

Page 4	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2013	9709	73

1	(i)	9.3	B1	1	
	(ii)	27.9	B1	1	
	(iii)	$E(S) = 17.4$, $E(T) = 19.4$ $E(S - T) = -2.0$, $\text{Var}(S - T) = 37.2$	M1 A1 B1ft	3	For subtracting their $E[S] - E[T]$ can be non-numerical ft (i) & (ii) Adding (i) and (ii) ft non-negative answers only
[Total: 5]					
2		Assume shots independent OR prob of scoring constant $H_0: P(\text{score}) = 0.82$ $H_1: P(\text{score}) > 0.82$ $20 \times 0.82^{19} \times 0.18 + 0.82^{20}$ $= 0.102$ (3 sf) No evidence that improved	B1 B1 M1 A1 B1f	5	In context Both. Allow 'p' For use of Bin(20,0.82) and either P(19) and/or P(20) attempted Valid comparison seen (with 0.05 if H_1 $p \neq 0.82$) and correct conclusion ft numerical errors in 0.102 only Normal approx'n: B1 B1 ($\mu = 16.4$ acceptable here) if earned, then: $CR = 1.222$ (from $\frac{18.5 - 20 \times 0.82}{\sqrt{20 \times 0.82 \times (1 - 0.82)}}$, need cc) comp $z = 1.282$ No evidence that improved SC 1 Same scheme for proportions
[Total: 5]					
3	(i)	$\bar{x} = 930/15 = 62$ $z = 1.751$ $'62' \pm z \times \frac{12}{\sqrt{15}}$ $= 56.6$ to 67.4 (3 sf)	B1 B1 M1 A1	4	Any z Must be an interval
	(ii)	92% of such intervals will contain μ	B1	1	Accept $P(\text{This interval contains } \mu) = 0.92$
	(iii)	Each possible sample of this size is equally likely	B1	1	Each member of pop equally likely to be chosen
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4	(i)	$e^{-2} \times 2 \times e^{-3} \times \frac{3^4}{4!}$	M1	Correct exp'n for P(1) with $\lambda=2$ OR P(4) with $\lambda=3$ Correct exp'n dep M1B1	
		$e^{-5} \times \frac{5^4}{5!}$	B1		
		\div	M1		
		$\frac{162}{625}$ or 0.259 (3 sf)	A1		4
	(ii)	$(e^{-2} \times \frac{2^r}{r!} = \frac{2}{3} e^{-2} \Rightarrow)$	B1	Legitimately shown Legitimately shown on either equation	
		$3 \times 2^r = 2 \times r!$ OR $2^{r-1} = \frac{1}{3} \times r!$	B1		
		$(\Rightarrow 3 \times 2^{r-1} = r!)$ $3 \times 2^3 = 24$ OR $3! = 24$ seen	B1		2
[Total: 6]					
5	(i)	$\int_1^{\infty} \frac{k}{x^3} dx = 1$	M1	All correct, including limits and an attempt to integrate or $0 + \frac{k}{2} = 1$ or $\frac{k}{2} = 1$ AG must be convincing	
		$\left[-\frac{k}{2x^2} \right]_1^{\infty} = 1$	A1		2
		$0 - \left(-\frac{k}{2} \right) = 1$			
	(ii)	$\int_1^2 \frac{2}{x^3} dx$	M1	Attempt integ f(x); ignore limits	
		$= \left[-\frac{1}{x^2} \right]_1^2$ $= \frac{3}{4}$	A1		2
	(iii)	$\int_1^{\infty} \frac{2}{x^2} dx$	M1	Attempt integ xf(x); ignore limits Correct & correct limits	
$= \left[-\frac{2}{x} \right]_1^{\infty}$		A1			
$= 2$		A1	3		
[Total: 7]					

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6	(i)	$\lambda (= 1.4 \times 2.5) = 3.5$ $1 - e^{-3.5} \left(1 + 3.5 + \frac{3.5^2}{2} + \frac{3.5^3}{3!} \right)$ $= 0.463$ (3 sf)	B1 M1 A1	3	Any λ allow one end error
	(ii)	$(\lambda = 672 \times 1.4 = 940.8)$ $N(940.8, 940.8)$ $\frac{999.5 - 940.8}{\sqrt{940.8}}$ (= 1.914) $\Phi('1.914')$ $= 0.972$ (3 sf)	B1 M1 M1 A1	4	Seen or implied Allow with wrong or no cc . no sd/var mixes
[Total: 7]					
7	(i)	Assume sd unchanged or 4500 H_0 : Pop mean = 34600 H_1 : Pop mean > 34600 $\frac{35400 - 34600}{\frac{4500}{\sqrt{90}}}$ $= 1.687/1.686$ (1.69) cf 1.645 < 1.686 Evidence that mean wkly profit has increased	B1 B1 M1 A1 M1 A1 f	6	Both. Allow just μ , but not just “mean” Allow without $\sqrt{90}$ Valid comparison (or 0.0458/0.0459 < 0.05 or 35380 < 35400 or 34600 < 34620) If $H_1: \neq$, and 1.96 used, max B1B0M1A1M1A1f No contradictions
	(ii)	Distr'n of X unknown. Yes	B1* B1* dep	2	Allow not Normal
	(iii)	0.05 or 5%	B1	1	
	(iv)	$\frac{a - 34600}{\frac{4500}{\sqrt{90}}} = 1.645$ $a = 35380$ $\frac{35380 - 36500}{\frac{4500}{\sqrt{90}}}$ (= -2.361) $1 - \Phi('2.361')$ $= 0.0091$	M1 A1 M1 M1 A1	6	Attempt to find cv must see (+) 1.645 allow without $\sqrt{90}$. If found in (i) award when used Standardising with their “ CV “ must use $\sqrt{90}$ Correct tail
[Total: 14]					