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Note: “(3 sfs)” means “answer which rounds to ... to 3 sfs”. If correct ans seen to ≥ 3 sfs, ISW for later rounding. Penalise < 3 sfs only once in paper.

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|----------|-------------|--|---|---|--|
| 1 | (i) | One of each is more likely $P(\text{one of each} = 0.5), P(\text{HH}) = 0.25$ | B1 B1 [2] | or $P(\text{TT}) = 0.25$ | |
| | (ii) | Choose Charlie only if H then T Throw again if T then H | B1 B1 [2] | or similar e.g. HH for A, HT for B, TT for C or vice versa | |
| 2 | | $H_0: \text{Pop mean} = 17$ $H_1: \text{Pop mean} \neq 17$ $\frac{18.2 - 17}{\frac{2.4}{\sqrt{5}}}$ $= 1.12$ (3 sf) '1.12' < 1.96 oe Claim can be accepted | B1 M1 A1 M1 A1ft [5] | Both correct. Allow μ , but not just “mean” Allow incorrect 18.2. Must have $\sqrt{5}$ Comp '1.12' with 1.96 or area '0.132' with 0.025 ft their '1.12' If $H_1: \mu > 17$ and cf 1.645: can score max B0M1A1M1A1ft | $17 \pm 1.96 \frac{2.4}{\sqrt{5}}$ M1 $= (14.9, 19.1)$ A1 '14.9' $< 18.2 < 19.1$ M1 |
| 3 | | $\text{Var}(\text{total}) = 6(3.2^2 + 2.6^2) (+ 0)$ (= 102) Total $\sim N(1528, 102)$ $\frac{1550 - 1528}{\sqrt{102}}$ (= 2.178) $1 - \Phi(2.178)$ $= 0.0147$ (3 sf) | B1 B1 M1 M1 A1 [5] | For mean (1528)oe and for variance (102) May be implied by use of $N(1528, 10.1^2)$ For standardising. No SD/Var mix For correct area consistent with working | |
| 4 | (i) | $\text{est}(\mu) = 2005/200 = (10.025)$ $\text{est}(\sigma^2) = \frac{1}{99} 20175 - \frac{2005^2}{200}$ $= 0.376$ (3 sf) | B1 M1 A1 [3] | Correct subst in correct formula | |
| | (ii) | $\frac{10 - 10.025}{\sqrt{\frac{0.376256}{50}}}$ (= -0.288) $1 - \Phi(0.288)$ $= 0.387$ (3 sf) | M1 M1 A1 [3] | Allow without $\sqrt{\quad}$, but $\div \sqrt{50}$ essential (Use of 'biased' variance can still score fully in (ii)) | |

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| (iii) | Yes; (assumed distr of \bar{X} normal) although distr of X unknown | B1 B1 [2] | |
| 5 (i) | B(520, 0.008) Po(4.16) $n = 500$ which is large, $np = 4.16$ which is < 5 or p small < 0.1 | B1 B1B1 B1 [4] | Po: B1, $\lambda = 4.16$: B1 Both needed |
| (ii) | (a) $1 - e^{-4.16} \left(1 + 4.16 + \frac{4.16^2}{2} + \frac{4.16^3}{3!} \right)$ $= 0.597$ (3 sf) | M1 A1 [2] | $1 - P(0,1,2,3)$ any λ allow one end error |
| | (b) $e^{-4.16} \times \frac{4.16^n}{n!} > e^{-4.16} \times \frac{4.16^{n+1}}{(n+1)!}$ $1 > \frac{4.16}{n+1}$ $n > 3.16$ Smallest n is 4 | M1 A1 A1 [3] | any λ or equiv equn without e and without factorials (Calculation of $P(0), P(1), \dots, P(5)$ scores M1 for at least 3 attempted, A1 all correct, A1 for $n = 4$) |
| 6 (i) | $\frac{1}{2} \int_4^t \frac{1}{\sqrt{t}} dt = 0.9$ or $\frac{1}{2} \int_t^9 \frac{1}{\sqrt{t}} dt = 0.1$ $[\sqrt{t}]_4^t = 0.9$ or $[\sqrt{t}]_t^9 = 0.1$ ($(\sqrt{t} - 2) = 0.9$ or $(3 - \sqrt{t}) = 0.1$) $t = 8.41$ (mins) (3 sf) | M1 A1 A1 [3] | Attempt integ $f(t)$ with unknown limit and 0.9/0.1. Correct integration & limits = 0.9 or 0.1. |
| (ii) | $\frac{1}{2} \int_4^9 \frac{t}{\sqrt{t}} dt$ oe $\frac{1}{2} \left[\frac{t^{1.5}}{1.5} \right]_4^9$ oe $= \frac{19}{3}$ $\frac{1}{2} \int_4^9 \frac{t^2}{\sqrt{t}} dt$ oe $(= \frac{1}{2} \left[\frac{t^{2.5}}{2.5} \right]_4^9 = \frac{211}{5})$ $= \frac{211}{5} - \left(\frac{19}{3} \right)^2$ $= \frac{94}{45}$ or 2.09 (3 sf) | M1 A1 A1 M1 M1 A1 [6] | Attempt integ $tf(t)$. Ignore limits Correct integration & limits Attempt integ $t^2f(t)$. Ignore limits integ $t^2f(t) - (\text{integ } tf(t))^2$ attempted |

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| 7 (i) | Conclude die is biased when it isn't or ${}^5C_3\left(\frac{1}{6}\right)^3\left(\frac{5}{6}\right)^2 + 5\left(\frac{1}{6}\right)^4\left(\frac{5}{6}\right) + \left(\frac{1}{6}\right)^5 + 5$ $= \frac{23}{648} \text{ or } 0.0355 \text{ (3 sf)}$ | B1 M1 A1 [3] | In context or $1 - \left({}^5C_2\left(\frac{1}{6}\right)^2\left(\frac{5}{6}\right)^3 + 5\left(\frac{1}{6}\right)\left(\frac{5}{6}\right)^4 + \left(\frac{5}{6}\right)^5 \right)$ allow 1 end error |
| (ii) | State or attempt $P(0, 1, 2)$ with $p = \frac{2}{3}$ ${}^5C_2\left(\frac{2}{3}\right)^2\left(\frac{1}{3}\right)^3 + 5\left(\frac{2}{3}\right)\left(\frac{1}{3}\right)^4 + \left(\frac{1}{3}\right)^5$ $= \frac{17}{81} \text{ or } 0.210 \text{ (3 sf)}$ | M1 M1 A1 [3] | Or $1 - P(3,4,5)$ Attempt at correct expression Allow 0.21 |
| (iii) | Est $\text{Var}(P_s) = \frac{0.625 \times (1 - 0.625)}{80}$ $\left(= \frac{3}{1024} \right)$ $z = 2.054 \text{ (or } 2.055)$ $0.625 \pm z \times \sqrt{\frac{3}{1024}}$ $= 0.514 \text{ to } 0.736 \text{ (3 sf)}$ | M1 B1 M1 A1 [4] | Any z |