

| Page 4 | Mark Scheme | Syllabus | Paper |
|--------|------------------------------|----------|-------|
| | GCE AS LEVEL – May/June 2014 | 9709 | 21 |

- 1 Either State or imply non-modular inequality $(3x-2)^2 > (x+4)^2$ or corresponding equation or pair of linear equations B1
 Attempt solution of 3-term quadratic equation or of 2 linear equations M1
 Obtain critical values $-\frac{1}{2}$ and 3 A1
 State answer $x < -\frac{1}{2}, x > 3$ A1 [4]
- Or Obtain critical value $x = 3$ from graphical method, inspection, equation B1
 Obtain critical value $x = -\frac{1}{2}$ similarly B2
 State answer $x < -\frac{1}{2}, x > 3$ B1 [4]
- 2 (i) Differentiate to obtain form $k_1 \cos x + k_2 \sec^2 2x$ M1
 Obtain correct second term $2\sec^2 2x$ A1
 Obtain $3\cos x + 2\sec^2 2x$ and hence answer 5 A1 [3]
- (ii) Differentiate to obtain form $ke^{2x}(1+e^{2x})^{-2}$ M1
 Obtain correct $-12e^{2x}(1+e^{2x})^{-2}$ or equivalent (may be implied) A1
 Obtain -3 A1 [3]
- 3 (i) Divide at least as far as x term in quotient, use synthetic division correctly or make use of an identity M1
 Obtain at least $6x^2 - x$ A1
 Obtain quotient $6x^2 - x - 2$ and confirm remainder is 7 (AG) A1 [3]
- (ii) State equation in form $(x^2 - 4)(6x^2 + kx - 2) = 0$, any constant k (may be implied) M1
 Obtain two of the roots $-2, 2, -\frac{1}{2}, \frac{2}{3}$ A1
 Obtain remaining two roots and no others A1 [3]
- 4 (i) Sketch, showing the correct shape of each, $y = 3\ln x$ and $y = 15 - x^3$ B1
 Indicate the correct intercepts $(1,0)$ and $(0,15)$ B1
 Indicate one real root from two correct sketches B1 [3]
- (ii) Consider sign of $3\ln x + x^3 - 15$ for 2.0 and 2.5 or equivalent M1
 Justify conclusion with correct calculations (-4.9 and 3.4 or equivalents) A1 [2]
- (iii) Use the iteration process correctly at least once M1
 Obtain final answer 2.319 A1
 Show sufficient iterations to 5 decimal places to justify answer or show a sign change in the interval $(2.3185, 2.3195)$ A1 [3]
- 5 (i) Express left-hand side as a single fraction M1
 Use $\sin 2\theta = 2\sin \theta \cos \theta$ at some point B1
 Complete proof with no errors seen (AG) A1 [3]

| Page 5 | Mark Scheme | Syllabus | Paper |
|--------|------------------------------|----------|-------|
| | GCE AS LEVEL – May/June 2014 | 9709 | 21 |

- (ii) (a) State $\frac{2}{\sin \frac{1}{4}\pi}$ or equivalent B1
 Obtain $2\sqrt{2}$ or exact equivalent (dependent on first B1) B1 [2]
- (b) State or imply $k \sin 2\theta$ for any k B1
 Integrate to obtain $-\frac{3}{2} \cos 2\theta$ B1
 Substitute both limits correctly to obtain 3 B1 [3]
- 6 (a) Integrate to obtain form $k \ln(2x - 7)$ M1
 Obtain correct $3 \ln(2x - 7)$ A1
 Substitute limits correctly (dependent on first M1) DM1
 Use law for logarithm of a quotient or power (dependent on first M1) DM1
 Confirm $\ln 125$ following correct work and sufficient detail (AG) A1 [5]
- (b) Evaluate y at (1), 5, 9, 13, 17 M1
 Use correct formula, or equivalent, with $h = 4$ and five y -values M1
 Obtain 13.5 A1 [3]
- 7 (i) Obtain $3y + 3x \frac{dy}{dx}$ as derivative of $3xy$ B1
 Obtain $2y \frac{dy}{dx}$ as derivative of y^2 B1
 State $4x + 3y + 3x \frac{dy}{dx} + 2y \frac{dy}{dx} = 0$ B1
 Substitute 2 and -1 to find gradient of curve (dependent on at least one B1) M1
 Form equation of tangent through (2, -1) with numerical gradient (dependent on previous M1) DM1
 Obtain $5x + 4y - 6 = 0$ or equivalent of required form A1 [6]
- (ii) Use $\frac{dy}{dx} = 0$ to find relation between x and y
 (dependent on at least one B1 from part(i)) M1
 Obtain $4x + 3y = 0$ or equivalent A1
 Substitute for x or y in equation of curve M1
 Obtain $-\frac{1}{8}y^2 = 3$ or $-\frac{2}{9}x^2 = 3$ or equivalent and conclude appropriately A1 [4]