="padding: 5px;">20/42</td> <td style="padding: 5px;">5/42</td> </tr> </table> <p>$P(0) = {}^6C_5 / {}^9C_5 = 6/126$ $P(1) = {}^6C_4 \times {}^3C_1 / {}^9C_5 = 45/126$ $P(3) = {}^6C_2 \times {}^3C_3 / 126 = 15/126$</p> | x | 0 | 1 | 2 | 3 | Prob | 2/42 | 15/42 | 20/42 | 5/42 | <p>B1</p> <p>B1</p> <p>B1</p> <p>B1^{ft}</p> | <p>0, 1, 2, 3 only seen in table. Condone $x = 4, 5$ in table if $P(x) = 0$ or blank and values in table for $x = 0, 1, 2, 3$</p> <p>Any correct prob other than $P(2)$ Any other correct prob $\Sigma P(x) = 1, 3 < n(x) < 6$</p> <p style="text-align: center;">4</p> | | | | | | | | | | | |
| x | 0 | 1 | 2 | 3 | | | | | | | | | | | | | | | | | | | |
| Prob | 2/42 | 15/42 | 20/42 | 5/42 | | | | | | | | | | | | | | | | | | | |

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| 4 | (i) new mean $\frac{172.6 \times 28 - 161.8}{27} = 173$ | M1 A1 | 2 | Mult by 28, sub 161.8 and dividing by 27 or 28 Correct ans |
| | (ii) original $\Sigma x^2 = (4.58^2 + 172.6^2) \times 28$ $= 834728.6$ (835000) Remaining $\Sigma x^2 = 834728.6 - 161.8^2$ $= 808549.36$ sd of remaining $= \sqrt{\frac{808549.36}{27} - 173^2}$ $= 4.16$ | M1 A1 M1 A1 | 4 | Subst in formula to find Σx^2 and attempt to make Σx^2 subject, with 2 terms both squared Correct answer Subtract 161.8^2 from their original Σx^2 Correct ans, accept 4.15 or 3.93 |
| 5 | (i) $z = -1.282$ $-1.282 = \frac{t - 6.5}{1.76}$ $t = 4.24$ | B1 M1 A1 | 3 | Rounding to ± 1.28 seen Standardising, no cc, no sq or sq rt, $z \neq \pm 0.9, \pm 0.1$ Correct answer, accept 4.25 |
| | (ii) $P(z < 1) = 0.8413$ $P(\text{within 1sd of mean}) = 2\Phi - 1$ $= 0.6826$ $P(8, 9)$ $= {}^9C_8(0.6826)^8(0.3174) + (0.6826)^9$ $= 0.167$ | M1 B1 M1 M1 A1 | 5 | $z = 1$ used to find a probability correct prob, accept answer rounding to 0.66, 0.67, 0.68, not from wrong working. If quoted, then implies first M1. Binomial term $p^r(1-p)^{9-r} {}^9C_r$, 9C_r must be seen Binomial expression for $P(8)+P(9)$, any p Correct ans |
| 6 | (i) $P(\text{B champ}) = 0.7 \times 0.7 = 0.49$ | B1 | 1 | |
| | (ii) $P(\text{B champ})$ $= P(\text{WW}) + P(\text{WLW}) + P(\text{LWW})$ $= (0.7 \times 0.7) + (0.7 \times 0.3 \times 0.7) +$ $(0.3 \times 0.7 \times 0.7)$ $= 0.49 + 0.147 + 0.147$ $= 0.784$ | M1 B1 A1 | 3 | Summing at least 2 options, at least one of which is 3-factor 0.147 seen, unsimplified Correct answer |
| | (iii) $P(T_2 T) = \frac{P(T_2 \cap T)}{P(T)}$ $= \frac{0.3 \times 0.3 + 0.7 \times 0.3 \times 0.3}{0.216}$ $= 0.708$ | M1 A1 M1 A1 | 4 | Attempt $P(T_2 \cap T)$ seen anywhere sum of 2 terms Correct unsimplified num of a fraction Dividing by their $(1 - (\text{ii}))$ oe Correct answer |

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| <p>7 (i) (a) $6!$ $(\times) 4!$ OR $(\times) 4 \times 3$ $\div 2!2!3!$ OR $\div 2!3!$ Total 720 ways</p> | <p>M1 M1 M1 A1</p> | <p>Seen in a single term expression as numerator Seen in a single term expression as numerator (denominator may be 1) Seen in a single term expression as denominator 4 Correct ans</p> |
| <p>(i) (b) $1*****3 = \frac{7!}{3!2!} = 420$ $3*****1 = 420$ $3*****3 = 420$ Total = 1260 ways</p> | <p>B1 M1 A1</p> | <p>$\frac{7!}{3!2!}$ seen oe Attempting to evaluate and sum at least 2 of $1***3, 3***1, 3***3$ 3 Correct ans</p> |
| <p>(ii) (a) $5 \times 4 \times 3 = 60$ ways (5P_3)</p> | <p>M1 A1</p> | <p>5P_3 or ${}^5C_3 \times 3!$ (can be implied) 2 Correct ans</p> |
| <p>(ii) (b) 2** in 212, 213, 214, 216, 221, 223, 224, 226, 231, 232, 233, 234, 236, 241, 242, 243, 246 261, 262, 263, 264, 266 Total = 22 ways Alternative Methods: $3 \times {}^4C_1 + 2 \times {}^5C_1$ OR ${}^5P_2 + {}^2C_1$ OR ${}^4P_2 + 2 \times {}^4P_1 + {}^2C_1$</p> | <p>M1 A1 M1 OR M1 OR M1</p> | <p>Listing attempt starting with 2, at least 10 correct entries 2 Correct ans $p \times {}^4C_1 + q \times {}^5C_1$, oe $p + q > 2$ 5P_2 seen Any 2 terms added</p> |